

FINAL JEE–MAIN EXAMINATION – APRIL, 2023

(Held On Thursday 06 April, 2023)

TIME : 9 : 00 AM to 12 : 00 NOON

MATHEMATICS

SECTION-A

1. Let $5f(x) + 4f\left(\frac{1}{x}\right) = \frac{1}{x} + 3, x > 0$. Then $\int_1^2 f(x) dx$

is equal to:

(1) $\log_e 2 - 1$

(2) $\log_e 2 + 1$

(3) $\log_e 2 + 2$

(4) $\log_e 2 - 2$

Official Ans. by NTA (1)

Sol. $5f(x) + 4f\left(\frac{1}{x}\right) = \frac{1}{x} + 3 \dots \dots (1)$

replace $x \rightarrow \frac{1}{x}$

$5f\left(\frac{1}{x}\right) + 4f(x) = x + 3 \dots \dots (2)$

Eq. (1) $\times 5$ - eq. (2) $\times 4$

$f(x) = \frac{1}{9} \left(\frac{5}{x} - 4x + 3 \right)$

$I = \int_1^2 \frac{1}{9} (5 - 4x^2 + 3x) dx = \frac{1}{9} \log_e 2 - 1$

2. A pair of dice is thrown n times. For each throw, a total of 6 is considered a success. If the probability of at least 4 successes is $\frac{k}{311}$, then k is equal to

(1) 82

(2) 123

(3) 164

(4) 70

Official Ans. by NTA (2)

Sol. Probability of success $\frac{1}{9} = p$

Probability of failure $q = \frac{8}{9}$

$P(\text{at least 4 success}) = P(4 \text{ success}) + P(5 \text{ success})$

$= {}^6C_4 p^4 q + {}^6C_5 p^5 q = \frac{41}{310} = \frac{123}{311}$

$k = 123$

TEST PAPER WITH SOLUTION

3. If ${}^{2n}C_3 : {}^nC_3 = 10 : 1$, then the ratio

${}^{n+3}C_2 : (n+3)!$ is

(1) 30 : 16

(2) 10 : 37

(3) 27 : 11

(4) 2 : 1

Official Ans. by NTA (4)

Sol. $\frac{{}^{2n}C_3}{{}^nC_3} = 10 \Rightarrow \frac{2n(2n-1)(2n-2)}{n(n-1)(n-2)} = 10$

$n = 8$

So ${}^{n+3}C_2 : (n+3)! = 2$

4. If the ratio of the fifth term from the beginning to the fifth term from the end in the expansion of

$(\sqrt{x} + \frac{1}{\sqrt{x}})^n$ is $\sqrt{6} : 1$, then the third term from the beginning is:

(1) $6\sqrt{2}$

(2) $6\sqrt{3}$

(3) $3\sqrt{2}$

(4) $3\sqrt{3}$

Official Ans. by NTA (2)

Sol. $\frac{{}^nC_{24} \cdot (\sqrt{x})^{n-24} \cdot (\frac{1}{\sqrt{x}})^{24}}{{}^nC_{23} \cdot (\sqrt{x})^{n-23} \cdot (\frac{1}{\sqrt{x}})^{23}} = \frac{\sqrt{6}}{1}$

$n = 10$

So $T_3 = {}^{10}C_2 \cdot (\sqrt{x})^{10-2} \cdot (\frac{1}{\sqrt{x}})^2 = \frac{45 \cdot 4}{\sqrt{3}} = 60\sqrt{3}$

5. Let $\vec{a} = 2\hat{i} + 3\hat{j} + 4\hat{k}$, $\vec{b} = 2\hat{i} - 2\hat{j} - 2\hat{k}$ and $\vec{c} = -\hat{i} + \hat{j} + \hat{k}$. If \vec{d} is a vector perpendicular to both \vec{b} and \vec{c} and $|\vec{d}| = 1$. Then $|\vec{a} \cdot \vec{d}|$ is equal to

(1) $\frac{1}{\sqrt{2}}$

(2) $\frac{1}{\sqrt{3}}$

(3) $\frac{1}{\sqrt{6}}$

(4) $\frac{1}{\sqrt{10}}$

Official Ans. by NTA (4)

Sol. $a = \begin{bmatrix} 1 & -2 & -2 \\ -1 & 4 & 3 \end{bmatrix}$

$$b \cdot c = \begin{bmatrix} 1 & -2 & -2 \\ -1 & 4 & 3 \end{bmatrix} = 2i + 2k$$

$$d = 2i + 2k$$

$$a \cdot d = 18$$

$$So \ d = 2(2i + 2k)$$

$$d \cdot a = \begin{bmatrix} 4 & -2 & 4 \\ 23 & 4 & 4 \end{bmatrix} = -20i + 8j + 16k$$

$$d \cdot a^2 = 720$$

6. The straight lines L_1 and L_2 pass through the origin and trisect the line segment of the line $L: 4x + 5y = 10$ between the axes. If m_1 and m_2 are the slopes of the lines L_1 and L_2 , then the point of intersection of the line $y = (m_1 + m_2)x$ with L lies on

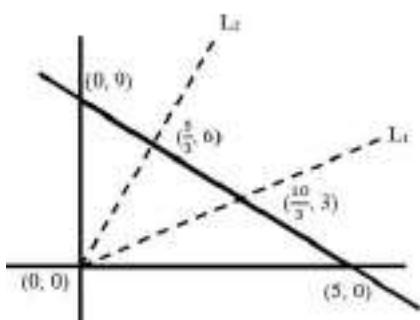
$$(1) 4x + y = 10$$

$$(2) 4x - y = 10$$

$$(3) y - x = 0$$

$$(4) y - 2x = 0$$

Official Ans. by NTA (3)



Sol.

$$m_{L_1} = \frac{3.3}{10} = \frac{9}{10}$$

$$m_{L_2} = \frac{6.3}{5} = \frac{18}{5}$$

$$y = (m_1 + m_2)x$$

$$y = \frac{9}{2}x$$

Point of intersection with L is $(\frac{10}{7}, \frac{45}{7})$

7.

From the top A of a vertical wall AB of height 30 m, the angles of depression of the top P and bottom Q of a vertical tower PQ are 15° and 60° respectively. B and Q are on the same horizontal level. If C is a point on AB such that $CB = PQ$, then the area (in m^2) of the quadrilateral BCPQ is equal to

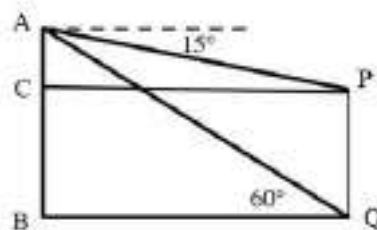
$$(1) 600(3-1)$$

$$(2) 300$$

$$(3) 200(3-1)$$

$$(4) 300(3-1)$$

Official Ans. by NTA (1)



Sol.

$$\tan 60^\circ = \sqrt{3} = \frac{30}{BQ}$$

$$BQ = 103m = CP$$

$$\tan 15^\circ = 2 - \sqrt{3} = \frac{AC}{CP}$$

$$AC = 103(2 - \sqrt{3})$$

$$\text{Area} = 103(60 - 203) = 600(3 - 1)$$

8.

The sum of the first 20 terms of the series $0 + 11 + 19 + 29 + 41 + \dots$ is

$$(1) 3450$$

$$(2) 3250$$

$$(3) 3420$$

$$(4) 3520$$

Official Ans. by NTA (4)

Sol. $S_n = 0 + 11 + 19 + 29 + \dots$

$$\text{Let } T_r = ar^{r-1} + br + c$$

$$T_1 = a + b + c = 0$$

$$T_2 = 2a + 2b + c = 11$$

$$T_3 = 3a + 3b + c = 19$$

$$a = 1, b = 3, c = 1$$

$$\text{Hence } S_{20} = \sum_{r=1}^{20} (r^2 + 3r + 1) = 3520$$

9. The mean and variance of a set of 10 numbers are 12 and 15 respectively. The mean and variance of another set of 10 numbers are 14 and 32 respectively. If the variance of all the 20 numbers in the two sets is 13, then s^2 is equal to

- (1) 9
(2) 12
(3) 11
(4) 10

Official Ans. by NTA (4)

Sol. Combine var. = $\frac{n_1 s_1^2 + n_2 s_2^2}{n_1 + n_2} + \frac{n_1 m_1^2 + n_2 m_2^2}{(n_1 + n_2)^2}$

$$13 = \frac{15 \cdot 14 + 15 s^2}{30} + \frac{15 \cdot 15 (12 - 14)^2}{30 \cdot 30}$$

$$13 = \frac{14 + s^2}{2} + 4$$

$$s^2 = 10$$

10. Let $A = [a_{ij}]$ where $a_{ij} = 1$ for all i, j and $A^T = I$. Let a be the sum of all diagonal elements of A and $b = |A|$, then $ra + \xi b$ is equal to (1) 1 (2) 11 (3) 3 (4) 1

Official Ans. by NTA (4)

