FINAL JEE-MAIN EXAMINATION - APRIL, 2023

(Held On Tuesday 11 April, 2023)

MATHEMATICS

SECTION-A

value ١. The of integral $\frac{\log_e^2}{e^x} \left(\frac{\log e}{1+e^{2x}} \right) dx_{\text{equal to}}$

(1)
$$\log \frac{\cancel{x}}{\cancel{y}} = \frac{1}{1} + \frac{5}{\cancel{y}} = \frac{5}{\cancel{y}}$$

(r) loge
$$\hat{\xi}$$
 $2(3-5)\ddot{0}$ $\div + 5$ $\ddot{\phi}$ 2

(1)
$$\log \frac{2}{c}$$
 2(2
(1) $\log \frac{2}{c}$ 1+ 5) $\frac{1}{6}$ 5
 $\frac{2}{c}$ 2
(2) $\frac{2}{c}$ 2(3-5) $\frac{1}{6}$ 5
 $\frac{1}{c}$ 4+ 5 $\frac{1}{6}$ 2
(2) $\frac{2}{c}$ 2(2+5) $\frac{1}{6}$ 6
(3) $\frac{1}{c}$ 2(2+5) $\frac{1}{6}$ 6
(4) $\frac{1}{c}$ 1+ 5 $\frac{1}{6}$ 2
(5) $\frac{1}{c}$ 2 (2+5) $\frac{1}{6}$ 6
(6) $\frac{1}{c}$ 1+ 5 $\frac{1}{6}$ 2

(1)
$$\log \frac{2(2+5)}{6}$$
 $\frac{3}{2}$ $\frac{3}{2}$

Official Ans. by NTA(§)

Sol. $I = \mathring{o}ex(1n(ex))dx$

Put $ex = t \Rightarrow edx = dt$

$$I = \frac{2}{10} ln(t_1 + t^2)$$

Applying integration by parts.

=
$$2 \ln (2 + 5) - \frac{1 \ln 20 + 5}{2 \text{ cc}} + \frac{5 \text{ c}}{2} + \frac{3}{6} + \frac{3}{12} + \frac{1}{12} + \frac{1}{12} = \frac{1}{12}$$

=
$$2\ln(2 + 5)$$
 - $\frac{1 \ln 2 + 5 \ddot{0}}{2 \text{ cçè}}$ - $\frac{5}{2}$ - $\frac{5}{2}$

TIME: 9:00 AM to 12:00 NOON

TEST PAPER WITH SOLUTION

۲. If equation of the plane that contains the point (۲٬۳٬۰) and is perpendicular to each of the planes

$$2x+4y+5z=8$$
 and $3x-2y+3z=5$ is

ax+by+gz+97=0then a+b+g=

- (٢) ١٧
- (٣) 17
- (٤) 10

Official Ans. by NTA(§)

Sol. The equation of plane through (-۲,۳,۵) is

$$a(x+r) + b(y-r) + c(z-0) = .$$

it is perpendicular to \x+\(\x\)+\(\overline{z}=\Lambda\&\rx\-\x\y+\rz=\overline{a}

$$2a+4b+5c=0$$

$$3a-2b+3c=0$$

$$\Rightarrow \frac{a}{22} = \frac{b}{9} = \frac{c}{-16}$$

Equation of Plane is

$$22(x+2)+9(y+3)-16(-z_5=0)$$

$$b = 22x + 9y - 16z + 97 = 0$$

Comparing with
$$x+by+gx+97=0$$

We get_a +
$$b$$
 + g = 22+9-16=15

١

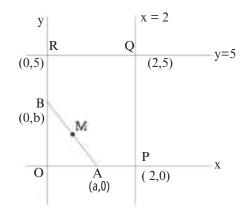
> divides the area of the rectangle R in the ratio 1:1. Then, the mid-point of AB lies on a (1) parabola

- (শ) hyberbola
- (۳) straight line
- (٤) circle

Official Ans. by NTA (Y)

Sol.
$$\frac{\text{ar OPQR}}{\text{or (OA}} \bar{B}^{1}$$

Let M be the mid-point of AB.



$$M(h,k^{\circ}) = \frac{c}{2}, \frac{b}{2} = \frac{\ddot{o}}{\dot{a}}$$

$$\Rightarrow \frac{10^{1} \frac{1}{2}ab}{\frac{1}{2}ab} = 4$$

$$\Rightarrow \frac{5}{2}ab = 10 \Rightarrow ab = 4$$

$$> 2h)2K)=4$$

\ Locus of M is xy = \

Which is a hyperbola.

Let sets A and B have o elements each. Let the mean of the elements in sets A and B be o and A respectively and the variance of the elements in sets A and B be or and rorespectively A new set C of orelements is formed by subtracting refrom each element of A and adding rote each element of B. Then the sum of the mean and variance of the elements of C is

Official Ans. by NTA (Y)

Sol.
$$wA=\{a_1,a_2,a_3,a_4,a_5\}$$

 $B=\{b_1,b_2,b_3,b_4,b_5\}$

$$\tilde{Now}_{C}$$
 = $\{C1$, $C2$, $\overset{\scriptscriptstyle i=1}{\ldots}$ $C10$

Mean of
$$C_{\cdot C} = \frac{(\mathring{a} \text{ ai} - 15) + \mathring{a} \text{ bi} + 10)}{10}$$

$$C = \frac{10 + 50}{10} = 6$$

\

Mean + Variance=
$$\overline{C} + s2 = 6 + 32 = 38$$

- \circ . Let f(x)=x2-x+|-x+[x]|, where
- xΡand
- denotes the greatest integer less than or equal t0 |ai| < 1, i=1,2,3, consider
- t. Then، f is
- (1) continuous at $x = \cdot$, but not continuous at x = 1
- (Y) continuous at $x = \cdot$ and $x = \cdot$
- (τ) not continuous at $x = \cdot$ and $x = \cdot$
- (٤) continuous at x = ١، but not continuous at x = •
 Official Ans. by NTA (٤)
- Sol. Here $f(x) = \dot{e}\dot{e}x(x-1\dot{u}\hat{u}+x)$

f o)=-1+0=-1	f1+ =0+0=0
f(o) =0	f1)=0
	f(1-)-1+1=0

- f(x) is continuous at x = \(\cdot\) discontinuous at x = \(\cdot\)
 The number of triplets (x, y, z), where x, y, z are
 - distinct non negative integers satisfying X + Y + Z = 10, is
 - (1) A+
 - (٢) 11 ٤
 - (٣) 97
 - (٤) ١٣٦

Official Ans . by NTA (Υ)

Sol. X + y + Z = 10

Total no . of solution = 10+45-11+977 ...(1) Let x=y¹z

2x+z=15bz= 15-2t

ÞrÎ{0,1,2,...7}-{5

- v solutions
- there are Y solutions in which exactly
- Two of x \ y \ z are equal
- ...(٢)
- There is one solution in which x=y=z ... (r)
- Required answer = 177-71-1 = 115

- v. For any vector $a=a\hat{1}i+a_2\hat{j}+a3k\hat{l}$ with equal t0|ai|<1,i=1,2,3,consider the following statements:
 - (A): $\max \{|a1|, |a2|, |a3|\} \pounds |a|$
 - (B): $|a|£3max {|a1|, |a2|, |a3|}$
 - (1) Only (B) is true
 - (Y) Only (A) is true
 - (٣) Neither (A) nor (B) is true
 - (\mathfrak{t}) Both (A) and (B) are true

Official Ans. by NTA(٤)

Sol. Without loss of generality

$$|^{r2}$$
 =a1|² +a2|² +a3|² 3(a3)²

$$a^{3}a3 = max\{a1,a2,a3\}$$

A is true

$$\left|\frac{2}{3}r\right|^{2} = \frac{1}{5}a^{2}\left|\frac{2}{3}a^{2}\right|^{2} + a^{2}\left|\frac{2}{3}a^{2}\right|^{2} + a^$$

þþ | 3

$$a£3a3=3maxa1,a2,a3$$

£ 3 $\max\{aa2, a3\}$

(Y) is true

A. Let w \ be the point obtained by the rotation of $z_1 = o + εi$ about the origin through a right angle

in

the anticlockwise direction, and we be the obtained by the rotation of $z_1 = r + oi$ about the origin; through a right angle in the clockwise will be a small of which are the principal argument of the princi

equal to $\frac{33}{5}$

(1) -p+tan-1 (Y) -p-

(r) -p+ $\frac{\tan -18}{9}$

 $(\mathfrak{t}) \quad \mathsf{p-} \quad \tan^{-1} \frac{\mathsf{8}}{\mathsf{9}}$

Official Ans . by NTA (٤)

Sol.
$$W1 = zii = 5 + 4ii = -4 + 5i$$

...(i

$$W2=z/2-i)=(3+5i(-i=5-3i...(2))$$

W1-W2=-9+8i

- An organization awarded £A medals in event 'A' .

