

Section 4: Mathematics / Biology

Students will have to attempt either Mathematics/Biology as per the eligibility of the program applied.

Mathematics

66. The solution of the equation $\log_5 \sqrt{x-5} - \sqrt{x} = 0$ is
 (a) 2 (b) 4 (c) 3 (d) 8
67. Let $\frac{1}{q+r}, \frac{1}{r+p}$ and $\frac{1}{p+q}$ are in A.P. where $p, q, r, \neq 0$, then
 (a) p, q, r are in A.P. (b) p^2, q^2, r^2 are in A.P.
 (c) $-\frac{1}{pq}, \frac{1}{r}$ in A.P. (d) none of these
68. If $b \in \mathbb{R}^+$ then the roots of the equation $a^2 - b^2x^2 + 3b^2x - 4b^2 = 0$ is
 (a) real and distinct (b) real and equal (c) imaginary (d) cannot predicted
69. Solve for integral solutions $x_1 + x_2 + x_3 + \dots + x_6 = 17$, where $1 \leq x_i \leq 6, i = 1, 2, \dots, 6$.
 Number of solutions will be
 (a) $17C_6 - 6 \cdot 11C_5$ (b) $17C_6 - 6 \cdot 11C_5$ (c) $17C_6 - 6 \cdot 11C_5$ (d) $17C_6 - 5 \cdot 11C_6$
70. The probability that a certain beginner at golf gets a good shot if he uses the correct club is $\frac{1}{3}$ and the probability of a good shot with an incorrect club is $\frac{1}{4}$. In his bag there are 5 different clubs, only one of which is correct for the shot in question. If he chooses a club at random and take a stroke, the probability that he gets a good shot is
 (a) $\frac{1}{3}$ (b) $\frac{1}{12}$ (c) $\frac{4}{15}$ (d) $\frac{7}{12}$

71. OPQR is a square and M, N are the middle points of the side PQ and QR respectively. Then the ratio of the area of the square and the triangle OMN is

- (a) 4 : 1 (b) 2 : 1 (c) 4 : 3 (d) 8 : 3

72. Two vertices of an equilateral triangle are $(-1, 0)$ and $(1, 0)$ and its circumcircle is

- (a) $x^2 + y^2 - \frac{1}{\sqrt{3}}x - \frac{4}{3}$ (b) $x^2 + y^2 - \frac{1}{\sqrt{3}}x - \frac{4}{3}$
 (c) $x^2 + y^2 - \frac{1}{\sqrt{3}}x - \frac{4}{3}$ (d) none of these

73. If in a $\triangle ABC$, $\sin 2A + \sin 2B + \sin 2C = 2$, then the triangle is always

- (a) isosceles triangle (b) right angled (c) acute angled (d) obtuse angled

74. If the vertex and the focus of a parabola are $(-1, 1)$ and $(2, 3)$ respectively, then the equation of the directrix is

- (a) $3x + 2y - 25 = 0$ (b) $x + 2y + 7 = 0$ (c) $2x - 3y + 10 = 0$ (d) $3x + 2y + 14 = 0$.

75. The radius of the circle passing through the foci of the ellipse $\frac{x^2}{16} + \frac{y^2}{9} = 1$ and having its centre at $(0, 3)$ is

- (a) 4 (b) 3 (c) $\sqrt{12}$ (d) $7/2$

76. If $P(x_1, y_1)$, $Q(x_2, y_2)$, $R(x_3, y_3)$ and $S(x_4, y_4)$ are four concyclic points on the rectangular hyperbola $xy = c^2$, then the co-ordinates of the orthocentre of $\triangle PQR$ are

- (a) $(x_4, -y_4)$ (b) (x_4, y_4) (c) $(-x_4, -y_4)$ (d) $(-x_4, y_4)$

77. The coefficient of $x^n y^n$ in the expansion of $[(1 + x)(1 + y)(x + y)]^n$ is

- (a) $\sum_{r=0}^n C_r$ (b) $\sum_{r=0}^n C_2$ (c) $\sum_{r=0}^n C_3$ (d) none of these