Sol. Let $A = \begin{bmatrix} p & q \\ r & s \end{bmatrix}$

$$A^2 = \begin{bmatrix} p^2 + qr & pq + qs \\ pr + rs & qs + s^2 \end{bmatrix}$$

$$p^2 + qr = 1 \quad (1) \quad pq + qs = 0 \Rightarrow p + s = 0 \quad (2)$$

$$pr + rs = 1 \quad (2) \quad pr + rs = 0 \Rightarrow r(p + s) = 0 \quad (3)$$

Equation (1) - equation (2)

$$p^2 = s^2 \Rightarrow p + s = 0$$

Now $ra + \xi b$

$$= 3(p + s) + 4(pq + rs)$$

$$= 3 \cdot 0 + 4(-p^2) = -4p^2 = -4$$

Let $I(x) = \int_0^x \frac{x^2 \sec^2 x + \tan x}{(x \tan x + 1)^2} dx$. If $I(\frac{\pi}{4}) = \frac{1}{4}$, the I

is equal to

(1) $\log_e \frac{(x+4)}{16} - \frac{p^2}{4(p+4)}$

(2) $\log_e \frac{(x+4)}{16} + \frac{p^2}{4(p+4)}$

(3) $\log_e \frac{(x+4)}{32} - \frac{p^2}{4(p+4)}$

(4) $\log_e \frac{(x+4)}{32} + \frac{p^2}{4(p+4)}$

Official Ans. by NTA (2)

Sol. $I(x) = \int_0^x \frac{x^2 (\sec^2 x + \tan x)}{(x \tan x + 1)^2} dx$

Let $x \tan x + 1 = t$

$$I = \int_0^x \frac{x^2 \sec^2 x + 1}{(x \tan x + 1)^2} dx$$

$$I = \int_0^x \frac{x^2 \sec^2 x + 1}{(x \tan x + 1)^2} dx = \int_0^x \frac{x^2 \cos^2 x + 1}{x^2 \sin^2 x + \cos^2 x} dx$$

$$I = \int_0^x \frac{x^2 \sec^2 x + 1}{x \tan x} dx = \int_0^x \frac{x^2 \sec^2 x}{x \tan x} dx + \int_0^x \frac{1}{x \tan x} dx$$

$$As I(\frac{\pi}{4}) = \frac{1}{4} \quad C = \frac{1}{4}$$

$$I(\frac{\pi}{4}) = \ln \frac{(p+4)}{32} - \frac{p^2}{4(p+4)}$$

11. If the equation of the plane passing through the line of intersection of the planes $x - y + z = 1$, $2x - 3y + 4z = 5$

and parallel to the line $ax + by + cz + d = 0$, then $a + b + c$ is equal to

$$\frac{x+1}{-2} = \frac{y+3}{4} = \frac{z-2}{5}$$

$a + b + c$ is equal to

- (1) 11
(2) 12
(3) 13
(4) 10

Official Ans. by NTA (1)

Sol. Equation of family of plane

$$2x - y + z - 3 + l(4x - 3y + 5z + 9) = 0$$

$$x(2+4l) - y(1+3l) + z(1+5l) - 3+9l = 0$$

Parallel to the line

$$-2(2+4l) - (1+3l)4 + (1+5l)5 = 0$$

$$5l = 3$$

$$l = \frac{3}{5}$$

equation of plane

$$11x - 7y + 10z + 6 = 0$$

$$a + b + c = 18$$

13. Statement $(P \supset Q) \cup (R \supset Q)$ is logically equivalent to

$$(1) P \cup R \supset Q$$

$$(2) P \supset R \cup Q \supset R$$

$$(3) P \supset R \cup Q \supset R$$

$$(4) P \cup R \supset Q$$

Official Ans. by NTA (1)

Sol. $P \supset Q \cup (R \supset Q)$

We know that $P \supset Q \equiv \sim P \cup Q$

$$\sim P \cup Q \cup \sim R \cup Q$$

$$\Rightarrow \sim P \cup \sim R \cup Q$$

$$\Rightarrow \sim(P \cup R) \cup Q$$

$$\Rightarrow P \cup R \supset Q$$

14. The sum of all the roots of the equation

$$x^2 - 8x + 15 - 2x + 7 = 0 \text{ is:}$$

$$(1) 9 + 3\sqrt{3}$$

$$(2) 11 + 3\sqrt{3}$$

$$(3) 9 - 3\sqrt{3}$$

$$(4) 11 - 3\sqrt{3}$$

Official Ans. by NTA (1)

Sol. For $x \leq 3$ or $x \geq 5$

$$x^2 - 8x + 15 - 2x + 7 = 0$$

$$x = 5 + 3\sqrt{3}$$

$$\text{For } x > 3 \text{ and } x < 5, x^2 - 8x + 15 + 2x - 7 = 0$$

$$x = 2$$

$$\text{Hence sum} = 9 + 3\sqrt{3}$$

15. Let $a_1, a_2, a_3, \dots, a_n$ be n positive consecutive terms of an arithmetic progression. If $d < 0$ is its common difference, then

$$\lim_{n \rightarrow \infty} \sqrt[n]{\frac{d}{e} \left(\frac{1}{\sqrt{a_1 + \sqrt{a_2}}} + \frac{1}{\sqrt{a_2 + \sqrt{a_3}}} + \dots + \frac{1}{\sqrt{a_{n-1} + \sqrt{a_n}}} \right)}$$

$$(1) 1$$

$$(2) \sqrt{d}$$

$$(3) \frac{1}{\sqrt{d}}$$

$$(4) 0$$

Official Ans. by NTA (1)

$$\text{Sol. } \lim_{n \rightarrow \infty} \sqrt[n]{\frac{d}{e} \left(\frac{1}{\sqrt{a_1 + \sqrt{a_2}}} + \frac{1}{\sqrt{a_2 + \sqrt{a_3}}} + \dots + \frac{1}{\sqrt{a_{n-1} + \sqrt{a_n}}} \right)}$$

On rationalising each term

$$\lim_{n \rightarrow \infty} \sqrt[n]{\frac{d}{e} \left(\frac{\sqrt{a_n} - \sqrt{a_1}}{d} \right)}$$

$$\lim_{n \rightarrow \infty} \sqrt[n]{\frac{d}{e} \left(\frac{(n-1)d}{(a_n + \sqrt{a_1})d} \right)}$$

16. If the system of equations $x + y + az = b$, $rx + sy + tz = c$, $ux + vy + wz = d$ has infinitely many solutions, then $ra + rb$ is equal to (1) rc (2) ra (3) rc (4) rb

Official Ans. by NTA (1)

$$\text{Sol. } D = \begin{vmatrix} 1 & 1 & a \\ 2 & 5 & 2 \\ 1 & 2 & 3 \end{vmatrix} = 0 \Rightarrow 11 - a = 0$$

$$a = 11$$

$$D1 = \begin{vmatrix} b & 1 & a \\ 6 & 5 & 2 \\ 3 & 2 & 3 \end{vmatrix} = 0 \Rightarrow 11b - 12 - 21 = 0$$

$$b = 3$$

$$ra + rb = rc$$

17. If $xy + yx = 2$, then $\frac{dy}{dx}$ at (x, y) is equal to

- (1) $-\frac{2 + \log_e 2}{2 + 8}$ (2) $-\frac{2 + \log_e 2}{3 + 8}$
 (3) $-\frac{3 + \log_e 16}{4 + \log_e 8}$ (4) $-\frac{3 + \log_e 4}{2 + \log_e 8}$

Official Ans. by NTA (2)

Sol. $xy + yx = 2$

$$2xy \frac{dy}{dx} + (\ln x) \frac{dy}{dx} + 3yx \frac{dy}{dx} + \ln y \frac{dy}{dx} = 0$$

$$y' = \frac{-(12 \ln 2 + 8)}{12 + 8 \ln 2} = -\frac{2 + \log_e 8}{3 + \log_e 4}$$

18. One vertex of a rectangular parallelepiped is at the origin O and the lengths of its edges along x, y and z axes are 3, 4 and 5 units respectively. Let P be the vertex (x, y, z) . Then the shortest distance between the diagonal OP and an edge parallel to z axis, not passing through O or P is:

- (1) $\frac{12}{\sqrt{5}}$ (2) $\frac{12}{5\sqrt{5}}$
 (3) $12\sqrt{5}$ (4) $\frac{12}{5}$

Official Ans. by NTA (4)

Sol. Equation of OP is $\frac{x}{3} = \frac{y}{4} = \frac{z}{5}$

$a = (3, 4, 5)$
 Equation of edge parallel to z axis
 $b = (0, 0, 1)$

axis

$$\frac{x-3}{0} = \frac{y-0}{0} = \frac{z-5}{1}$$

$$S.D = \frac{(a_2 - a_1) \cdot (b_1 - b_2)}{|b_1 - b_2|}$$

$$\begin{vmatrix} 3 & 0 & 5 \\ 3 & 4 & 5 \\ 0 & 0 & 1 \end{vmatrix} = 3(4) = 12$$

$$\begin{vmatrix} 3 & 4 & 5 \\ 3 & 0 & 5 \\ 0 & 0 & 1 \end{vmatrix} = 4(3) - 5(3) = 12 - 15 = -3$$

19. Let the position vectors of the points A, B, C and D be $5\hat{i} + 5\hat{j} + 2\hat{k}$, $\hat{i} + 2\hat{j} + 3\hat{k}$, $-2\hat{i} + \hat{j} + 4\hat{k}$ and $-\hat{i} + \hat{j} + \hat{k}$. Let the set $S = \{\hat{i}\}$. The points A, B, C and D are coplanar. Then $\frac{a}{(1+2)^2}$ is

to

- (1) 1 (2) 20
 (3) 13 (4) $\frac{37}{2}$

Official Ans. by NTA (1)