 10 in event 'B' and 1A in event 'C'. If these medals went to total 11 men and only five men got medals in all the three events 1 then 1 how many received medals in exactly two of three events?
 - (1) 1 •
 - (٢) ٩
 - (٣) ٢1
 - (٤) 10

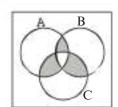
Official Ans . by NTA (*)

Sol.
$$A=48$$

$$|B|=25$$

$$C=18$$

$$|ACBC| = 5$$



= ٣٦

No . of men who received exactly τ medals

= ۲1

Let $S=\{M=[a\ ij],\ aij\ \hat{I}\{0,1,2\},1\ \pm i,j\pm 2\}$ be a sample space and $A=\{M\ \hat{B}:M\ is\ invertible\}$ be an event. Then P(A) is equal to

- (1) $\frac{50}{81}$
- $(7) \frac{47}{81}$
- (r) $\frac{49}{81}$
- (£) <u>16</u>

Official Ans. by NTA(1)

Sol.
$$\mathbf{M} \stackrel{\text{\'ea}}{\underset{\text{c}}{\overset{\text{bù}}{\text{d\'u}}}} \stackrel{\text{bù}}{\underset{\text{d\'u}}{\text{d\'u}}} \text{, where a. b. c. } \mathbf{\mathring{g}} \text{, } \{0,1,2\}$$

we first boun $\phi(A)$

$$|\mathbf{m}| = 0 \, \mathsf{P} \quad \mathsf{ad} = \mathsf{bc}$$

ad=bc= \cdot P no. of (a,b,c,d) = ($\tau\tau$ - $\tau\tau$) τ = τ 0 ad=bc= τ 1 P no. of (a,b,c,d) = $\tau\tau$ 2 ad=bc= τ 2 P no. of (a,b,c,d) = $\tau\tau$ 3 = $\tau\tau$ 4 ad=bc= τ 5 P no. of (a,b,c,d) = $\tau\tau$ 5 ad=bc= τ 5 P no. of (a,b,c,d) = $\tau\tau$ 5 ad=bc= τ 7 P no. of (a,b,c,d) = $\tau\tau$ 7 = τ 8

$$P(A) = \frac{31}{81} P(A) = \frac{50}{81}$$

11. Consider ellipses **k**: kxx+kxyx=1, k=1, x,

r.. Let Ck be the circle which touches the four chords joining the end points (one on minor axis and another on major axis) of the ellipse Ek. If rk is

the radius of the cirle Ck $_{\rm c}$ then the value of a 1 $_{k=1^2{\rm rk}}^{26}$ is

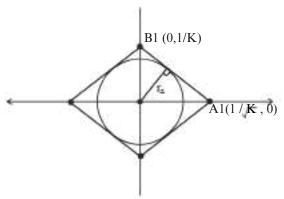
- (1) * 4 •
- (1) 771.
- (٣) ٣٣٢.
- (٤) ٢٨٧٠

Official Ans. by NTA (1)

Sol.
$$Kx2+ K2y21$$

$$\frac{x^2}{1/K} + \frac{y^2}{1/K^2} = 1$$

Now



Equation of

A1B2; x +
$$\frac{y}{1/\sqrt{K}}$$
 = 1 b $\sqrt{Kx + Ky}$ = 1

 $r_{K} = ^{r} distance of(\cdot, \cdot) from line A_{B_{1}}$

$$r_k = \frac{(0+0-1)}{K+K2} = \frac{1}{K+K2}$$

$$=\frac{20'21}{2}+\frac{20.21.41}{6}$$

$$=210+10'7'41$$

$$=210 + 2870$$

$$=3080$$

 $\ensuremath{\text{1}}\ensuremath{\text{r}}.$ The number of integral solutions x of

$$\log_{\overset{\leftarrow}{\mathbb{R}}^{x}+2\frac{3}{2}\overset{\leftarrow}{\mathbb{R}}} \frac{\overset{\rightarrow}{\mathbb{R}}^{2}}{(x-3)} \stackrel{\overset{\rightarrow}{\mathbb{R}}^{2}}{\overset{\rightarrow}{\mathbb{R}}} {}^{3} \text{ 0 is}$$

(1) 7

 $(Y) \Lambda$

(۳) ه

(ξ) V

Official Ans. by NTA(1)

Sol.
$$\log_{x+7} e^{x-7} \dot{g}^{2} = 2x-3 \dot{g}^{3} = 0$$

Feasible region_X + $\frac{7}{2}$ 0 \(\text{v} \) x > - $\frac{7}{2}$

And
$$x + \frac{7}{2} \not= 1^{1} - x$$
 5

And
$$\frac{x-7}{2x^3}$$
 0 and $2x-3$ 0 8 8 x^1 7 x 1 3

Taking intersection
$$\hat{x}^{\hat{1}} = \frac{7}{\hat{e}^2}, \hat{y}^{\hat{0}} = \frac{5}{\hat{e}^2}, \frac{3}{2}, 7\ddot{y}$$

Now $log b^3 0$ if a < 1 and b^3

$$\hat{\mathrm{al}}(0,1)$$
 and $\hat{\mathbf{l}}_{0,1}$

C- I;
$$x + \frac{7}{2} > 1$$
 and $e^{\frac{2}{3}} \frac{x - 7}{2x - 3} = \frac{\ddot{o}^2}{\dot{\phi}} = 1$

$$x > -\frac{5}{2}$$
 $(2x \cdot 3)^2 - (x - 7)^2 \notin 0$

$$2x-3+n-7$$
) $(2x-3-x+7) \in 0$

$$(3x-10)(x+40)$$

$$x\hat{1}e_{\hat{e}}^{-4}, 10\dot{u}_{3\dot{u}}$$

Intersection $\stackrel{\text{X}}{:} \stackrel{\text{fac-}}{=} \frac{5,10}{2} \stackrel{\text{Y}}{:} \frac{10}{3} \stackrel{\text{Y}}{:}$

C-II x
7
½ $\hat{\mathbf{1}}$ (0,1) and $^{\text{æ x-7}}_{\text{e2x-3+ø}}$ 2 $\hat{\mathbf{0}}$ $\hat{\mathbf{1}}$ (0 ,1)

$$0 < x \frac{7+}{2} < 1 \qquad \text{$\frac{2\ddot{0}}{2x-3}$} < 1$$

$$-\frac{7}{2} < x < \frac{2^5}{2} \qquad (2x-3)^2$$

$$x^{\hat{I}}$$
- $\overset{\text{\'e}}{(}$, $\overset{\text{\'e}}{(}$, $\overset{\text{\'e}}{(}$) $\overset{\text{IO}}{\overset{\text{\'e}}{(}}$, $\overset{\text{\'e}}{\overset{\text{\'e}}{(}}$

No common values of x.

Hence intersection with feasible region

Weget
$$x = \frac{1205,10}{5}$$
 $\frac{100}{2}$ $\frac{130}{3}$ $\frac{130}{5}$

Nr. Area of the region
$$\{(x,y):x2+(y-2)2 \not\in 4, x^2 \ni 2y\}$$
 is

(1)
$$2p - \frac{16}{3}$$

(Y)
$$p - \frac{8}{3}$$

$$(r) p + \frac{8}{3}$$

(1)
$$2p + \frac{16}{3}$$

Official Ans. by NTA(1)

Sol.
$$x2+(y-2)2£22$$
 and $x2^{3}2y$

 $Solving\ circle\ and\ parabola\ simultaneously:$

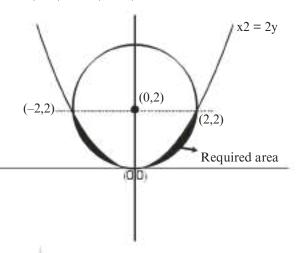
$$2y + y^2 - 4y + 4 = 4$$

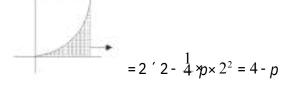
$$y^2 - 2y = 0$$

$$y = 0,2$$

Put
$$y = r in xr = ry \otimes x = \pm 2$$

P(Y,Y) and (-Y,Y)





Required area
$$2 \stackrel{\acute{e}}{\stackrel{?}{0}} \stackrel{?}{0} \stackrel{?}{2} = dx - (4 - p) \stackrel{\grave{v}}{\stackrel{\lor}{u}}$$

$$= 2 \stackrel{\acute{e}}{\stackrel{?}{0}} = -4 + p \stackrel{\grave{v}}{\stackrel{\lor}{u}}$$

$$= 2 \stackrel{\acute{e}}{\stackrel{?}{0}} = -4 \stackrel{\grave{v}}{\stackrel{\lor}{0}} = -4 \stackrel{\grave{v}}{\stackrel{\backprime}{0}} = -4 \stackrel{\grave{v}}{\stackrel{}{\stackrel{\lor}{0}} = -4 \stackrel{\grave{v}}{\stackrel{}{\stackrel{}{0}} = -4 \stackrel{v}{\stackrel{}{\stackrel{}{0}} = -4$$

Let f:[2,4] be a differentiable function such that $\log x$ if $f(x) \log x$ $f(x)^{3}$.

$$x\hat{I}[2,4]$$
 with $f(2) = \frac{1}{2}$ and $f(4) = \frac{1}{4}$.

Consider the following two statements:

(A) :
$$f(x)E_1$$
, for all $x\hat{I} = Y$, ξ

(B):
$$f(x) = \frac{1}{8}$$
, for all $x\hat{l} = x$, ξ

Then،

(1) Only statement (B) is true

(y) Neither statement (A) nor statement (B) is true

 (Υ) Both the statement (A) and (B) are true

(٤) Only statement (A) is true

Official Ans. by NTA (*)

Sol.
$$x \ln x f'(x) + \ln x f(x) + f_x$$
 3 I.xî 2,4]

And
$$f(r)=,f(4)^{1}$$

Now
$$x \ln x dy + (\ln \frac{1}{4}1)y^3$$

$$\frac{d}{dx}(f(x).x\ln x)^{3}1$$

d

dx

$$\Rightarrow \frac{d}{dx}(x\ln x f(x)-x)^3 02x\hat{A}$$

 \Rightarrow The function $g(x) = x \ln_X f(x) - x$ is increasing in

And
$$g(2 = 21n 2(f 2) = 1n 2 - 2$$

$$g(4 = 4\ln 4f)(4 = \ln 4 - 4)$$

$$=2(1n2-2)$$

Now $g(2) \in g(X) \in g(4)$

$$ln2-2£ xlnxf ()-x£2(ln2-2)$$

$$\frac{1112-2}{x \ln x} + \frac{1}{\ln x} \mathcal{E} f(x) \mathcal{E} \frac{2 \ln 2-2}{x \ln x} + \frac{1}{\ln x}$$

Now for
$$\hat{1}$$
 2,4

$$\frac{2 \ln 2 - 2}{x \ln x} + \frac{1}{\ln x} < \frac{2(\ln 2 - 2)}{2 \ln 2} + \frac{1}{\ln 2} = 1 - \frac{1}{\ln 2} < 1$$

$$\triangleright f(x) \le 1 \text{ for } x \ \hat{I} = [2,4]$$

Alsoforx $\hat{1}$ 2,4]:

$$\frac{\ln 2-2}{\ln x} + \frac{1}{\ln x}^3 + \frac{\ln 2-2}{4\ln 4} + \frac{1}{\ln 4} = \frac{1}{8} + \frac{1}{2\ln 2} > \frac{1}{8}$$

$$Pf(x)^3 = \frac{1}{8} for x \hat{I} \text{ where } x \text{ is the property of } x \text{ is the property of } x \text{ in } x \text{ is the property of } x \text{ in } x \text{ is the property of } x \text{ in } x \text{ is the property of } x \text{ in } x \text{ is the property of } x \text{ in } x \text{ in$$

Hence both A and B are true.