78. z_0 is one of the roots of the equation $z^n \cos^{n-1} \theta + z^{n-1} \cos^{n-2} \theta + \dots + \cos \theta = 2$, where $\theta \in \mathbb{R}$, then

- (a) $|z_0| = \frac{1}{2}$ (b) $|z_0| = \frac{1}{2}$ (c) $|z_0| = \frac{1}{2}$ (d) none of these

79. The second order differential equation is

- (a) $y'' + x + y^2$ (b) $y'' + y = \sin x$ (c) $y'' + y'' + y = 0$ (d) $y'' = 0$

80. $\int e^{3x} \frac{3 \sin x}{1 + \cos x} dx$ is equal to

- (a) $e^{3x} \cot x + c$ (b) $e^{3x} \tan \frac{x}{2} + c$ (c) $e^{3x} \sin x + c$ (d) $e^{3x} \cos x + c$

81. If m and n are positive integers and $f(x) = \frac{1}{x} \sin \frac{x}{m} \cos \frac{x}{n}$

- (a) $x = b$ is a point of local minimum (b) $x = b$ is a point of local maximum
 (c) $x = a$ is a point of local minimum (d) $x = a$ is a point of local maximum

82. If in a triangle ABC $\frac{2 \cos A}{a} = \frac{\cos B}{b} = \frac{2 \cos C}{c} = \frac{a}{bc} = \frac{b}{ca}$, then the value of the angle A is

- (a) 45° (b) 90° (c) 135° (d) 60°

83. The general solution of the equation $2 \cos 2x - 3 \sin^2 x = 0$ is

- (a) $n\pi$ (b) $n\pi + \frac{\pi}{2}$ (c) $n\pi + \frac{\pi}{2}$ (d) all of the above.

84. Total number of positive real values of x satisfying $2[x] = x + \{x\}$, where $[.]$ and $\{.\}$ denote the greatest integer function and fractional part respectively is equal to

- (a) 2 (b) 1 (c) 0 (d) 3

85. If $\lim_{x \rightarrow 0} \frac{(a^n - n x^n + \tan x) \sin nx}{x^2} = 0$, where n is nonzero real number, then a is equal to

- (a) 0 (b) $\frac{n-1}{n}$ (c) n (d) $n + \frac{1}{n}$

86. $f(x) = \frac{4x^3 - 3x^2 + \ln a}{x^3 + 18}$. Find the complete set of values of a such that

- $f(x)$ has a local minima at $x = 3$ is
 (a) $[-1, 2]$ (b) $(-\infty, 1) \cup (2, \infty)$ (c) $[1, 2]$ (d) $(-\infty, -1) \cup (2, \infty)$

87. The number of values of k for the system of equations $(k + 1)x + 8y = 4k$ and $kx + (k + 3)y = 3k - 1$ has infinitely many solutions

- (a) 0 (b) 1 (c) 2 (d) infinite

88. The matrix $\begin{bmatrix} 1 & i \\ 2 & i \\ 1 & i \\ 2 \end{bmatrix}$ is

- (a) unitary (b) null matrix (c) symmetric (d) none of these

89. The area between the curves $y = x e^x$ and $y = x e^{-x}$ and the line $x = 1$ is

- (a) $2e$ (b) e (c) $2/e$ (d) $1/e$

90. If the unit vectors \vec{a} and \vec{b} are inclined at an angle 2θ and $|\vec{a} \cdot \vec{b}| < 1$ then θ lies in the interval

- (a) $0, \frac{\pi}{6}$ (b) $\frac{\pi}{6}, \frac{\pi}{2}$ (c) $\frac{\pi}{6}, \frac{\pi}{3}$ (d) $\frac{\pi}{2}, \frac{5\pi}{6}$