Sol. Since A, B, C, D are coplanar

Hence $\vec{r}_{BA} \cdot \vec{r}_{CA} \cdot \vec{r}_{DA} = 0$

$$\begin{vmatrix} 4 & 7 & 3 & 2 \\ 6 & 5 & 1 & 2 \\ 1 & 0 & 2 & 6 \end{vmatrix} = 0$$

$$2, 3 \text{ Hence } \frac{a}{(1+2)^2} = 41$$

20. Let $A = \{x \in \mathbb{I} : [x+3] + [x+4] \in 3\}$,

$B = \{x \in \mathbb{I} : 3x \in \mathbb{I}\}$, where $\{x\}$ denotes greatest integer function. Then,

(1) $A \cap B = \emptyset$

(2) $A = B$

(3) $B \subset A$, $A \not\subset B$

(4) $A \subset B$, $A \not\subset B$

Official Ans. by NTA (2)

Sol. $x] + 3 + [x + 4 \in 3$

$$2[x] + 4$$

$$x] - 2 \quad x \in (-\frac{1}{2}, -\frac{1}{3}, \dots) \dots (A)$$

$$\frac{3 \times 10}{1 - 1} < 3^{-3x}$$

$$27 < 3 - 3x$$

$$-3x > +3$$

$$x > -1 \dots \dots \dots (B)$$

$$A = B$$

SECTION-B

21. Let $a \in \mathbb{R}$ and t be the greatest integer $> t$. Then the number of points, where the function $f(x) = a + \sin x$ is not differentiable, is _____

Official Ans. by NTA (20)

Sol. $f(x) = a + \sin x$, $x \in \mathbb{R}$
For $\sin x$: Total number of non differentiable points are $= 2n - 1$ for $x \in (0, p)$

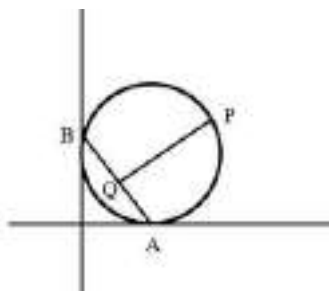
So number of non differentiable points for $\sin x$

$x \in \mathbb{R}$ 20 Points

22. A circle passing through the point $P(a, b)$ in the first quadrant touches the two coordinate axes at the points A and B. The point P is above the line AB. The point Q on the line segment AB is the foot of perpendicular from P on AB. If PQ is equal to 11 units, then the value of ab is _____

Official Ans. by NTA (121)

Sol.



Let equation of circle is $(x-a)^2 + (y-a)^2 = a^2$ which is passing through $P(a, b)$

then $(a-a)^2 + (b-a)^2 = a^2$

$$a^2 + b^2 - 2ab + a^2 = 0$$

Here equation of AB is $x + y = a$

Let $Q(a', b')$ be foot of perpendicular of P on AB

$$\frac{a' - a}{1} = \frac{b' - b}{1} = \frac{-(a + b - a)}{2}$$

$$PQ^2 = (a' - a)^2 + (b' - b)^2 = \frac{1}{4}(a + b - a)^2 + \frac{1}{4}(a + b - a)^2$$

$$121 = \frac{1}{2}(a + b - a)^2$$

$$242 = a^2 + b^2 - 2ab + a^2 + 2ab$$

$$242 = 2a^2 + 2b^2 - 2ab + 2ab$$

$$121 = a^2 + b^2 - ab$$

23. The number of ways of giving 20 distinct oranges to 3 children such that each child gets at least one orange is _____

Official Ans. by NTA (171)

24. In the distinct oranges distributed among 3 children so

that each child gets at least one orange

$$= {}^{20}C_1 - {}^3C_1 {}^{19}C_0 + {}^3C_2 {}^{18}C_0$$

Bonus

If the area of the region

24.

$S = \{(x, y) : 2y \leq x^2 \leq 2y, x^3 \leq y\}$ is equal to

$\frac{n+1}{n} - \frac{p}{n-1}$, then the natural number n is equal to

Official Ans. by NTA (0)

Sol. $x^2 + y^2 - 2y^3 \geq 0$ & $x^2 - 2y \leq 0$, $x^3 \leq y$

Hence required area $= \int_0^1 \left(\frac{x^2}{2} - \frac{x^3}{3} \right) dx = \frac{1}{24}$

$$= \frac{7}{6} - \frac{1}{2} = \frac{5}{6} \quad n = 0$$

25. Let the point $(p, p+1)$ lie inside the region

$E = \{(x, y) : 2y \leq x^2 \leq 2y, x^3 \leq y\}$

all values of p is the interval (a, b) . then $b^2 + b - a^2$ is equal to _____

Official Ans. by NTA (2)

Sol. $3 - x \in y \in \sqrt{9 - x^2}$

Points $(p, p+1)$ lies on $y = x+1$

So point of intersection between

$y = x+1$ & $y = \sqrt{9 - x^2}$ is $x = -1, y = 2$

and point of intersection between

$x+1 = \sqrt{9 - x^2}$ is $x = \frac{-1 + \sqrt{17}}{2}$

Hence $\frac{2}{\sqrt{17}}$

Hence $b^2 + b - a^2 = 2$

26. Let $y = y(x)$ be a solution of the differential equation $(x \cos x) dy + (x y \sin x + y \cos x - 1) dx = 0$

$0 < x < \frac{\pi}{2}$. If $\frac{dy}{dx} + \frac{y}{x} = \frac{1}{x \cos x}$, then

$\left| \frac{dy}{dx} + \frac{y}{x} - \frac{1}{x \cos x} \right|$ is equal to _____

Official Ans. by NTA (2)

Sol. $(x \cos x) dy + (x y \sin x + y \cos x - 1) dx = 0$ $0 < x < \frac{\pi}{2}$

$\frac{dy}{dx} + \frac{y}{x} = \frac{1}{x \cos x}$

IF = $x \sec x$

$y \cdot x \sec x = \int \sec x dx = \tan x + c$

Since $y = \frac{3\sqrt{3}}{p}$

Hence $c = \sqrt{3}$

Hence $\left| \frac{dy}{dx} + \frac{y}{x} - \frac{1}{x \cos x} \right| = 2$

27. The coefficient of x^{14} in the expansion of

$\frac{x^4}{e} - \frac{1}{x^3}$ is _____

Official Ans. by NTA (000)

Sol. $\frac{x^4}{e} - \frac{1}{x^3}$

$T_{r+1} = \frac{1}{e} \cdot \frac{1}{x^3} \cdot \frac{1}{x^3}$

$1 - \sqrt{e} = 18$

$r = 6$

Hence coeff. of $x^{14} = 10C6 = 210$

28. Let $A = \{1, 2, 3, 4, \dots, 10\}$ and $B = \{0, 1, 2, 3, 4\}$.

The number of elements in the relation $R = \{(a, b) \in A \times A : (a-b) \in B\}$ is _____

$A \times A : (a-b) \in B$ is _____

Official Ans. by NTA (18)

Sol. $A = \{1, 2, 3, \dots, 10\}$

$B = \{0, 1, 2, 3, 4\}$

$R = \{(a, b) \in A \times A : (a-b) \in B\}$

Now $2(a-b) + 3(a-b) = (a-b)(2(a-b)+3)$

$a = b$ or $a-b = -2$

When $a-b = -2$, order pairs

Total = 18 order pairs

Let the image of the point $P(1, 2, 3)$ in the plane $x - y + z = 9$ be Q . If the coordinates of the point R are $(1, 1, 1)$, then the square of the area of the triangle PQR is _____

29. Let $Q(a, b, g)$ be the image of P about the plane $x - y + z = 9$. If the coordinates of the point R are $(1, 1, 1)$, then the square of the area of the triangle PQR is _____

Official Ans. by NTA (094)

Sol. Let $Q(a, b, g)$ be the image of P about the plane

$x - y + z = 9$

$\frac{a-1}{2} = \frac{b-2}{-1} = \frac{g-3}{1} = 2$

$a=5, b=0, g=5$

Then area of triangle $PQR = \frac{1}{2} |PQ \times PR|$

$= \frac{1}{2} |12i - 3j + 21k| = \frac{1}{2} \sqrt{144 + 9 + 441} = \frac{1}{2} \sqrt{594}$

Square of area = 094

30. Let the tangent to the curve $x^2 + 2x - 3y + 4 = 0$ at the point $P(1, 3)$ on it meet the y-axis at A. Let the line passing through P and parallel to the line $x - 3y = 6$ meet the parabola $y^2 = 4x$ at B. If B lies on the line $2x - 3y = 8$, then $(AB)^2$ is equal to

Official Ans. by NTA (292)

Sol. Equation of tangent at $P(1, 3)$ to the curve

$$x^2 + 2x - 3y + 4 = 0 \text{ is } y - x = 2$$

Then the point A is $(0, 2)$

Equation of line passing through P and parallel to the line $x - 3y = 6$.