 $LMVT \ on \ (yx \ (lnx)) \ not \ satisfied \ .$

Hence no such function exists.

Therefore it should be bonus.

Let y = y(x) be a solution curve of the differential equation, (1-x2y2)dx=ydx+xdy. If the line x = x intersects the curve y = y(x) at y = x and the line x = x intersects the curve y = y(x) at y = y(x) at y = a, then a value of ais

(1)
$$\frac{3e2}{2(3e2-1)}$$

$$\begin{array}{c}
3e2 \\
2(3e2 + 1) \\
1-3e2
\end{array}$$

(r)
$$2(3e2 + 1)$$

 $1 + 3e2$

Official Ans . by NTA (\mathfrak{t})

sol.
$$1-x2y2)dx=ydx_{yy}(1)=2$$

$$y(2 = \mu = ?$$

$$dx = \frac{d xy}{1 - (xy)^2}$$

$$\partial dx \partial \frac{d xy}{1 - (xy)}$$

$$x = \frac{1}{2} \ln \frac{1 + xy}{1 - xy} + C$$

Put x = 1 and y = Y :

$$1 = \frac{1}{2} \ln \frac{1+2}{1-2} + C$$

$$C = 1 - \frac{1}{2} \ln 3$$

Now put x = r:

$$2 = \frac{1 \ln 1 + 2a}{2} + 1 \quad \frac{1}{2} \ln 3$$

$$1 \ln 1 + 2a$$

$$1 + \frac{1 \ln 3}{2} = \frac{1}{2} \quad \boxed{1 - 2a}$$

$$\left|\frac{1+2a}{1-2a}\right| = 3e2$$

$$\frac{1+2a}{1+2a} = 3e2, -3e2$$
 $\frac{1-2a}{1-2a} = 3e2$

=3e2
$$\Rightarrow \alpha = \frac{3e2-1}{2(3e2)}$$

And
$$\frac{1+2a}{1-2a} = -3e2 \, pa = \frac{3e2+1}{2(e2-1)}$$

. Let A be a $\tau \times \tau$ matrix with real entries such that A'=aA+I, where $a\hat{I}_i$ -{-1,1}. If det $(A\tau - A) = \epsilon$, then the sum of all possible values of ais equal to

$$(7) \frac{3}{2}$$

Official Ans . by NTA (r)

Sol.
$$AT = a A + I$$

$$A = a AT + I$$

$$A \neq a(aA + I)$$

$$A \notin {}^{a2A + a + 1}I$$

$$1 - a2 = a + 1)I$$

$$A = \frac{I}{1 - a} \qquad \dots$$

$$|A| = \frac{1}{(1-\alpha)2} \qquad \dots (7)$$

$$|A2 - A| = |AA - I|$$
 ...(r)

$$A - I = \frac{I}{1 - a} \qquad \frac{a}{1 - a} I$$

$$|\mathbf{A} - \mathbf{I}| = \underbrace{\mathbf{e} \mathbf{c} \ a}_{\mathbf{I}} \underbrace{\mathbf{o}^{2}}_{\mathbf{I}} \dots (\mathfrak{t})$$

Now
$$|A2-A| = 4$$

$$\begin{vmatrix} A | A - I | = 4 \\ 1 \end{vmatrix}$$

$$\frac{1}{(1-a)^2} \frac{a^2}{(1-a)^2} = 4$$

$$\Rightarrow \frac{a}{(1-a)2} = \pm 2$$

$$\Rightarrow 2(1-a)2 = \pm a$$

(C₁)
$$2(1-a^{-2}=a)$$
 (C₁) $7(-a)3=-a$
 $2a2-5a+2=0 $2a2-3a+2=0$
 $a1+a2=\frac{5}{2}$ $a\ddot{1}R$$

 $_{\text{Sum}}$ of value of \underline{a} $\frac{5}{2}$

Let (a, b, g)be the image of the point P(Y,

the plane $\forall x + y - \forall z = 1$. Then a+b+g is equal

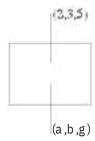
to

- (1)1.
- (٢)0
- (٣) 11
- (٤) ٩

Official Ans. by NTA(1)

Sol.
$$\frac{a-2}{2} = \frac{b-3}{1} = \frac{g-5}{-3} = \frac{2 \text{ ex} (2+3-3) \cdot 5-6 \circ \frac{3}{6}}{\frac{1}{6} \cdot 22+12+1-32 \circ \frac{3}{6}} = 2$$

$\frac{a-2}{2}=2$	b - r = r	g-0=-7
a = 6	D = 0	g = - \



$$a + b + g = 10$$

Let a be a non-zero vector parallel to the line of intersection of the two planes described by i+sj, i+k, and i-sj, sj-k, Ifq is the angle

between the vector a and the

$$(7) \begin{array}{c} & & & & & \\$$

Official Ans. by NTA(1)

Sol. n^{γ} and n^{γ} are normal vector to the plane \hat{i}_{+} \hat{j} , \hat{i}_{+} \hat{k} and \hat{i} $-\hat{j}$ \hat{j} $-\hat{k}$ respectively

$$\mathbf{f}_{1} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{j} \\ 1 & 1 & 0 \\ 1 & 0 & 1 \end{vmatrix} = \mathbf{i}\hat{\mathbf{j}} - \mathbf{k}$$

$$\hat{\mathbf{i}} \quad \hat{\mathbf{j}} \quad \hat{\mathbf{j}}$$

$$\mathbf{f}_{1} = \begin{bmatrix} \hat{\mathbf{i}} & \hat{\mathbf{j}} & \hat{\mathbf{j}} \\ 1 & -1 & 0 \\ 1 & 0 & -1 \end{bmatrix} = \hat{\mathbf{i}} + \hat{\mathbf{j}} + \hat{\mathbf{k}}$$

$$\ddot{a} = l \mid n_2^{r}, \ddot{n}_2$$

$$= l \begin{vmatrix} \hat{i} & \hat{j} & k \\ 1 & -1 & -1 \\ 1 & 1 & 1 \\ 0 + 4 + 2 \end{vmatrix} = l(-2\hat{j} + 2\hat{k})$$

$$\begin{bmatrix} x \\ b \\ b \\ l = 1 \end{bmatrix} = 6$$

$$p \begin{vmatrix} \hat{i} \\ b \\ k \end{vmatrix} = 6$$

$$p \begin{vmatrix} \hat{i} \\ b \\ k \end{vmatrix} = 6$$

$$p \begin{vmatrix} \hat{i} \\ a \\ cos \end{vmatrix} = \frac{\hat{i} \\ a \\ b \end{vmatrix}$$

$$\cos q = \frac{6}{2\sqrt{2} \cdot 3} = \frac{1}{\sqrt{2}}$$

$$q^{p=}{q\over 4}$$

Now
$$|\vec{a}.\vec{b}|^2 + |\vec{a}'.\vec{b}|^2 = |a|^2 |b|^2$$

 $36 + |\vec{a}'.b|^2 = 8'.9 = 72$

$$ab'b = 6$$

The number of elements in the set
$$S = \hat{q} \hat{1}$$
 where $\hat{q} = \hat{q} \hat{q} + \hat{q} = \hat{q}$

Official Ans. by NTA (*)

Sol.
$$3\cos 4q - 5\cos 2q - 2\sin 6$$
 $q + 2\theta$

$$\Rightarrow 3\cos 4q - 3\cos 2q - 2\cos 2q - 2\sin 6q + 2 = 0$$

$$\Rightarrow 3\cos 4q - 3\cos 2q + 2\sin 2q - 2\sin 6q = 0$$

b
$$3\cos 2q(\cos 2q + 1) + 2\sin^2 q(\sin^4 q - 1) = 0$$

$$-3\cos 2q\sin 2q + 2\sin^2 q \left(1 + \sin 2q \cos 2q - 1\right)$$

$$\Rightarrow \frac{-3\cos 2q\sin 2q + 2\sin 2q}{|q|} = \frac{\cos 2q}{|q|}$$

$$\Rightarrow si 2q cos 2q(+2sin -3=0)$$

n
$$2q\cos 2q 2\sin q - 1 = 0$$

(C1)
$$\sin 2q = 0$$
 ® resolution $q = 0, p, 2p$

(C₁)
$$\cos 2q = 0$$
 \circ r solution $q = i i \frac{p}{2}$, $3p\ddot{u}$

(Cr)
$$\sin q = \frac{1}{2}$$
 ® ε solution $\dot{q} = \frac{1}{14} \frac{1}{4} \frac{1}{4}$

Let x1, x2, x100 be in an arithmetic progression,

with x1 = 2 and their mean equal to 200. If

yi = i xi - i), \frac{1}{2} i \frac{1}{2} \ldots \cdot \text{then the mean of y \ldots y \text{y \cdot \cdot }.

