

AMU

Engineering Entrance Exam

Solved Paper 2020

Physics

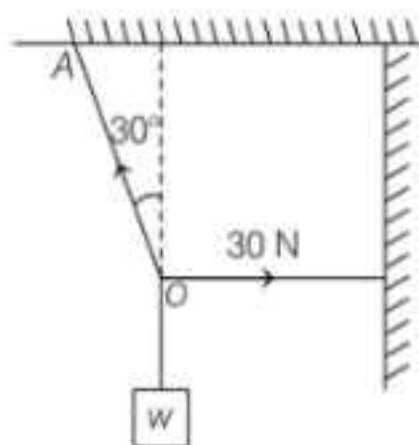
1. If L, C and R represent inductance, capacitance and resistance respectively, then which of the following does not represent dimensions of frequency?

(a) $\frac{1}{RC}$ (b) $\frac{R}{L}$
(c) $\frac{1}{\sqrt{LC}}$ (d) $\frac{C}{L}$

2. The pressure applied from all directions on a cube is p . How much its temperature should be raised to maintain the original volume? The volume elasticity of the cube is β and the coefficient of volume expansion is α .

(a) $\frac{\rho}{\alpha\beta}$ (b) $\frac{\rho\alpha}{\beta}$
(c) $\frac{\rho\beta}{\alpha}$ (d) $\frac{\alpha\beta}{\rho}$

3. As shown in figure, the tension in the horizontal cord is 30 N. The weight w and tension in the string OA in newton are

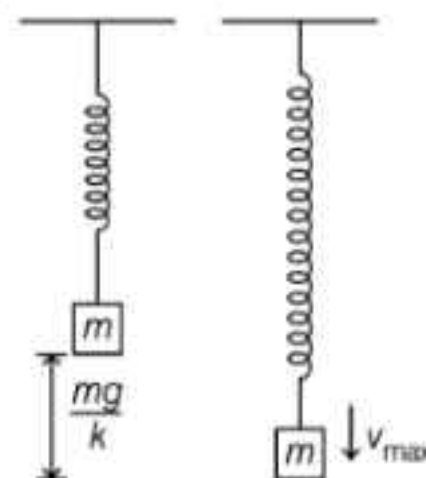


(a) $30\sqrt{3}, 30$ (b) $30\sqrt{3}, 60$
(c) $60\sqrt{3}, 30$ (d) None of these

4. A car turns a corner on a slippery road at a constant speed of 10 m/s. If the coefficient of friction is 0.5, the minimum radius of the arc in metre in which the car turns is

(a) 20 (b) 10 (c) 5 (d) 4

5. A particle suspended from a vertical spring oscillates 10 times per second. At the highest point of oscillation, the spring becomes unstretched. Find the speed when the spring is stretched by 0.20 cm. (Take, $g = \pi^2 \text{ m/s}^2$)

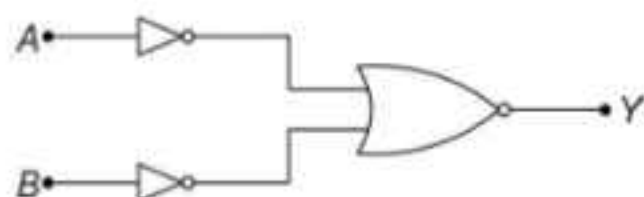


(a) 110.25 cm/s (b) 12.14 cm/s
(c) 15.4 cm/s (d) 16.7 cm/s

6. Two cells of equal emf and of internal resistances r_1 and r_2 ($r_1 > r_2$) are connected in series. On connecting this combination to an external resistance R , it is observed that the potential difference across the first cell becomes zero. The value of R will be

(a) $r_1 + r_2$ (b) $r_1 - r_2$
(c) $\frac{r_1 + r_2}{2}$ (d) $\frac{r_1 - r_2}{2}$

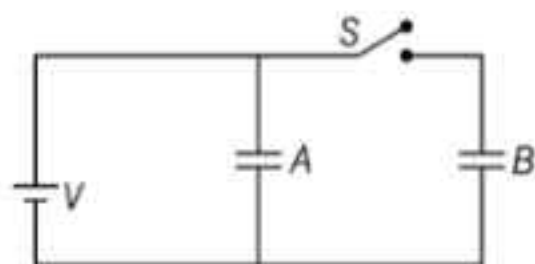
7. Which logic gate is represented by the following combination of logic gates?