The possible coordinate of B are $(4, 4)$ or $(16, 8)$

But $(4, 4)$ does not satisfy $2x - 3y = 8$

Thus the point B is $(16, 8)$

Then $(AB)^2 = 292$

PHYSICS

SECTION-A

31. For the plane electromagnetic wave given by $E = E_0 \sin(\omega t - kx)$ and $B = B_0 \sin(\omega t - kx)$, the ratio of average electric energy density to average magnetic energy density is

- (1) 1 (2) $1/2$
(3) 2 (4) 2

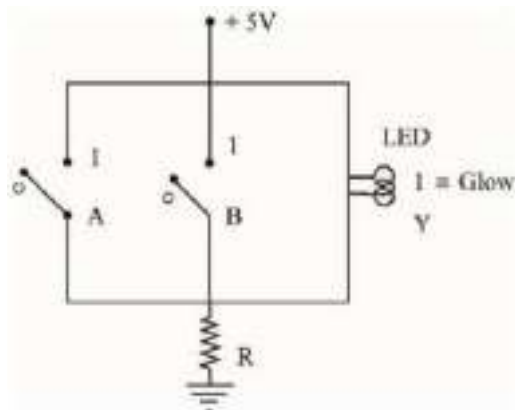
Official Ans. by NTA (1)

Sol.
$$\frac{\text{Electric energy density}}{\text{Magnetic energy density}} = \frac{\frac{1}{2} \epsilon_0 E_{rms}^2}{\frac{1}{2} \mu_0 B_{rms}^2}$$

$$\frac{E_{rms}}{B_{rms}} = \frac{1}{\epsilon_0 \mu_0} = c$$

$$\frac{E_{rms}}{B_{rms}} = c$$

32. Name the logic gate equivalent to the diagram attached



- (1) OR (2) NOR
(3) NAND (4) AND

Official Ans. by NTA (2)

Sol. Circuit is closed when neither A nor B is closed. Current flows for $A = 0$, $B = 0$. When either or both of A & B is closed we get current bypass from switch.

Hence it is "NOR" gate

TEST PAPER WITH SOLUTION

33. A small ball of mass M and density ρ is dropped in a viscous liquid of density ρ_0 . After some time, the ball falls with a constant velocity. What is the viscous force on the ball?

- (1) $F = Mg$ (2) $F = Mg \frac{\rho_0}{\rho}$
(3) $F = Mg \frac{\rho}{\rho_0}$ (4) $F = Mg(1 - \frac{\rho_0}{\rho})$

Official Ans. by NTA (1)

$$F_{vis} = Mg$$

Sol.

$$F_{vis} + Mg = Mg$$

$$F_{vis} = Mg - Mg$$

$$F_{vis} = Mg(1 - \frac{\rho_0}{\rho})$$

34. The number of air molecules per cm^3 increased from 3×10^{20} to 12×10^{20} . The ratio of collision frequency of air molecules before and after the increase in number respectively is

- (1) 1:20 (2) 1:20
(3) 1:40 (4) 1:50

Official Ans. by NTA (2)

Sol. Collision frequency,

$$f = \frac{1}{4} n \bar{v} \sigma$$

$$f = n \bar{v} \sigma$$

$$\frac{f_1}{f_2} = \frac{n_1 \bar{v}_1 \sigma_1}{n_2 \bar{v}_2 \sigma_2}$$

35. A source supplies heat to a system at the rate of 1000 W . If the system performs work at a rate of 200 W . The rate at which internal energy of the system increases (1) 1200 W (2) 800 W (3) 1000 W (4) 1800 W

Official Ans. by NTA (2)
(2) 800 W

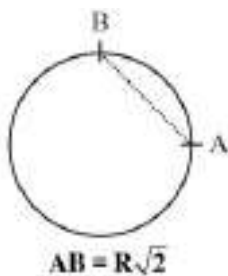
Sol. $dQ = dU + dw$

$$\frac{dU}{dt} = \frac{dQ}{dt} - \frac{dw}{dt}$$

$$\frac{dU}{dt} = 1000 - 200 = 800 \text{ W}$$

36. A particle is moving with constant speed in a circular path. When the particle turns by an angle 90° , the ratio of instantaneous velocity to its average velocity is $\frac{1}{x}$. The value of x will be (1) 2 (2) 5 (3) 1 (4) 7

Official Ans. by NTA (1)
(1) 2



Sol.

Let instantaneous velocity be v . time.

$$t = \frac{\text{Arc length}}{v} = \frac{R \cdot \frac{\pi}{2}}{v} = \frac{\pi R}{2v}$$

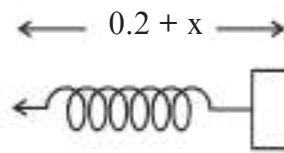
average velocity.

$$\frac{AB}{t} = \frac{R\sqrt{2}}{\frac{\pi R}{2v}} = \frac{2v\sqrt{2}}{\pi}$$

37. A small block of mass 100 g is tied to a spring of spring constant 100 N/m and length 20 cm . The other end of spring is fixed at a particular point A. If the block moves in a circular path on a smooth horizontal surface with constant angular velocity 2 rad/s about point A, then tension in the spring is (1) 1.0 N (2) 0.70 N (3) 0.20 N (4) 0.50 N

Official Ans. by NTA (2)
(2) 0.70 N

Official Ans. by NTA (2)



Sol.

$$kx = m\omega^2 r$$

Let extension in length of spring be x .

Radius of circle $r = 0.2 + x$

$$Kx = m\omega^2 r$$

$$100x = 0.1 \times 10 \times (2)^2 (0.2 + x)$$

$$100x = 4(0.2 + x)$$

$$100x = 0.8 + 4x$$

$$Tension \text{ in spring } = kx = 100 \times 0.008 = 0.8 \text{ N}$$

38.

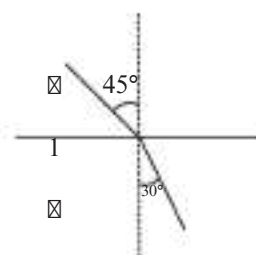
A monochromatic light wave with wavelength λ_1 and frequency ν_1 in air enters another medium. If the angle of incidence and angle of refraction at the interface are 45° and 30° respectively, then the wavelength λ_2 and frequency ν_2 of the refracted wave are :

(1) $\frac{\lambda_1}{\sqrt{2}}, \frac{\nu_1}{\sqrt{2}}$ (2) $\frac{\lambda_1}{\sqrt{2}}, \nu_1$

(3) $\lambda_1 \sqrt{2}, \frac{\nu_1}{\sqrt{2}}$ (4) $\lambda_1 \sqrt{2}, \nu_1$

Official Ans. by NTA (2)

Sol.



$$\text{Snell's law } \sin 45^\circ = \mu \sin 30^\circ$$

$$\frac{1}{\sqrt{2}} = \mu \cdot \frac{1}{2}$$

$$\mu = \frac{2}{\sqrt{2}} = \sqrt{2}$$

$$\lambda_2 = \frac{\lambda_1}{\mu} = \frac{\lambda_1}{\sqrt{2}}$$

Frequency doesn't change on change in medium.

39. Given below are two statements : one is labelled as Assertion A and the other is labelled as Reason R.
 Assertion A : When a body is projected at an angle θ° , its range is maximum.
 Reason R : For maximum range, the value of $\sin 2\theta$ should be equal to one.
 In the light of the above statements, choose the correct answer from the options given below :
 (1) Both A and R are correct but R is NOT the correct explanation of A
 (2) Both A and R are correct R is the correct explanation of A
 (3) A is true but R is false
 (4) A is false but R is true
 Official Ans. by NTA (2)

Sol. $R = \frac{u^2 \sin 2\theta}{g}$

R is maximum for $2\theta = 90^\circ$.

40. Two resistances are given as $R_1(100 \pm 5)\Omega$ and $R_2(150 \pm 5)\Omega$. The percentage error in the measurement of equivalent resistance when they are connected in parallel is
 (1) 6.33 (2) 2.33
 (3) 4.33 (4) 5.33
 Official Ans. by NTA (3)

Sol. $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$

Differentiating both sides, we get

$$\frac{-1}{R^2} dR = \frac{-1}{R_1^2} dR_1 + \frac{-1}{R_2^2} dR_2$$

$$\frac{dR}{R} = \frac{R_2^2}{R^2} \frac{dR_1}{R_1} + \frac{R_1^2}{R^2} \frac{dR_2}{R_2}$$

$$\frac{dR}{R} = \frac{R_2^2}{R^2} \frac{5}{100} + \frac{R_1^2}{R^2} \frac{5}{150}$$

$$\frac{dR}{R} = \frac{1}{20} + \frac{1}{12} = \frac{3}{60} + \frac{5}{60} = \frac{8}{60} = \frac{2}{15}$$

$$\frac{dR}{R} = 13.33\%$$

A planet has double the mass of the earth. Its average density is equal to the that of the earth. An object weighing W on earth will weigh on that planet :

- (1) $\frac{1}{2}W$
 (2) W
 (3) $2W$
 (4) $\frac{1}{3}W$

Official Ans. by NTA (3)

Sol. $m \propto R^3$

$R \propto m^{\frac{1}{3}}$ (constant)

weight $\propto W_g \propto \frac{Gm}{R^2}$

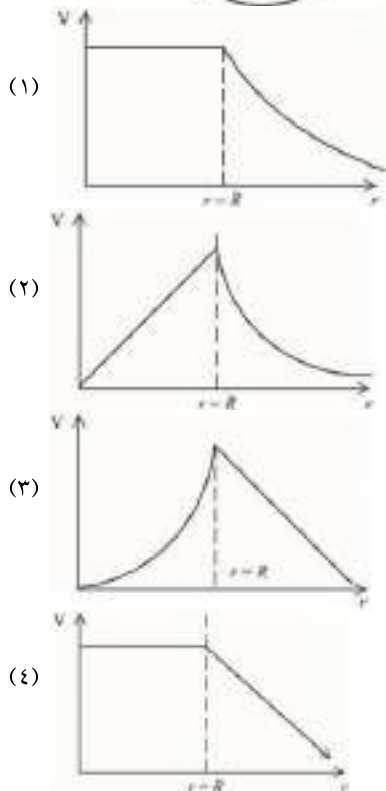
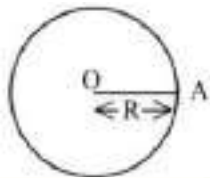
$W \propto \frac{m}{R^2} \propto m^{1/3}$

So, $W_1 \propto (2)^{1/3} W$

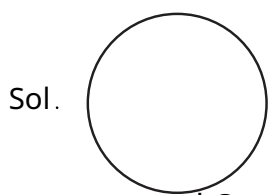
42. Given below are two statements : one is labelled as Assertion A and the other is labelled as Reason R.
 Assertion A : Earth has atmosphere whereas moon doesn't have any atmosphere.
 Reason R : The escape velocity on moon is very small as compared to that on earth.
 In the light of the above statement, choose the correct answer from the options given below :
 (1) A is true but R is false
 (2) A is false but R is true
 (3) Both A and R are correct but R is NOT the correct explanation of A
 (4) Both A and R are correct and R is correct explanation of A
 Official Ans. by NTA (4)

Sol. At Moon, due to low escape velocity, the rms velocity of molecules is greater than escape velocity. Hence molecules escape and there is no atmosphere at Moon.