Official Ans by NTA (+)

Sol. Mean = Y · ·

$$\frac{\frac{100}{2}(2'2+99d)}{\frac{100}{100}} = 200$$

$$\Rightarrow$$
 4+99d = 400

$$yi = i(xi-i)$$

$$=i(2 i-1)4-i)=3i2-2i$$

$$\text{Mean} = \overset{\mathring{a}}{100} \overset{\mathring{a}}{10} \overset{\mathring{a}}{100} \overset{\mathring{a}}$$

$$= \frac{1^{\overset{100}{a}}3i2-2i}{100 i=1}$$

$$= \frac{1 i 3' 100' 101' 201}{6} - \frac{2' 100' 101}{2} \ddot{y}$$

=101
$$\hat{i}$$
201 -1 \hat{u} \hat{y} =101'99.5

$$=10049.50$$

SECTION-B

- Sol. Coefficient of_x =9C₂8 Of x2=9C₂2⁷ Of x7=9C7 &2 Mean = $\frac{{}^{9}C_{1} \times 2^{8} + {}^{9}C_{2} \times 2^{7}..... + {}^{9}C_{7}}{7}$ = $\frac{(1+2)^{9} - {}^{9}C_{0} \cdot 2 - {}^{9}C_{8} \times {}^{1}2 \cdot {}^{9}C_{9}}{7}$ = $\frac{3^{9} - 29 - 18 - 1}{7}$ = $\frac{19152}{7} = 2736$
- YY. Let $S = 1 \cdot 9 + \frac{1 \cdot 1}{0} + \frac{1 \cdot 1}{0} + \dots + \frac{1}{0} + \frac{1}{0} + \dots + \frac{1}{0} + \frac{1}{0} + \dots + \frac{1}{0} + \frac{1}{0} + \dots + \frac{$

Sol.
$$S=109 + \frac{108}{5} + \frac{107}{5} \cdot ... \frac{1}{5108^{08}}$$

$$\frac{S}{S} = \frac{109}{5} + \frac{1008}{5100} \cdot ... + \frac{1}{5109}$$

$$\frac{4S}{5} = \frac{109 - 1}{5} \cdot \frac{1}{5100} \cdot \frac{1}{5100} \cdot \frac{1}{5109}$$

$$= 109 - \frac{1}{6} \cdot \frac{1}{6} \cdot \frac{1}{5100} \cdot \frac{1}{6} \cdot \frac{1}{5100} \cdot \frac{1}{6} \cdot \frac{1}{5109}$$

$$= 109 - \frac{1}{4} \cdot \frac{1}{4} \cdot \frac{1}{5109} \cdot \frac{1}{5109} \cdot \frac{1}{6} \cdot \frac{1}{5109} \cdot \frac{1}{6} \cdot \frac{1}{6}$$

- For m, $n < \cdot$, let $a = (m, n) = (m, r) \cdot (m + r) \cdot$
- Sol. $a(m,n) \stackrel{?}{\underset{0}{\circ}} t \stackrel{?}{\underset{0}{\circ}} t$
- In an examination of students have been allotted their seats as per their roll numbers.

 The number of ways in which none of the atlodterdseits on the Official Ans. by NTA (££)
- Sol. Derangement of o students

$$D5 = {}^{5!} \frac{\&}{\&} 1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} + \frac{1}{4!} - \frac{1}{5!} \frac{\ddot{o}}{\ddot{\phi}}$$

$$= 120 \frac{\&}{\&} 2 - \frac{1}{6} + \frac{1}{24} - \frac{1}{120} \frac{\ddot{o}}{\ddot{\phi}}$$

$$= 60 - 20 + 5 - 1$$

$$= 40 + 4$$

$$= 44$$

Let a line I pass through the origin and be 10. perpendicular to the lines

$$I_{i} : \Gamma = i (1) \cdot j - vk + (\$^{r} \cdot j + rk \cdot l \hat{I}_{i})$$

and
$$i : f = -\$i + k\$ + m(Y \$ i \$ j_+ k\$) m \hat{I}_i$$

If P is the point of intersection of I and I ι and $\mathbb{Q}(a)$ ، b، g) is the foot of perpendicular from P on lر then $\P(a+b+g)$ is equal to ______.

Official Ans. by NTA (a)

Sol. Let
$$I = 0i^+ 0j^+ 0k^- + gai^+ bj^+ ck^-$$

$$= g a i^+ bj^ck^-$$

$$ai_{+}^{2}bj_{+}^{2}ck_{-}^{2}\begin{vmatrix} \hat{i} & \hat{j} & k \\ 1 & 2 & 3 \\ 2 & 2 & 1 \end{vmatrix}$$

$$= \hat{i} \quad \underset{4 = \hat{i} \\ 5 = \hat{i}}{2 - 6} - \hat{j}_{k} (1 - 6) k^{2} (24)$$

$$I = g(-4i^+5j^-2k^-)$$

P is intersection of and 1,

$$-4g = 1 + l$$
, $5g = -11 + 2$ $l - 2g = -+7$ $3l$ By solving there equation $P(\xi_1 - \xi_2)$

Let Q(-1+2m,2m,1+m)

$$\mathbf{PQ} \times (2\mathbf{i}^2 + 2\mathbf{j}^2 + \mathbf{k}^2) = 0$$

-2+4m+4m+1+m=0

$$9m = 1$$

$$m = \frac{1}{9}$$

$$Q = \frac{2}{\xi} = \frac{7}{9}, \frac{2}{9}, \frac{105}{9} = \frac{2}{9}$$

$$9(a b+g) = 9\xi = \frac{2}{9} + \frac{2}{9} + \frac{10}{9} = \frac{5}{9}$$

The number of integral terms in the expansion of $\overset{\text{e}}{\xi}$

Official Ans. by NTA (1V1)

Sol. The number of integral term in the expression of

$$\overset{\text{æ}}{\underset{\text{c}}{\overset{1}{32}}} + \overset{1}{\overset{0}{\overset{\circ}{54}}} \overset{\circ}{\overset{\circ}{\overset{\circ}{500}}} \text{ is equal to}$$

$$=6806^{\frac{680-r}{2}}5^{\frac{r}{4}}$$

Value's of r، wher ﴿ goes to integer

 $\begin{array}{lll} r=\cdot,\,\, \xi,\, \lambda,\,\, \text{NY},\,\, \dots\,\, \dots\,\, \text{NA}\cdot\\ \text{All value of } r\,\, \text{are accepted fo}_{680}-r\\ \text{No of integral terms} &=&\,\, \text{NY}\cdot\,\, \text{Line} \\ \text{numbers of} \end{array}$ ordered triplets of the truth values of pagandr such that the truth value of the statement (pÚq)Ù(pÚr)Þ(qÚr)is True, is

equal to ______ . Official Ans. by NTA (v)

Sol.

р	q	r	Pvq	Pvr	(pvq) Ù (pvr)	qvr	(pvq) Ù (pvr) ® qvr
Т	Т	Т	Т	T	Т	Т	Т
T	Т	F	Т	Т	Т	Т	т
Т	F	Т	Т	Т	Т	Т	т
Т	F	F	Т	Т	Т	F	F
F	Т	Т .	Т	Т	Т	Т	Т
F	Т	F	Т	F	F	Т	Т
F	F	Т	F	Т	F	Т	т
F	F	F	F	F	F	F	Т

Hence total no of ordered triplets are v

YA. Let
$$H_n = \frac{X^{\frac{1}{2}}}{1+n} - \frac{y^{\frac{1}{2}}}{r+n} = 1$$
, $n\hat{I}N$. Let k be the smallest even value of n such that the eccentricity of Hk is a rational number! If is length of the latus return of Hk , then I_1 is equal to _______

Official Ans . by NTA (٣٠٦)

Sol.
$$\operatorname{Hn}
abla \frac{x^2}{1+n} - \frac{y^2}{3+n} = 1$$

$$e = \sqrt{1 + \frac{b}{2}} = \sqrt{1 + \frac{3+n}{1+n}} = \sqrt{\frac{2n+4}{n+1}}$$

$$e = \sqrt{\frac{2n+4}{n+1}}$$

$$n = 48$$
 (smallest even value for whiel \hat{Q})

$$e^{\frac{10}{7}}$$

$$a^{2} = n + 1, b^{2} = n + 3$$

$$= 49 = 51$$

$$1 = \frac{2b^{2}}{a}$$

$$L = 2.51$$

$$1 = \frac{102}{7}$$

211=306

If a and b are the roots of equation xy - yx - y = 0, then the value of ayy + byy is equal to

Official Ans . by NTA (01)

Sol.
$$x \cdot 2 - 7x - 1 = 0 < \frac{a}{b}$$

By newton's theorem
$$S_{n+2} - 7S_{n+1} - Sn = 0$$

$$S_{21} - 7S_{20} \quad S1 = 0$$

$$S_{20} - 7S_{19} \quad 9 = 0$$

$$S_{19} - 7S_{18} - \$17 = 0$$

$$\frac{S_{21} + S_{17}}{S_{19}} = \frac{\$21 + \$19 - 7S_{18}}{\$19}$$

$$= \frac{S_{21} + S_{19} - 7(\$20 - 7\$19)}{\$19}$$

$$= \frac{50S_{19} + (\$21 - 7\$20)}{\$19}$$

$$= \frac{51S \times 8}{S_{19}} = 51$$

Let
$$A = \stackrel{\acute{e}0}{\stackrel{\circ}{e}} \stackrel{\checkmark}{\iota} \stackrel{\acute{\iota}}{\iota}$$
, where $a \cdot c\hat{l}R$. If $Ar = A$ $\stackrel{\acute{e}}{\stackrel{\circ}{e}} \stackrel{\circ}{\iota} \stackrel{\checkmark}{\iota}$ where $a \cdot c\hat{l}R$. If $Ar = A$ $\stackrel{\acute{e}}{\stackrel{\circ}{e}} \stackrel{\circ}{\iota} \stackrel{\checkmark}{\iota}$ and the positive value of a belongs to the interval $(n-1) \cdot n = 0$, where $n\hat{l}N$, then n is equal to

Official Ans. by NTA (Y)

Given
$$Ar = A$$

 $rac + r = r \dots (1)$ and $a + r + r = r$
 $a + r + r = r$

$$a + 1 - 9 = \frac{1}{2a}$$

$$7ay + 7a - 9 = \frac{1}{2a}$$

$$f(1) > \frac{1}{2a}$$

$$f(1,2)$$

n=2

PHYSICS

SECTION-A

The electric field in an electromagnetic wave is given as $E[r \cdot sin] = t - \frac{x}{c} NC^{-1}$

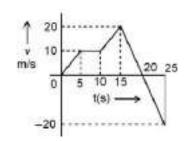
Official Ans . by NTA (٣)

Sol. Elv-sinIlt Ij M &

Average energy density of an em wav $\stackrel{\circ}{\underset{\bullet}{\stackrel{}}}$ E $\stackrel{\circ}{\underset{\bullet}{\stackrel{}}}$

Enegy stored = $\begin{bmatrix} 1 & 2 \end{bmatrix}$ volume $\begin{bmatrix} 1 & 2 \end{bmatrix}$ $\begin{bmatrix} 1 & 2 \end{bmatrix}$

From the v-t graph shown . the ratio of distance to displacement in $v \circ s$ of motion



$$(7) \frac{1}{7}$$

Official Ans . by NTA (r)

TEST PAPER WITH SOLUTION

Sol. Area under the graph from $t = \cdot to t = \tau \cdot sec = \tau \cdot \cdot m$ Area under the graph from $t = \tau \cdot to t = \tau \circ sec = \circ \cdot m$

> So distance covered = $(\Upsilon \cdot \cdot + \circ \cdot) m = \Upsilon \circ \cdot m$ Displacement = $(\Upsilon \cdot \cdot - \circ \cdot) m = \Upsilon \circ \cdot m$

The radii of two planets 'A' and 'B' are 'R' and ' ξ R' and their densities are \Box and \Box/τ respectively. The ratio of acceleration due to gravity at their surfaces (ξ A : ξ B) will be :

(1)1:17

(۲) ": 17

(٣)٣ : ٤

(٤)٤:٣

Official Ans. by NTA (٣)

Sol. $g = R_{x} = R_{$

$$\frac{g_{_{A}}}{g_{_{B}}} \, \square \frac{R \, \square \, \square}{{}_{\xi}R \, \square^{\frac{r}{2}}} \, \square^{\frac{r}{\xi}}$$

A coin placed on a rotating table just slips when it is placed at a distance of 1 cm from the center. If the angular velocity of the table in halved 1 it will just slip when placed at a distance of _____ from the centre:

- (1)Y CM
- (۲) \ cm
- (٣) \ cm
- (٤) £ CM

Official Ans. by NTA(٤)

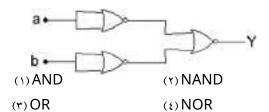
Sol. $fs ma \not = m \square \land R \square R \square \frac{\mu g}{\square 2}$

So if \square becomes $\underline{\mathbb{Y}}$, R will become $\mathfrak{t}R$.

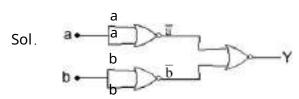
So distance from the center will be ¿ cm.

١

The logic performed by the circuit shown in figure. is equivalent to:



Official Ans . by NTA (1)



Y∏a∐b∏a∙b

The truth table for the given circuit will be

а	b	output
•	,	
1	•	•
-	1	

Hence it will be equivalent to AND gate.

- ra. A parallel plate capacitor of capacitance a Fis charged to a potential V. The energy stored in the
 - capacitor is Ev. The capacitor is now connected to another uncharged identical capacitor in parallel

combination. The emergy stored in the combination is Ex . The পি atio ৰি r / Ex is :

Official Ans. by NTA (Y)

(٣) 1 : ٤

Sol. <u>Initially</u>

$$Q = CV = (Y)V$$

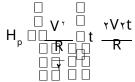
$$E_1 = 1/Y CV = 1/Y (Y)V = V^{Y}$$
Finally

Charge on each pacitor, Q $\square \, \frac{Q_{,}}{r} \, \square \, \frac{r V}{V} \, \square V$

$$\mathsf{E}_{\tau} \, \square \, 2 \, \frac{\mathsf{D}_{\tau} \, \mathsf{C} \, \mathsf{D}}{\mathsf{C} \, \mathsf{D}} \, \square \, \frac{\mathsf{V}_{\tau}}{\mathsf{V}} \qquad \square \, \frac{\mathsf{E}}{\mathsf{E}^{\tau}} \, \square \, \frac{\mathsf{V}_{\tau}}{\mathsf{V}}$$

Two identical heater filaments are connected first in parallel and then in series. At the same applied voltage, the ratio of heat produced in same time for parallel to series will be:

Sol. Parallel combination



Series combination

$$H_s \square \xrightarrow{\text{$\mid V_T \> \mid \ }} H_b \square \xrightarrow{\text{$\mid H_S \> \mid \ }} H_s \square \xrightarrow{\text{$\mid H_S$$

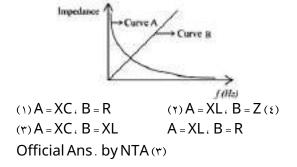
A transmitting antenna is kept on the surface of the earth. The minimum height of receiving antenna required to receive the signal in line of sight at £ km distance from it is x × 15 m. The value of x is (Let. radius of earth R = 1500 km)

 As per the given graph choose the correct representation for curve A and curve B.
 Where XC = reactance of pure capacitive circuit connected with A.C. source

XL = reactance of pure inductive circuit connected with A.C. source

R = impedance of pure resistive circuit connected with A.C. source

Z = Impedance of the LCR series circuit»



Sol.	$X_c = \frac{1}{C} = \frac{1}{2} = f = C$
	١
	$\Box X_c \Box \underline{f}$

Curve A

$$X_{L} \square \square L \square \square 2 \square f \square L$$

0x0_f

CurveB

\ kg of water at \...°C is converted into steam at ٤٠. · · · °C by boiling at atmospheric pressure . The volume of water changes from v. · · × v · m as a liquid to 1. 371 m as steam. The change in internal energy of the system during the process will be (Given latent heat of vaporisaiton = YYOV kJ/kg.

Atmospheric pressure = $1 \times 1 \cdot Pa$

$$(\xi) + Y \xi V \mathcal{I} k J$$

Official Ans. by NTA(1)

Sol. QQQQUQW

$$\square\square U \square \square Q \square \square W$$

 $\Box mL_{v}\Box P\Box V$

[1704] 1.4 [] 1.7 [] 1.4 [[7.9.K]

The critical angle for a denser-rarer interface is ٤١. ٤٥°. The speed of light in rarer medium is ٣٠٪ بر ms. The speed of light in the denser medium is:

Official Ans. by NTA (Y)

Sol. i Criticalangle

$$\frac{\Box}{C} \Box \frac{1}{\mu} \operatorname{Isini}_{c} \operatorname{Isini}_{c} \overline{\Box} \frac{1}{\sqrt{Y}}$$

A metallic surface is illuminated with radiation of wavelength \square , the stopping potential is Vo. If the same surface is illuminated with radiation of wavelength x 🛮 ، the stopping potential becomes

 $\frac{V_{\circ}}{L}$. The threshold wavelength for this metallic

surface will be -

Official Ans. by NTA(٤)

Sol. From the equation of photoelectric effect

$$eV \square \quad \frac{hc}{\square} \square \square \square \quad \frac{hc}{\square} \stackrel{hc}{\square} \square$$

$$_{*} \stackrel{\text{eV}}{\underset{\raisebox{1pt}{\stackrel{}{\scriptstyle 1}}}{}} 0 \stackrel{\text{hc}}{\underset{\raisebox{1pt}{\scriptstyle 2}}{}} \stackrel{\text{hc}}{\underset{\raisebox{1pt}{\scriptstyle 1}}{}} \stackrel{\text{hc}}{\underset{\raisebox{1pt}{\scriptstyle 1}}{}}$$

The free space inside a current carrying toroid is filled with a material of susceptibility $\forall x \forall \cdot \cdot$. The percentage increase in the value of magnetic field inside the toroid will be

Official Ans. by NTA(1)

$$\mu_r^{\text{\tiny Ω}} \text{\tiny V} \text{\tiny M} \text{\tiny$$

So percentageincrease in magnetic field

$$\square \frac{B \square B}{B} \cdot \square no \% \square \forall \%$$

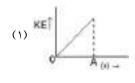
- galvanometer is increased by Yo'. This increase is achieved only by changing in the number of turns of coils and area of cross section of the wire while keeping the resistance of galvanometer coil constant. The percentage change in the voltage sensitivity will be:
 - (1)+70%
- (Y) 0·%
- (۳) Zero
- (ξ) Yο%

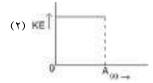
Official Ans. by NTA(1)

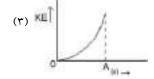
Sol.
$$I_s \square \frac{NBA}{CG} \& V_s \square \frac{NBA}{CG}$$

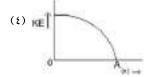
so percentage change in VS is also Yo/...

The variation of kinetic energy (KE) of a particle executing simple harmonic motion with the displacement (x) starting from mean position to extreme position (A) is given by









Official Ans . by NTA (\mathfrak{t})

Sol . For a particle executing SHM

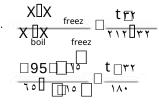
$$\mathsf{KE} \, \mathsf{D} \, \, \underset{\tau}{\overset{\vee}{\longrightarrow}} \, m \, \mathsf{D} \, \tau \, \mathsf{D} \, \mathsf{A} \, \tau \, \mathsf{D} \, \mathsf{X} \, \tau \, \mathsf{D}$$

When $x = \cdot$, KE is maximum & when x = A, KE is zero and KE V /S x graph is parabola.