For a uniformly charged thin spherical shell, the electric potential (V) radially away from the center (O) of shell can be graphically represented as

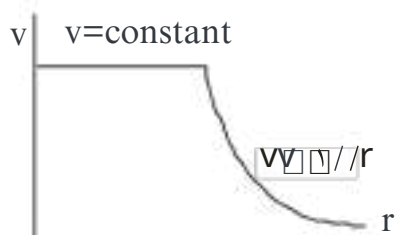


Official Ans. by NTA (1)

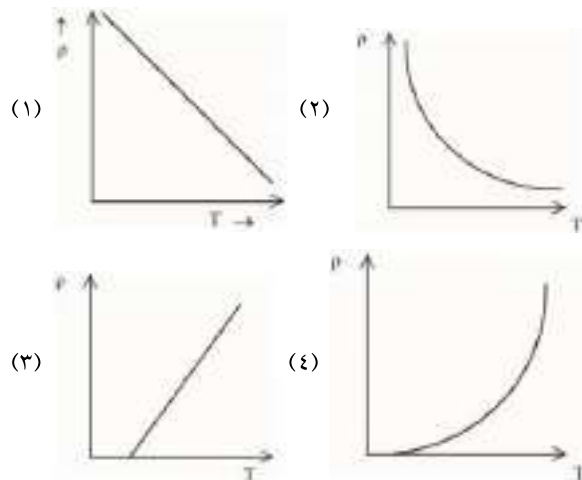


$$V_{\text{inside}} = \frac{kQ}{R}$$

$$V_{\text{outside}} = \frac{kQ}{r}$$



ξξ. The resistivity (ρ) of semiconductor varies with temperature. Which of the following curve represents the correct behaviour



Official Ans. by NTA (2)

Sol.

$$\rho = \frac{m}{ne^2 \tau}$$

With rise in temperature, number density (n) of electrons and holes increases for semiconductors. As m, e, τ are constant

$\rho \propto \frac{1}{n}$ Rectangular hyperbola

ξο. The kinetic energy of an electron, β -particle and a proton are given as $\epsilon K, \gamma K$ and K respectively. The de-Broglie wavelength associated with electron (λ_e), β -particle (λ_β) and the proton (λ_p) are as follows :

(1) $\lambda_\beta = \lambda_p > \lambda_e$

(2) $\lambda_\beta < \lambda_p < \lambda_e$

(3) $\lambda_\beta > \lambda_p > \lambda_e$

(4) $\lambda_\beta = \lambda_p < \lambda_e$

Official Ans. by NTA (2)

	Electron	Alpha	Proton
Mass :	m	$4m$	m
Charge :	e	$2e$	e
Kinetic energy	$4K$	$2K$	K
$\lambda = \frac{h}{\sqrt{2mK}}$	$\frac{h}{\sqrt{2m \cdot 4K}}$	$\frac{h}{\sqrt{2 \cdot 4m \cdot 2K}}$	$\frac{h}{\sqrt{2mK}}$

Sol.

ε 6.

By what percentage will the transmission range of a TV tower be affected when the height of the tower is increased by 1%?

- (1) 1% (2) 12%
(3) 10% (4) 15%

Official Ans. by NTA (3)

Sol.

Range, $R \propto \sqrt{h}$

$$R_1 \propto \sqrt{h_1}$$

$$h_1 \propto h_2 \Rightarrow \frac{R_1}{R_2} = \sqrt{\frac{h_1}{h_2}} = \sqrt{1.01} \approx 1.005$$

$$R_2 \propto \sqrt{h_2} \Rightarrow \frac{R_2}{R_1} = \sqrt{\frac{h_2}{h_1}} = \sqrt{1.01} \approx 1.005$$

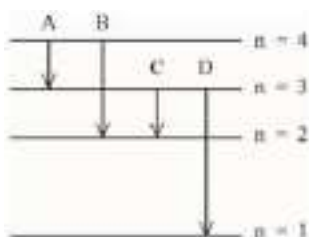
% increase in range

$$\frac{R_2 - R_1}{R_1} \times 100 = \frac{1.005R_1 - R_1}{R_1} \times 100 = 0.5\%$$

$$= (1.005 - 1) \times 100 = 0.5\%$$

ε 7.

The energy levels of an hydrogen atom are shown below. The transition corresponding to emission of shortest wavelength is



- (1) C (2) D (3) B (4) A

Official Ans. by NTA (2)

Sol.

$$E = \frac{hc}{\lambda} \Rightarrow \lambda = \frac{hc}{E}$$

For shortest wavelength, energy gap should be maximum.

So, correct choice is transition from $n = 4$ to $n = 1$.

ε 8.

A mass m is attached to two springs as shown in figure. The spring constants of two springs are K_1 and K_2 . For the frictionless surface, the time period of oscillation of mass m is



(1) $\frac{1}{2\pi} \sqrt{\frac{K_1 + K_2}{m}}$

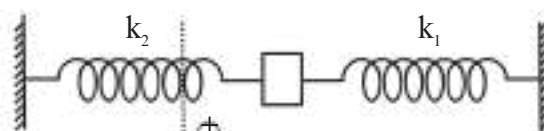
(2) $\frac{1}{2\pi} \sqrt{\frac{K_1 K_2}{m}}$

(3) $\frac{1}{2\pi} \sqrt{\frac{m}{K_1 + K_2}}$

(4) $\frac{1}{2\pi} \sqrt{\frac{m}{K_1 K_2}}$

Official Ans. by NTA (1)

Sol.



On displacing m to right by x

$$F = -(K_1 x + K_2 x) = -(K_1 + K_2)x$$

$$a = \frac{F}{m} = \frac{-(K_1 + K_2)x}{m} \Rightarrow \omega^2 = \frac{K_1 + K_2}{m}$$

$$T = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{m}{K_1 + K_2}}$$

ε 9.

The induced emf can be produced in a coil by
A. moving the coil with uniform speed inside magnetic field
B. moving the coil with non-uniform speed inside uniform magnetic field
C. rotating the coil inside the uniform magnetic field
D. changing the area of the coil inside the uniform magnetic field
Choose the correct answer from the options given below:

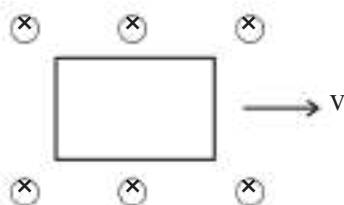
- (1) B and D only (2) A and C only

(3) B and C only

(4) C and D only

Official Ans. by NTA (2)

Sol.



Moving a coil inside a uniform magnetic field either with uniform or non-uniform speed doesn't change flux, so, no emf is induced.

- Q. A long straight wire of circular cross-section (radius a) is carrying steady current I . The current I is uniformly distributed across this cross-section. The magnetic field is
- Zero in the region $r > a$ and inversely proportional to r in the region $r < a$
 - Inversely proportional to r in the region $r > a$ and uniform throughout in the region $r < a$
 - Directly proportional to r in the region $r > a$ and inversely proportional to r in the region $r < a$
 - Uniform in the region $r > a$ and inversely proportional to distance r from the axis in the region $r < a$
- Official Ans. by NTA (c)

Sol.

$$B = \frac{\mu_0 I r}{2\pi a^2} \quad r \leq a$$

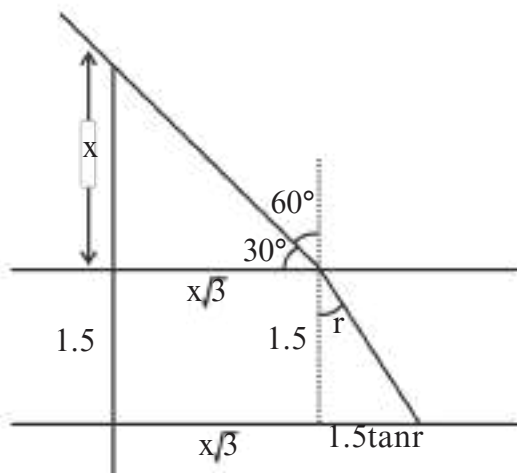
$$B = \frac{\mu_0 I}{2\pi r} \quad r \geq a$$

SECTION-B

- Q. A pole is vertically submerged in swimming pool, such that it gives a length of shadow 2.10 m within water when sunlight is incident at an angle of 30° with the surface of water. If swimming pool is filled to a height of 1.0 m, then the height of the pole above the water surface in centimetres is (NW = $\frac{1}{\sqrt{3}}$)

Official Ans. by NTA (50)

Sol.