- On a temperature scale 'X'. The boiling point of water is 70° X and the freezing point is -10° X. Assume that the X scale is linear. The equivalent temperature corresponding to -40° X on the Farenheit scale would be:
- (1) -14°F
- (Y) -117°F
- (٣) ξΛ°F
- (ξ)-\ξλ°F

Official Ans. by NTA(٤)

Sol.



$$\frac{\Box^{\Lambda \cdot}}{\Lambda \cdot} \Box \frac{\mathsf{t} \Box^{\Upsilon \Upsilon}}{\mathsf{1} \Lambda \cdot}$$

t[][\1.1.[]#Y

t□□\٤∧□f

Given below are two statements:

Statements I: Astronomical unit (Au). Parsec (Pc) and Light year (ly) are units for measuring astronomical distances.

 $Statements\ II:\ Au>Parsec\ (Pc)>ly$

In the light of the above statements . choose the most appropriate answer from the options given below :

- (1) Both Statements I and Statements II are correct.
- $\label{eq:correct} \textbf{(t) Statements I is correct but Statements II is} \\ incorrect.$
- (r) Both Statements I and Statements II are incorrect.
- $\mbox{($\mathfrak{z}$) Statements I is incorrect but statements II is } \\ \mbox{correct}.$

Official Ans. by NTA (Y)

Sol. 1AU[]1. 897[]1.11m

parsec[r...l] 1.17 m

\lightyear 4. £7 \lightyear

So،Au[ly[Persec

at the same temperature and pressure. The first vessel contains neon (monoatomic), the second contains chlorine (diatomic) and third contains uranium hexafloride (polyatomic).

Arrange these on the

basis of their root mean square speed (vrms)

choosents of rectations with post the options sol. give in state of the control o

(٤) V monotty ms dia livensily

Official Ans. by NTA (Y)

Sol. v_{rms} mono rate v_{rms} v_{rms} mono



vrms[ply[MRT]

So correct relation is

An average force of ۱۲۰ N is applied on a machine gun firing bullets each of mass 1. g at the speed of 10. m/s to keep it in position. The number of bullets fired per second by the machine gun is

(1) 0 (Y) 0.

(٤) ١٠٠

Official Ans. by NTA (Y)

Sol. F□nmv

where n = number of bullets fired per second

$$n \Box \frac{f}{mv} \Box \frac{150}{1 \cdot 15} \Box 300$$

have same number of atoms. The half life of A is same

eartheaveragedifardBBIfreapediatrydegayn

choose the correct relation from the given options.

Official Ans . by NTA (*)

Sol. T, DATE PUBL.

NY

L
DA DAY

SECTION-B

A monochromatic light is incident on a hydrogen sample in ground state. Hydrogen atoms absorb a fraction of light and subsequently emit radiation of six different wavelengths. The frequency of incident light is x x 1 Hz. The value of x is

incident light is $x \times 1$. Hz. The value of x = 1. (Given h = 1. We with h = 1.

Official Ans . by NTA (٣)

Sol. \(\tau \) \(\ta

The radius of curvature of each surface of a convex lens having refractive index v.A is v.Cm. The lens is now immersed in a liquid of refractive index v.A. The ratio of power of lens in air to its power in the liquid will be v.A. The value of v.A is v.A. Official Ans. by NTA(v.A)

Sol. P = 1.8 by lens maker's formula

Dividing $\frac{P}{P'} \cap \frac{\cdot \cdot \wedge}{1 \cdot \cdot \cdot \cap 1} \cap \xi$

The equation of wave is given by

Where x and Y are in m and t in s. The speed of the wave is ____ km h Official Ans. by NTA (1101)

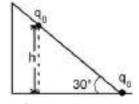
Sol.
$$V = \frac{1}{k} = \frac{1}{100} = \frac{1}{100}$$

٥٤.

direction where F is in newton and x is in meter. The work done by this force during a displacement Official Ans. by NTA (٣٢)

$\Pi \wedge \Pi \wedge X \Pi \wedge X$ Sol. W

As shown in the figure. a configuration of two 00. equal point charges $(q \cdot = + \tau \mu C)$ is placed on an inclined plane. Mass of each point charge is τ , q. Assume that there is no friction between charge and plane. For the system of two point charges to be in equilibrium (at rest) the height $h = x \times \sqrt[n]{\cdot} m$ The value of x is .



Official Ans. by NTA (***)

Sol. For equilibrium along the plane

$$\begin{array}{c|c} & 2 \\ \hline \end{array} 10 \\ \hline \end{array} 6 \\ \hline$$

$$\square \ h \ \square \ " \ " \ " \ " \ \square$$

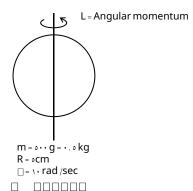
∏٠.٣m

□٣·· mm

A force F To Tax Tild acts on a particle in the x

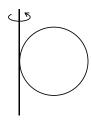
A solid sphere of mass ... g and radius .. cm is rotated about one of its diameter with angular speed of wrad 3. If the moment of inertia of the sphere about its tangent is x × 1. times its angular momentum about the diameter. Then the value of x will be ____

Official Ans. by NTA (٣٥)



Sol.

moment of inertia about tangent = IT



$$I_{_{t}} \mathop{\square} X \mathop{\square} {}^{\backslash} \cdot \mathop{\square} {}^{\backslash} L$$

$$\frac{\overset{\vee}{\circ}}{\circ} m\, R^{\overset{}{\circ}} \, \square\, \, x \, \overset{\square}{\circ} \, 1 \, \cdot \, \overset{\square}{\circ} \, R \, \Upsilon \quad \, _{\square}$$

$$\frac{v}{v}$$
 $\Box x \Box 10 \Box 2 \Box \frac{v}{v}$

The length of wire becomes I and I when W and I N tensions are applied respectively. If

 $1 \cdot 1_{Y} = 111$, the natural length of wire will $b = \frac{1}{2} 11$.

Here the value of x is _____.

Official Ans. by NTA (Y)

Sol. Let the original length be

When $T_1 = 1 \cdot \cdot \cdot N_i$ Extension = $[]_i$

When $T_{\tau} = v_{\tau} \cdot N_{\tau}$ Extension = $\ell_{\tau} \square \ell'$

Then \... [K] \... (\)

And \r. IKI = 0 ...(r)

o/, □5. □6, □6·

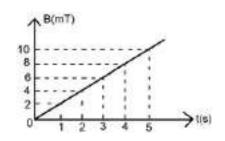
. □6 , □5 '

 ℓ . $\Box 6\ell$, $\Box \frac{11\ell}{r}$

 $\ell. \ \Box \frac{\ell}{r}$

0 x 0 r

The magnetic field B crossing normally a square metallic plate of area ϵ m is changing with time as shown in figure . The magnitude of induced emf in

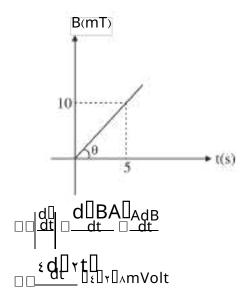


the plate during $t = \gamma s$ to $t = \xi s$, is _

Official Ans. by NTA (A)

Sol. m[tan][] \\ \frac{1}{\cdot} \]

B∏mt B∏rt



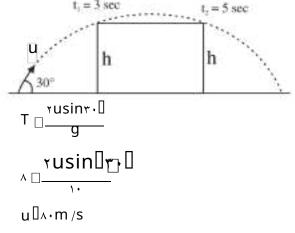
Approjectile bired same height at time +s and

projection of the projectile is _____ ms

 $(Given g = v \cdot m s)^{r}$

Official Ans. by NTA ($\wedge \cdot$)

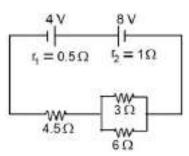
Sol. Time of flight t[]t[]+[] o [] \(\) sec



10. In the circuit diagram shown in figure given below.

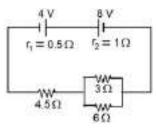
the current flowing through resistance $r_{\underline{\underline{\underline{u}}}}^{\underline{\underline{M}}}$ is.

The value of x is _____

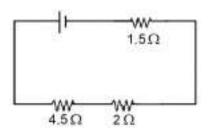


Official Ans. by NTA (1)

Sol.

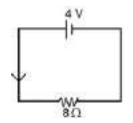


 $\mathsf{E}_{\mathsf{v}} \, \square \mathsf{E}_{\mathsf{v}} \, \square \, \mathsf{8} \, \square \, \mathsf{4} \, \square \, \mathsf{V}$

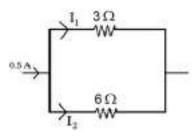


$$\frac{1}{r} \square \frac{1}{7} \square \frac{1}{r} \square \frac{1}{R}$$

 $R \square r \square$



I _ λ .. ο Α



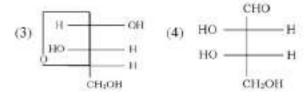
$$I_{,} \square_{X} \square \cdot . \circ \square_{X} \wedge A$$

$$I' \square \frac{k}{X} \square \frac{k}{I}$$

SECTION-A

61. L -isomer of tetrose X (C₄H₈O₄) gives positive Schiff's test and has two chiral carbons. On acetylation. 'X' yields triacetate. 'X' also undergoes following reactions

'X' is



Official Ans. by NTA (2)

Sol.

CHO
H * OH
HO * H

CH₂OH

(x)

COOH
H * OH
HO * H

COOH
(A)

L-tetrose with two chiral centre

- (x) gives positive schiff's test due -CHO group
- (x) is L-tetrose,

- 62. The polymer X consists of linear molecules and is closely packed. It is prepared in the presence of triethylaluminium and titanium tetrachloride under low pressure. The polymer X is –
 - (1) Polyacrylonitrile
 - (2) Low density polythene
 - (3) Polytetrafluoroethane
 - (4) High density polythene

Official Ans. by NTA (4)

Sol. Ethene undergoes addition polymerisation to high density polythene in the presence of catalyst such as AlEt₃ and TiCl₄ (Ziegler – Natta catalyst) at a temperature of 333 K to 343 K and under a pressure of 6-7 atmosphere.