By Snell's law

$$\sin 60^\circ = \frac{x}{2x} \Rightarrow \sin 60^\circ = \frac{1}{2} \Rightarrow \frac{\sqrt{3}}{2} = \frac{1}{2} \Rightarrow \tan 60^\circ = \frac{\sqrt{3}}{1} \Rightarrow \sqrt{3} = \frac{x}{1.5} \Rightarrow x = 1.5\sqrt{3}$$

By the diagram

$$x\sqrt{3} = 1.5 \tan 60^\circ = 1.5 \times \sqrt{3}$$

$$x\sqrt{3} = 2.10 - 1.5 \Rightarrow \frac{x\sqrt{3}}{\sqrt{3}} = \frac{0.6}{\sqrt{3}} \Rightarrow x = \frac{0.6}{\sqrt{3}}$$

$$x = \frac{2.10}{\sqrt{3}} - \frac{1.5}{\sqrt{3}}$$

$$= 1.241 - 0.866$$

$$= 0.375$$

$$= 0.375 \text{ meter}$$

Q.

- The length of a metallic wire is increased by 1% and its area of cross section is reduced by 1%. The percentage change in resistance of the metallic wire is
- Official Ans. by NTA (20)

Sol. $R = \frac{\rho l}{A}$ be the initial resistance new resistance

$$R' = \frac{1.01l}{0.99A} = 1.02 \times \frac{l}{A} = 1.02R$$

$$\text{percentage change} = \frac{R' - R}{R} \times 100 = 2\%$$

Q3. A particle of mass 1 kg moves in a straight line with retardation $\propto x$, where x is the displacement in SI units. Its loss of kinetic energy for above displacement is 10 J . The value of n will be

$\square \times \square$

Official Ans. by NTA (2)

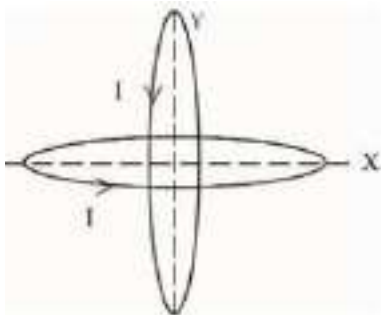
Sol. Loss of K.E = work done against retarding force

$$\int 0 \text{ to } x m a dx = \int 0 \text{ to } x m \propto x dx$$

$$(1 \times 10^2 \text{ kg}) \times \frac{1}{2} \times \frac{1}{x} \times x^2 = 10 \text{ J}$$

So $n = 2$

Q4. Two identical circular wires of radius 2 cm and carrying current 4 A are placed in perpendicular planes as shown in figure. The net magnetic field at the centre of the circular wire is $\square \times 10^{-5} \text{ T}$. (Take $\mu_0 = 4\pi \times 10^{-7} \text{ Tm/A}$)



Official Ans. by NTA (628)

Sol. Magnetic field BC at center $\frac{\mu_0 i}{2r}$

$$\frac{4\pi \times 10^{-7} \times 4}{2 \times 0.02} = \sqrt{2} \text{ T}$$

Net magnetic field is

$$BC = \sqrt{2} \times \frac{4\pi \times 10^{-7} \times 4}{2 \times 0.02} = 2\pi \times 10^{-5} \text{ T}$$

$$2\pi \times 10^{-5} \text{ T}$$

$$2\pi \times 10^{-5} \text{ T}$$

$$628 \times 10^{-5} \text{ T}$$

Q5. A person driving car at a constant speed of 10 m/s is approaching a vertical wall. The person notices a change of 2 Hz in the frequency of his car's horn upon reflection from the wall. The frequency of horn is _____ Hz.

(Given : Speed of sound : 330 m/s)

Official Ans. by NTA (220)

Sol. Frequency of reflected sound $f' = \frac{v + v_o}{v - v_s} f$

$$f' = \frac{330 + 10}{330 - 10} f$$

$$\frac{340}{320} f$$

$$\frac{340}{320} f - f = 2$$

$$\frac{30}{320} f = 2$$

$$f = \frac{2 \times 320}{30} = 42.67 \text{ Hz}$$

Q6. The radius of fifth orbit of the Li^{2+} is _____ \AA . m. Take : radius of hydrogen atom = 0.51 \AA

Official Ans. by NTA (220)

Sol. $r_n = n^2 \times \frac{a_0}{Z}$ $r_5 = 5^2 \times \frac{0.51}{3} \text{ \AA}$

$$= 42.5 \times 10^{-12} \text{ m}$$

Q7. A steel rod has a radius of 2 mm and a length of 2 m . A force of 62.8 kN stretches it along its length. Young's modulus of steel is $2.0 \times 10^{11} \text{ N/m}^2$. The longitudinal strain produced in the wire is _____ $\times 10^{-3}$

Official Ans. by NTA (20)

Sol. Strain $\square \frac{\text{stress}}{Y} \square \frac{62.8 \times 10^7}{2 \times 10^{11}}$

$$\square \frac{62.8 \times 10^7}{2 \times 10^{11}}$$

$$= 2.5 \times 10^{-4}$$

$$= 25 \times 10^{-6}$$

An ideal transformer with purely resistive load operates at 12 kV on the primary side. It supplies electrical energy to a number of nearby houses at 120 V. The average rate of energy consumption in the houses served by the transformer is 6 kW. The value of resistive load (R_s) required in the secondary circuit will be _____ m Ω .

Official Ans. by NTA (240)

Sol. $v_p = 12 \times 10^3$ volts

$$v_s = 120 \text{ volts}$$

$$p_s = 6 \text{ KW} = v_s \times i_s$$

$$i_s \square \frac{6 \times 10^3}{120} \square 50 \text{ A}$$

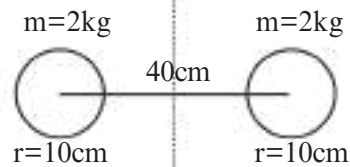
$$R_L \square \frac{V_s}{I_s} \square \frac{120}{50 \times 10^{-3}} \square 2400 \square 24 \times 10^2 \square 24 \times 10^3 \square 24 \text{ m}\Omega$$

$$= 24 \times 10^3 \text{ m}\Omega$$

Two identical solid spheres each of mass 2 kg and radii 10 cm are fixed at the ends of a light rod. The separation between the centres of the spheres is 40 cm. The moment of inertia of the system about an axis perpendicular to the rod passing through its middle point is _____ $\times 10^3$ kg-m

Official Ans. by NTA (176)

Sol.



$$I \square \int r^2 dm$$

$$\square \int \frac{2m}{\pi} r^2 dm$$

$$\square \frac{2}{\pi} \int r^2 dm$$

$$\square \frac{2}{\pi} \int r^2 dm$$

$$\square \frac{2}{\pi} \int r^2 dm$$

$$I \square 176 \times 10^3 \text{ kg m}^2$$

A parallel plate capacitor with plate area A and plate separation d is filled with a dielectric material of dielectric constant $K = \epsilon$. The thickness of the dielectric material is x, where $x > d$.



Let C_1 and C_2 be the capacitance of the system for $x < d$ and $x > d$, respectively. If $C_1 = 2$ F the

value of C_2 is _____ F

Official Ans. by NTA (3)

Sol. For $x = \frac{d}{2}$

$$C_1 \square \frac{\epsilon_0 \cdot A}{\frac{d}{2} + \frac{d}{2}} \square \frac{\epsilon_0 \cdot A}{d}$$

$$\square \frac{\epsilon_0 \cdot A}{d}$$

$$C_1 \square \frac{\epsilon \cdot A}{\frac{d}{2}} \square 2 \text{ F}$$

$$\text{for } x = \frac{d}{2}$$

$$C_2 \square \frac{\epsilon_0 \cdot A}{\frac{d}{2} + \frac{d}{2}} \square \frac{\epsilon_0 \cdot A}{d} \square 2$$

$$\square \frac{1}{2} \square 2 \square 1 \text{ F}$$

CHEMISTRY

SECTION-A

٦١. A compound is formed by two elements X and Y. The element Y forms cubic close packed arrangement and those of element X occupy one third of the tetrahedral voids. What is the formula of the compound?