- 63. When a solution of mixture having two inorganic salts was treated with freshly prepared ferrous sulphate in acidic medium, a dark brown ring was formed whereas on treatment with neutral FeCl₅, it gave deep red colour which disappeared on boiling and a brown red ppt was formed. The mixture contains
 - (1) CH₃COO & NO;
 - (2) C2O4 & NO3
 - (3) SO₃² & CH₃COO
 - (4) SO₃²⁻ & C₂O₄²⁻

Official Ans. by NTA (1)

Sol.
$$CH_3COO^- + FeCl_3 \rightarrow Fe(CH_3COO)_3$$
 or
$$\begin{bmatrix} Fe_3(OH)_2(CH_3COO)_6 \end{bmatrix}^*$$
Blood red colour
$$\downarrow \Delta$$

$$Fe(OH)_2(CH_3COO) \downarrow$$
Red-brown precipitate
$$2NO_3^- + 4H_2SO_4^- + 6Fe^{2\alpha} \rightarrow 6Fe^{3\alpha} + 2NO \uparrow + 4SO_4^{2\alpha} + 4H_2O$$

$$\begin{bmatrix} Fe(H_2O)_4 \end{bmatrix}^{2\alpha} + NO \rightarrow \begin{bmatrix} Fe(H_2O)_5(NO) \end{bmatrix}^{2\alpha} + H_2O$$

64. Given below are two statements : one is labelled as Assertion A and the other is labelled as Reason R :

Assertion A: In the photoelectric effect, the electrons are ejected from the metal surface as soon as the beam of light of frequency greater than threshold frequency strikes the surface.

Reason R: When the photon of any energy strikes an electron in the atom, transfer of energy from the photon to the electron takes place.

In the light of the above statements, choose the most appropriate answer from the options given below:

- Both A and R are correct but R is NOT the correct explanation of A
- (2) A is correct but R is not correct
- (3) Both A and R are correct and R is the correct explanation of A
- (4) A is not correct but R is correct

Official Ans. by NTA (2)

Sol. There is a characteristic minimum frequency, or "threshold frequency," for each metal below which the photoelectric effect is not seen. The ejected electrons leave with a specific amount of kinetic energy at a frequency $v > v_0$ with an increase in light frequency of these electron kinetic energies also rise.

- 65. 25 mL of silver nitrate solution (1 M) is added dropwise to 25 mL of potassium iodide (1.05 M) solution. The ion(s) present in very small quantity in the solution is/are
 - (1) NO₃ only
 - (2) K* only
 - (3) Ag* and Γ both
 - (4) I only

Official Ans. by NTA (3)

Sol. $AgNO_3 + KI \rightarrow AgI \downarrow + KNO_3$

$$AgI \rightarrow Ag^{+} + I^{-}_{5-0.625}$$

AgI is a insoluble salt so concentration Ag^* and Γ will be negligible. 66. 'A' and 'B' in the below reactions are :

(R = alkyl)

$$B = R$$
 CO_2H
 CH_3

$$B = R$$
 CH_3

(4)
$$R$$
 $CO_2H = A$,
 $B = R$ CO_2H

Official Ans. by NTA (4)

Sol.

- 67. The set which does not have ambidentate ligand(s) is
 - (1) C2O4, ethylene diammine, H2O
 - (2) EDTA4-, NCS-, C2O4-
 - (3) NO2, C2O4, EDTA4-
 - (4) C2O4-, NO2, NCS

Official Ans. by NTA (1)

Sol. NO, NCS are ambidentate ligand

$$C_2O_4^ O_4^-$$
 Ethylene diammine $H_2N - CH_2 - CH_2 - NH_3$

EDTA Ethylene diamine tetra acetate

Where Nu = Nucleophile

Find out the correct statement from the options given below for the above 2 reactions.

- Reaction (I) is of 2nd order and reaction (II) is of 1st order
- (2) Reaction (I) and (II) both are of 2nd order
- (3) Reaction (I) is of 1st order and reaction (II) is of 2nd order
- (4) Reactions (I) and (II) both are of 1st order Official Ans. by NTA (3)

Sol.

$$\bigcirc_{\text{OMe}}^{\text{Cl}} \rightarrow \bigcirc_{\text{O-Me}}^{\text{+}} \bigcirc_{\text{OMe}}^{\text{Nu}} \longrightarrow_{\text{OMe}}^{\text{Nu}}$$

Electron Donating group S_N¹ Mech. : Iⁿ order

Electron withdrawing group

S_N² Mech: 2nd order

- For elements B, C, N, Li, Be, O and F the correct order of first ionization enthalpy is
 - (1) Li < Be < B < C < N < O < F
 - (2) B > Li > Be > C > N > O > F
 - (3) Li < B < Be < C < O < N < F
 - (4) Li < Be < B < C < O < N < F</p>

Official Ans. by NTA (3)

Sol. First I.E.

F > N > O > C > Be > B > Li

Li-520kJ/mol

Be-899kJ/mol

B-801 kJ/mol

C-1086 kJ/mol

N-1402 kJ/mol

O-1314 kJ/mol

F-1681 kJ/mol

70. Match List-I with List-II:

List-I Species	List-II Geometry/Shape
A. H ₃ O*	I. Tetrahedral
B. Acetylide anion	II. Linear
C. NH ₄	III. Pyramidal
D. ClO ₂	IV. Bent

Choose the correct answer from the options given below:

- (1) A-III, B-II, C-I, D-IV
- (2) A-III, B-I, C-II, D-IV
- (3) A-III, B-IV, C-I, D-II
- (4) A-III, B-IV, C-II, D-I

Official Ans. by NTA (1)

Sol. Molecule/Ion Hybridisation Shape

$$H_3O$$
 sp³ Pyramidal $\overline{C} = \overline{C}$

Acelylide sp linear $\overline{C} = \overline{C}$
 NH_4^+ sp³ tetrahedral H
 $O = \overline{C}$
 $O = \overline{C}$

- For compound having the formula GaAlCl₄, the correct option from the following is
 - Ga is more electronegative than Al and is present as a cationic part of the salt GaAlCl₄
 - Oxidation state of Ga in the salt GaAlCl₄ is +3.
 - (3) Cl forms bond with both Al and Ga in GaAlCl₄
 - (4) Ga is coordinated with Cl in GaAlCl_d

Official Ans. by NTA (1)

Sol. Gallous tetrachloro aluminate Ga*AlCl;

$$2Ga + Ga^+GaCl_4^- + 2Al_2Cl_6 \xrightarrow{190^9} 4Ga^+AlCl_4^-$$

$$Ga^{+} \begin{bmatrix} CI \\ I \\ CI \\ CI \end{bmatrix} CI$$

Structure of Ga A ICI,

Ga is cationic part of salt GaAlCl,

- 72. In the extraction process of copper, the product obtained after carrying out the reactions
 - (i) $2Cu_2S + 3O_2 \rightarrow 2Cu_2O + 2SO_2$
 - (ii) 2Cu,O+Cu,S→6Cu+SO, is called
 - (1) Blister copper
 - (2) Copper scrap
 - (3) Reduced copper
 - (4) Copper matte

Official Ans. by NTA (1)

Sol.
$$2Cu_2S + 3O_2 \rightarrow 2Cu_2O + 3SO_2$$

$$2Cu_2O + Cu_2S \rightarrow 6Cu + SO_2$$

Blister copper

Due to evolution of SO₂, the solidified copper formed has a blistered look and is referred to as blister copper. 73. Match List-I with List-II:

List-I	List-II	
A. K	I. Thermonuclear reactions	
B. KCI	II. Fertilizer	
С. КОН	III. Sodium potassium pump	
D. Li	IV. Absorbent of CO ₂	

Choose the correct answer from the options given below:

- (1) A-III, B-II, C-IV, D-I
- (2) A-IV, B-I, C-III, D-II
- (3) A-IV, B-III, C-I, D-II
- (4) A-III, B-IV, C-II, D-I

Official Ans. by NTA (1)

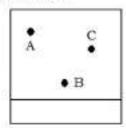
Sol. K+ - Sodium - Potassium Pump

KCl - Fertiliser

KOH - absorber of CO,

Li - used in thermonuclear reactions

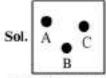
74. Thin layer chromatography of a mixture shows the following observation:



The correct order of elution in the silica gel column chromatography is

- (1) A, C, B
- (2) B, C, A
- (3) C, A, B
- (4) B, A, C

Official Ans. by NTA (1)



According to the observation, A is more mobile and interacts with the mobile phase more than C, and C is more drawn to the mobile phase than B.

Hence, the correct order of elution in the silico gel column chromatography is -B < C < A

- 75. Which of the following complex has a possibility to exist as meridional isomer?
 - (1) [Co(NH₃)₃(NO₂)₃]
 - (2) [Co (en)₃]
 - (3) [Co (en)2 Cl2]
 - (4) [Pt (NH₃)₂ Cl₂]

Official Ans. by NTA (1)

Sol. [MA₃B₃] type of compound exists as facial and meridonial isomer.





76. Given below are two statements:

Statement-1: Methane and steam passed over a heated Ni catalyst produces hydrogen gas.

Statement-II: Sodium nitrite reacts with NH₄Cl to give H₂O, N₂ and NaCl.

In the light of the above statements, choose the most appropriate answer from the options given below:

- (1) Both the statements I and II are correct
- (2) Both the statements I and II are incorrect
- (3) Statement I is incorrect but Statement II is
- (4) Statement I is correct but Statement II is incorrect

Official Ans. by NTA (1)

Sol.
$$CH_4(g) + \underset{Steem}{H_2O(g)} \xrightarrow{10} CO(g) + 3H_2(g)$$

 $NaNO_{\ell}(aq) + NH_{\ell}Cl(aq) \rightarrow N_{\ell}(g) + NaCl(aq) + 2H_{\ell}O(\ell)$

77. Given below are two statements:

Statement I: If BOD is 4 ppm and dissolved oxygen is 8 ppm, then it is a good quality water.