- (١) X_2Y_3
 (٢) X_3Y
 (٣) X_3Y_2
 (٤) XY_3

Official Ans. by NTA (١)

Sol. Y : CCP \Rightarrow 4Y

$$X = \frac{1}{3} \text{ THV} = \frac{1}{3} \times 8 \times \frac{1}{8} = \frac{1}{3}$$

$$\text{Formula : } X_{\frac{1}{3}}Y_4 \text{ or } X_1Y_{12}$$

٦٢. Match List I with List II

List I		List II	
Element detected		Reagent used / Product formed	
A	Nitrogen	I.	$\text{Na}_2[\text{Fe}(\text{CN})_5\text{NO}]$
B	Sulphur	II.	AgNO_3
C	Phosphorous	III.	$\text{Fe}_4[\text{Fe}(\text{CN})_6]_3$
D	Halogen	IV.	$(\text{NH}_4)_2\text{MoO}_4$

Choose the correct answer from the options given below:

- (١) A-II, B-IV, C-I, D-III
 (٢) A-IV, B-II, C-I, D-III
 (٣) A-II, B-I, C-IV, D-III
 (٤) A-III, B-I, C-IV, D-II

Official Ans. by NTA (٤)

Nitrogen detection by lassaingne's method



(Prussian blue)

Sulphur detection by Sodium nitroprusside

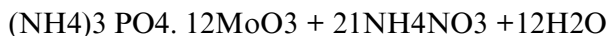
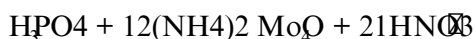


[Purple]

Phosphorus detection by ammonium molybdate

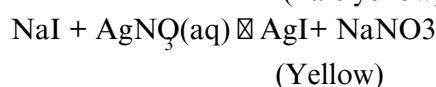
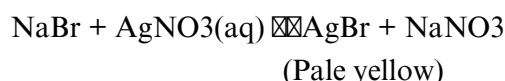
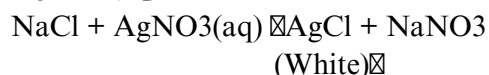


TEST PAPER WITH SOLUTION



(canary yellow)

Halogen give specific coloured ppt with $\text{AgNO}_3(\text{aq})$



٦٣. The standard electrode potential of M/M in aqueous solution does not depend on

- (١) Ionisation of a solid metal atom
 (٢) Sublimation of a solid metal
 (٣) Ionisation of a gaseous metal atom
 (٤) Hydration of a gaseous metal ion

Official Ans. by NTA (١)

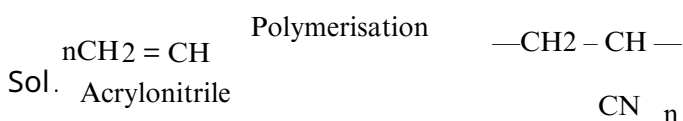
Sol. Factual

٦٤. Polymer used in orlon is:

- (١) Polyacrylonitrile
 (٢) Polyethylene
 (٣) Polycarbonate
 (٤) Polyamide

Official Ans. by NTA (١)

CN



Polyacrylonitrile
(Orlon)

٦٥. The difference between electron gain enthalpies will be maximum between:

- (١) Ne and F
 (٢) Ne and Cl
 (٣) Ar and Cl
 (٤) Ar and F

Official Ans. by NTA (٢)

- Sol. Cl has the most negative ΔH_{eg} among all the elements and Ne has the most positive ΔH_{eg} .

76. Match List I with List II

List I Enzymatic reaction	List II Enzyme
A Sucrose \rightarrow Glucose and Fructose	I. Zymase
B Glucose \rightarrow Ethyl alcohol and CO ₂	II. Pepsin
C Starch \rightarrow Maltose	III. Invertase
D Proteins \rightarrow Amino acids	IV. Diastase

Choose the correct answer from the options given below:

(1) A-III, B-I, C-II, D-IV

(2) A-I, B-IV, C-III, D-II

(3) A-III, B-I, C-IV, D-II

(4) A-I, B-II, C-IV, D-III

Official Ans. by NTA (3)

Sol. Factual

77. The possibility of photochemical smog formation is more at

(1) The places with healthy vegetation

(2) Himalayan villages in winter

(3) Marshy lands

(4) Industrial areas

Official Ans. by NTA (4)

Sol. Photochemical smog formation occurs in sunny climate. The main components come from the action of sunlight on unsaturated hydrocarbon and nitrogen oxides produced by automobiles and factories.

The setting time of Cement is increased by adding

(1) Clay

(2) Silica

(3) Limestone

(4) Gypsum

Official Ans. by NTA (4)

Sol. Factual

79. Given below are two statements: one is labelled as assertion and the other is labelled as reason.

Assertion: Loss of electron from hydrogen atom results in nucleus of $\sim 1.0 \times 10^{-17}$ pm size.

Reason: Proton (H) always exists in combined form

In the light of the above statements, choose the most appropriate answer from the options given below:

(1) Both A and R are correct and R is the correct explanation of A

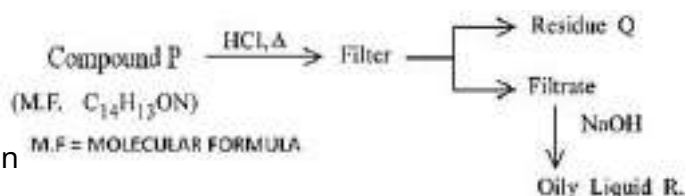
(2) A is correct but R is not correct

(3) A is not correct but R is correct

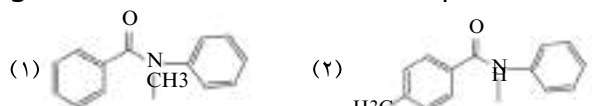
(4) Both A and R are correct but R is NOT the correct explanation of A.

Official Ans. by NTA (4)

Sol. Factual

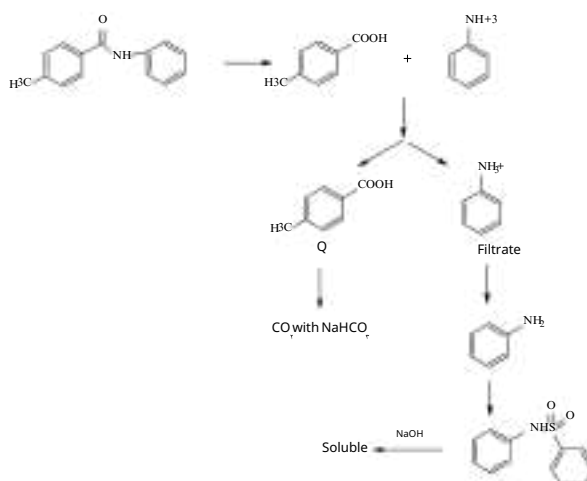


Compound P is neutral. Q gives effervescence with $NaHCO_3$ while R reacts with Hinsberg's reagent to give solid soluble in NaOH. Compound P is



(3) CC(=O)Nc1ccc2ccccc2c1 (4) CC(=O)Nc1ccc2ccccc2c1
 Official Ans. by NTA (2)

Sol.



71. Match List I with List II

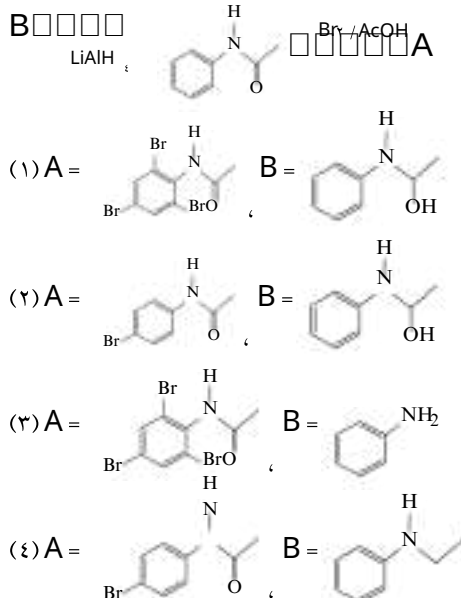
List I	List II
Name of reaction	Reagent used
A Hell-Volhard-Zelinsky reaction	I. NaOH + I ₂
B Iodoform reaction	II. (i) CrO ₂ Cl ₂ , CS ₂ (ii) H ₂ O
C Etard reaction Gatterman-Koch reaction	III. (i) Br ₂ /red phosphorus (ii) H ₂ O
D	IV. CO, HCl, anhyd. AlCl ₃

Choose the correct answer from the options given below:

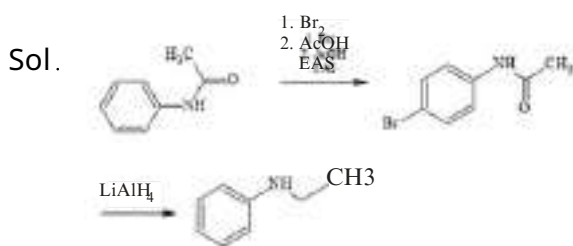
- (1) A-III, B-II, C-I, D-IV
 (2) A-III, B-I, C-IV, D-II
 (3) A-I, B-II, C-III, D-IV
 (4) A-III, B-I, C-II, D-IV
 Official Ans. by NTA (4)

Sol. HVZ reactions = Br₂ / red P
 Iodoform reaction = NaOH + I₂
 Etard reaction = (i) CrO₂Cl₂, CS₂ (ii) H₂O
 Gatterman-Koch Reaction = CO, HCl, Anhydrous, AlCl₃

72. The major products A and B from the following reactions are:



Official Ans. by NTA (4)

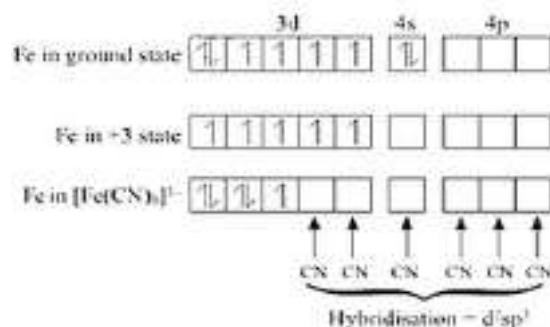


73. Given below are two statements, one is labelled as Assertion A and the other is labelled as Reason R.
 Assertion A: The spin only magnetic moment value for $\text{Fe}(\text{CN})_6^{4-}$ is 1.73 BM, whereas for $\text{Fe}(\text{H}_2\text{O})_6^{3+}$ is 5.92 BM.
 Reason R: In both complexes, Fe is present in +3 oxidation state.