Statement II: If the concentration of zinc and nitrate salts are 5 ppm each, then it can be a good quality water.

In the light of the above statements, choose the most appropriate answer from the options given below:

- (1) Both the statements I and II are incorrect
- (2) Statement I is incorrect but Statement II is correct
- (3) Both the statements I and II are correct
- (4) Statement I is correct but Statement II is incorrect

Official Ans. by NTA (3)

Sol. Clean water would have BOD value of less than 5 ppm.

Maximum limit of Zn in clean water

 $= 5.0 \text{ ppm or mg dm}^{-3}$

Maximum limit of NO; in clean water

- = 50 ppm or mg dm⁻³
- Arrange the following compounds in increasing order of rate of aromatic electrophilic substitution reaction

(d)

- (c) (1) d, b, c, a
- (2) b, c, a, d
- (3) c, a, b, d
- (4) d, b, a, c

Official Ans. by NTA (3)

Sol. Benzene becomes more reactive towards EAS when any substituent raises the electron density.

Correct order

c < a < b < d

- 79. The complex that dissolves in water is
 - (1) Fe₄[Fe(CN)₆]₈
 - (2) [Fe₃(OH)₂(OAc)₆]Cl
 - (3) K₂[Co(NO₂)₆]
 - (4) (NH₄)₃[As(Mo₅O₁₀)₄]

Official Ans. by NTA (2)

Allen Ans. (2)

Sol. Fe₄ [Fe(CN)₆]₄ Prussian Blue–water insoluble K_3 [Co(NO₂)₆] very poorly water soluble (NH₄)₃ [As (MO₃O₁₀)₄] water insoluble ammonium arseno molybdate

[Fe₃(OH)₂(OAc)₆]Cl is water soluble.

80. o-Phenylenediamine HNO₂ 'X'

Major Product

'X' is

$$(3) \bigcirc \bigvee_{N_2}^{+} N \equiv N$$

Official Ans. by NTA (1)

Sol. Orthophenyl amine.

SECTION-B

81. A mixture of 1 mole of H₂O and 1 mole of CO is taken in a 10 litre container and heated to 725 K. At equilibrium 40% of water by mass reacts with carbon monoxide according to the equation:

$$CO(g) + H_2O(g) \rightleftharpoons CO_2(g) + H_2(g)$$
.

The equilibrium constant $K_C \times 10^2$ for the reaction is _____, (Nearest integer)

Official Ans. by NTA (44)

Sol. $CO_{(g)} + H_2O_{(g)} \rightleftharpoons CO_{2(g)} + H_{2(g)}$

t = 0 1 mol 1 mol 0 0

at equ. 1-x 1-x x x

at equilibrium 40% by mass water reacts with CO

x = 0.4 1 - x = 0.6

 $K_C = \frac{[CO_2][H_2]}{[CO][H_2O]} = \frac{0.4 \times 0.4}{0.6 \times 0.6} = 0.44$

 $K_{\scriptscriptstyle\rm C}\times 10^2=44$

82. The ratio of spin-only magnetic moment values μ_{eff} [Cr(CN)₆]⁵⁻ / μ_{eff} [Cr(H₂O)₆]⁵⁺ is ______.

Official Ans. by NTA (1)

Sol. Spin magnetic moment of $\left[\text{Cr(CN)}_6 \right]^{3} \cdot \left(t_{2g}^3 e_g^6 \right)$

$$\mu_t = \sqrt{3(3+2)} = \sqrt{15} \text{ BM}$$

Spin magnetic moment of $[Cr(H_2O)_6]^{3+}(t_{2g}^3e_g^0)$

$$\mu_2 = \sqrt{3(3+2)} = \sqrt{15}$$
 BM

$$\frac{\mu_1}{\mu_2} = \frac{\sqrt{15}}{\sqrt{15}} = 1$$

83. An atomic substance A of molar mass 12 g mol⁻¹ has a cubic crystal structure with edge length of 300 pm. The no. of atoms present in one unit cell of A is _______. (Nearest integer)

Given the density of A is 3.0 g mL $^{-1}$ and $N_A = 6.02$ $\times~10^{23}~\text{mol}^{-1}$

Official Ans. by NTA (4)

Sol. d = 3 g/cc

M = 12 g/mol

 $a = 300 \text{ pm} = 3 \times 10^{-8} \text{ cm}$

$$Z = \frac{d \times N_{x} \times a^{3}}{M} = \frac{3 \times 6.02 \times 10^{23} \times (3 \times 10^{-8})^{3}}{12}$$

 $= 4.06 \approx 4$

84.

The ratio x/y on completion of the above reaction

is____.

Official Ans. by NTA (2)

Sol.

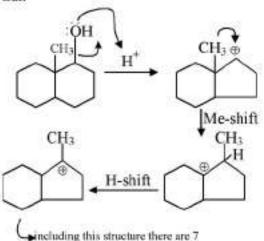
∴ x = 2 mole

$$\frac{x}{y} = \frac{2}{1} = 2$$

The number of hyperconjugation structures involved to stabilize carbocation formed in the above reaction is ______.

Official Ans. by NTA (7)

Sol.



86. Solid fuel used in rocket is a mixture of Fe₂O₃ and Al (in ratio 1 : 2). The heat evolved (kJ) per gram

of the mixture is _____ (Neatest integer)

Given: $\Delta H_t^0 (Al_2O_3) = -1700 \text{ kJ mol}^{-1}$

Hyperconjugation structure

$$\Delta H_f^9 (Fe_2O_3) = -840 \text{ kJ mol}^{-1}$$

Molar mass of Fe. Al and O are 56, 27 and 16 g mol⁻¹ respectively.

Official Ans. by NTA (4)

Sol. $\frac{\text{Fe}_2\text{O}_3 + 2\text{Al} \rightarrow \text{Al}_2\text{O}_3 + 2\text{Fe}}{\text{Molar mass } 160\text{g} \ 27\text{g}}$

$$\left(\Delta H_{t}^{0}\right)_{\text{seartion}} = \left[\left(\Delta H_{t}^{0}\right)_{Al_{2}O_{3}} + 2\left(\Delta H_{t}^{0}\right)_{Fe}\right] - \left[\left(\Delta H_{t}^{0}\right)_{Fe,O_{s}} + 2\left(\Delta H_{t}^{0}\right)_{Al}\right]$$

= [-1700 + 0] - [-840 + 0]

= - 860 kJ/mol

Total mass of mixture = $Fe_2O_3 + Al(1:2 \text{ molar ratio})$

 $= 160 + 2 \times 27$

= 214 g/mol

Heat evolved per gram = $\frac{860}{214}$ = 4 kJ/g

7

 A solution of sugar is obtained by mixing 200 g of its 25% solution and 500 g of its 40% solution (both by mass). The mass percentage of the resulting sugar solution is ______. (Nearest integer)

Official Ans. by NTA (36)

Sol. Total mass of sugar in mixture of 25% of 200

and 40% of 500 g

Sugar solution = $0.25 \times 200 + 0.40 \times 500$

$$=50 + 200 = 250 g$$

Total mass of solution = 200 + 500 = 700 g

Mass of sugar in solution =
$$\frac{250}{700} \times 100 = 35.7\%$$

≈36%

The above reaction was studied at 300 K by monitoring the concentration of FeSO₄ in which initial concentration was 10 M and after half an hour became 8.8 M. The rate of production of Fe₂(SO₄)₃ is _____ × 10⁻⁶ mol L⁻¹ s⁻¹.

(Nearest integer)

Official Ans. by NTA (333)

Sol. $KClO_3 + 6FeSO_4 + 3H_2SO_4 \rightarrow KCl + 3Fe_2(SO_4)_3 + 3H_2O$

$$ROR = -\frac{\Delta[KCIO_3]}{\Delta t} = \frac{-1}{6} \frac{\Delta[FeSO_4]}{\Delta t}$$
$$= \frac{+1}{3} \frac{\Delta[Fe_2(SO_4)_3]}{\Delta t}$$

$$\frac{\Delta[\text{Fe}_2(\text{SO}_4)_3]}{\Delta t} = \frac{1}{2} \frac{-\Delta[\text{FeSO}_4]}{\Delta t}$$

$$= \frac{1}{2} \frac{(10 - 8.8)}{30 \times 60}$$

$$= 0.333 \times 10^{-3}$$

$$= 333 \times 10^{-6} \text{ mol litre}^{-1} \text{ sec}^{-1}$$

89. 0.004 M K₂SO₄ solution is isotonic with 0.01 M glucose solution. Percentage dissociation of K₂SO₄ is ______(Nearest integer)

Official Ans. by NTA (75)

Sol. Isotonic solutions,

$$\pi_{K_{*}SO_{*}} = \pi_{Ghucose}$$

$$i \times 0.004 \times RT = 0.01 \times RT$$

$$i = 2.5$$

For K_2SO_4 {for dissociation $i = 1 + (n - 1)\alpha$ }

DOD(
$$\alpha$$
) = $\frac{i-1}{n-1} = \frac{2.5-1}{3-1} = 0.75$

% dissociation = 75

Official Ans. by NTA (2)

Sol.
$$Pb^{2+} + 2e^- \rightarrow Pb$$
 $\Delta G_i^0 = -2FE_i^0$

$$Pb^{4+} + 4e^- \rightarrow Pb \qquad \qquad \Delta G_2^0 = -4FE_2^0$$

$$Pb^{2+} \rightarrow Pb^{4+} + 2e^{-}$$
 $\Delta G_3^0 = -2FE_3^0$

$$\Delta G_3^0 = \Delta G_1^0 - \Delta G_2^0$$

$$-2FE_3^0 = 2F(2n-m)$$

$$E_0^0 = m - 2n = m - xn$$

Hence x = 2