In the light of the above statements, choose the correct answer from the options given below:

- (1) Both A and R are true but R is NOT the correct explanation of A
 (2) A is false but R is true
 (3) A is true but R is false
 (4) Both A and R are true and R is the correct explanation of A
 Official Ans. by NTA (1)

Sol. $\text{Fe}(\text{CN})_6^{4-}$



Unpaired electron = 1

$\mu = \sqrt{n(n+2)} = \sqrt{1(1+2)} = 1.73 \text{ B.M.}$

$\text{Fe}(\text{H}_2\text{O})_6^{3+}$: No pairing because H₂O is WFL
 Number of unpaired electrons = 5, $\mu = 5.92 \text{ BM}$
 Assertion is true. Reason is true but not correct explanation.

74. Match List I with List II

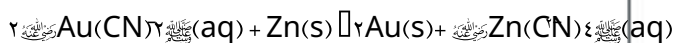
List I Vitamin	List II Deficiency disease
A Vitamin A	I. Beri-Beri
B Thiamine	II. Cheilosis
C Ascorbic acid	III. Xerophthalmia
D Riboflavin	IV. Scurvy

Choose the correct answer from the options given below:

- (1) A-IV, B-II, C-III, D-I (2) A-III, B-II, C-IV, D-I
 (3) A-IV, B-I, C-III, D-II (4) A-III, B-I, C-IV, D-II
 Official Ans. by NTA (4)

Sol. Factual

v5. Which of the following options are correct for the reaction

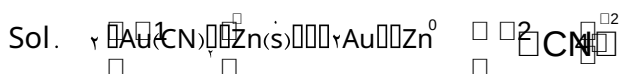


- A. Redox reaction
B. Displacement reaction
C. Decomposition reaction
D. Combination reaction

Choose the correct answer from the options given below:

- (1) A and B only (2) A only
(3) C and D only (4) A and D only

Official Ans. by NTA (1)



Zn displaced Au

Reduction and Oxidation both are taking place.

v6. Match List I with List II

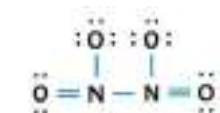
List I	List II
Oxide	Type of Bond
A. N_2O	I. 1N = O bond
B. NO_2	II. 1N - O - N bond
C. N_2O_5	III. 1N - N bond
D. N_2O	IV. 1N = N / N - N bond

Choose the correct answer from the options given below:

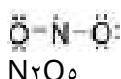
- (1) A-II, B-IV, C-III, D-I
(2) A-II, B-I, C-III, D-IV
(3) A-III, B-I, C-IV, D-II
(4) A-III, B-I, C-II, D-IV

Official Ans. by NTA (4)

Sol. N_2O_5



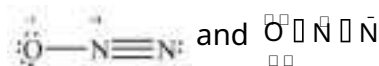
NO_2



N_2O



N_2O



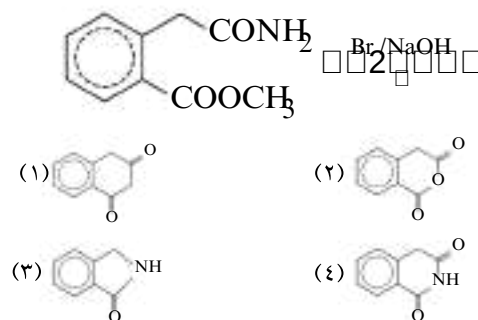
and $\text{O}=\text{N}-\text{N}$

Strong reducing and oxidizing agents among the following, respectively, are

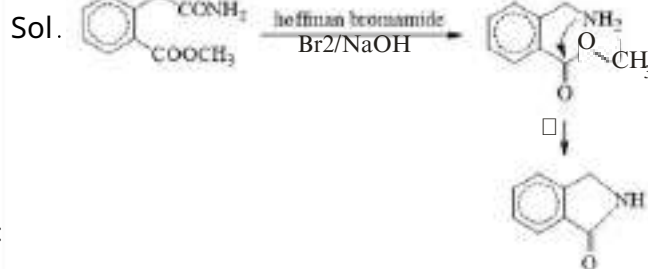
- (1) Ce^{4+} and Eu^{3+} (2) Ce^{3+} and Tb^{3+}
Official Ans. by NTA (2)

Sol. Factual

The major product formed in the following reaction is



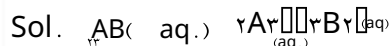
Official Ans. by NTA (3)



v9. For a concentrated solution of a weak electrolyte (K_{eq} = equilibrium constant) $\text{A} \rightleftharpoons \text{B} + \text{C}$ of concentration 'c', the degree of dissociation α is

- (1) $\frac{K_{eq}}{1 + \alpha c}$ (2) $\frac{K_{eq}}{1 + c}$
(3) $\frac{K_{eq}}{1 + 5c}$ (4) $\frac{K_{eq}}{1 + c^2}$

Official Ans. by NTA (1)



$$K_{eq} = \frac{[\text{A}][\text{B}]}{[\text{AB}]}$$

$$K_{eq} = \frac{1 + \alpha c}{c} = \frac{K_{eq}}{1 + \alpha c}$$

$$\text{RCHBr} \xrightarrow{\gamma} \text{A} \xrightarrow{\text{ceto}} \text{ne} \xrightarrow{\gamma} \text{RCHI} \xrightarrow{\text{major}} \text{Br}$$

Official Ans. by NTA (1)

So only (1) is correct

Official Ans. by NTA (v)

Therefore Ans = y

D Wrong

84. Mass of Urea (NH_2CONH_2) required to be dissolved in 100 g of water to reduce the vapour pressure of water by 2% is ... g. (Nearest integer)

Given: Molar mass of N, C, O and H are 14, 12, and 16 mol respectively.

Official Ans. by NTA (1111)

$$\text{Sol. } \frac{P_s - P}{P_s} = \frac{n_{\text{solute}}}{n_{\text{solvent}}} = \frac{x}{\frac{100}{18}} = \frac{P_s - P}{P_s} = \frac{2}{100}$$

$$\Rightarrow x = \frac{2 \times 100 \times 18}{100} = 3.6 \text{ gm}$$

Ans: 1111

85. The value of $\log K$ for the reaction $\text{A} \rightleftharpoons \text{B}$ at 298 K is ... (Nearest integer)

Given: $\Delta H = -54.07 \text{ kJ mol}^{-1}$

$\Delta S = 10 \text{ JK mol}^{-1}$

(Take $2.303 \times 8.314 \times 298 = 5705$)

Official Ans. by NTA (10)

$$\text{Sol. } G = H - TS$$

$$\Rightarrow G = (-54.070 - 10 \times 298)$$

$$\text{Also, } G = (-2.303 RT \log K)$$

$$\Rightarrow (-54.070 - 10 \times 298)$$

$$= (-2.303 \times 8.314 \times 298 \log K)$$

$$\Rightarrow \log K = 10 \text{ Ans: } 10$$

The number of species from the following which have square pyramidal structure is

86.

PF_5 , BrF_3 , IF_5 , BrF_3 , XeOF_4 , ICl_4

Official Ans. by NTA (3)

Sol. PF_5

sp^3d (0 lone pair)

Trigonal bipyramidal



BrF_3

sp^3d (2 lone pair)



square planar

IF_5

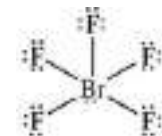
sp^3d (1 lone pair)



square pyramidal

BrF_5

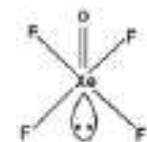
sp^3d (1 lone pair)



square pyramidal

XeOF_4

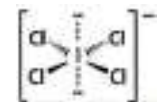
sp^3d (1 lone pair)



square pyramidal

ICl_4^-

sp^3d (2 lone pair)



square planar

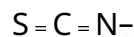
87.

Number of ambidentate ligands in a representative metal complex M(en)(SCN)_2 is

en = ethylenediamine

Official Ans. by NTA (2)

Sol. M(en)(SCN)_2



Ambidentate ligand means two ligand site, so ambidentate ligand is SCN.

Ans: 2

88. For the adsorption of hydrogen on platinum, the activation energy is 30 kJ mol^{-1} and for the adsorption of hydrogen on nickel, the activation energy is 51.5 kJ mol^{-1} . The logarithm of the ratio of the rates of chemisorption on equal areas of the metals at 300 K is ... (Nearest integer)

Given: $\ln 10 = 2.3$ $R = 8.3 \text{ JK mol}^{-1}$

Official Ans. by NTA (2)

Sol.
$$\frac{K_1}{K_2} = e^{\frac{E_a - E_a}{RT}}$$

$$\frac{K_1}{K_2} = e^{\frac{51.5 - 30}{8.3 \times 300}}$$

$$\log \frac{K_1}{K_2} = \frac{21.5}{24.9}$$

$$\log \frac{K_1}{K_2} = 0.863457$$

$$\frac{K_1}{K_2} = 7.31$$

Ans: 2

89. If 5 moles of BaCl_2 is mixed with 2 moles of Na_3PO_4 , the maximum number of moles of $\text{Ba}_3(\text{PO}_4)_2$ formed is ... (Nearest integer)

Official Ans. by NTA (1)



2 5

Na_3PO_4 is limiting reagent.

2 mole Na_3PO_4 gives 1 mole of $\text{Ba}_3(\text{PO}_4)_2$

Ans: 1

90. In ammonium-phosphomolybdate, the oxidation state of Mo is ...

Official Ans. by NTA (6)



Let X = oxidation state of Mo in MoO_4

$$X + (-2) \times 4 = 0$$

$$X = +6$$

Ans: 6