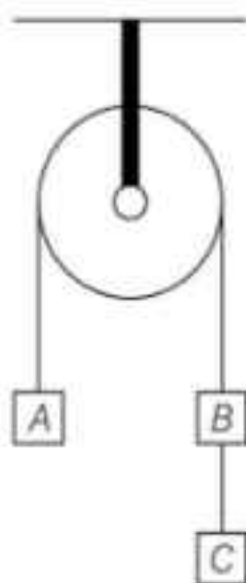
- (a) OR
(c) AND
- (b) NAND
(d) NOR
8. Calculate the electric and magnetic fields produced by the radiation coming from a $30\pi\text{W}$ bulb at a distance of 3 m. Assume that the efficiency of the bulb is 10% and it is a point source.
- (a) $0.22 \times 10^{-8} \text{ T}$
(b) $0.88 \times 10^{-6} \text{ T}$
(c) $0.22 \times 10^{-6} \text{ T}$
(d) $2.64 \times 10^{-8} \text{ T}$
9. One end of a uniform wire of length L and of weight w is attached rigidly to a point in the roof and a weight w_1 is suspended from its lower end. If S is the area of cross-section of the wire, then the stress in the wire at a height $\frac{3L}{4}$ from its lower end is
- (a) $\frac{w_1}{S}$
(c) $\frac{w_1 + (3w/4)}{S}$
- (b) $\frac{w_1 + (w/4)}{S}$
(d) $\frac{w_1 + w}{S}$
10. When a tuning fork A of frequency 100 Hz is sounded with a tuning fork B , the number of beats per second is 2. On putting some wax on the prongs of B , the number of beats per second becomes 1. The frequency of the fork B is
- (a) 98 Hz
(c) 101 Hz
- (b) 99 Hz
(d) 102 Hz
11. A 200 km long telegraph wire has a capacitance of $0.014 \mu\text{F/km}$. If it carries an alternating current of $50 \times 10^3 \text{ Hz}$, what should be the value of an inductance required to be connected in series, so that impedance is minimum?
- (a) $0.48 \times 10^{-2} \text{ mH}$
(c) $0.52 \times 10^{-2} \text{ mH}$
- (b) $0.36 \times 10^{-2} \text{ mH}$
(d) $0.49 \times 10^{-2} \text{ mH}$
12. The density of liquid contained in the tank of area 0.5 m^2 is 1200 kg/m^3 . It has a hole of area 1 cm^2 near the bottom. A load of 30 kg is applied on the liquid at the top. Find the velocity of efflux when the height of liquid level is 75 cm above the bottom. (Take, $g = 10 \text{ m/s}^2$)
- (a) 2 m/s
(b) 4 m/s
(c) 6 m/s
(d) 8 m/s
13. The rear side of a truck is open and a box of mass 2 kg is placed on the truck 8 m away from the open end. The truck starts from rest with an acceleration of 2 m/s^2 on a straight road. The box will fall off the truck when it is at distance from the starting point equal to
- (Given, $\mu = 0.1$ and $g = 10 \text{ m/s}^2$).
- (a) 4 m
(b) 8 m
(c) 12 m
(d) 16 m
14. In Young's double slit experiment, one of the slit is wider than another, so that amplitude of the light from one slit is double of that from other slit. If I_m be the maximum intensity, the resultant intensity I when they interfere at phase difference ϕ is given by
- (a) $\frac{I_m}{9}(4 + 5 \cos \phi)$
(c) $\frac{I_m}{5}\left(1 + 4 \cos^2 \frac{\phi}{2}\right)$
- (b) $\frac{I_m}{3}\left(1 + 2 \cos^2 \frac{\phi}{2}\right)$
(d) $\frac{I_m}{9}\left(1 + 8 \cos^2 \frac{\phi}{2}\right)$
15. The length of a magnet is large compared to its width and breadth. The time period of its oscillation in a vibration magnetometer is 2s. The magnet is cut along its length into three equal parts and three parts are then placed on each other with their like poles together. The time period of this combination will be
- (a) 2s
(b) $2/3\text{s}$
(c) $2\sqrt{3}\text{s}$
(d) $2/\sqrt{3}\text{s}$
16. A cubical box with porous walls containing an equal number of O_2 and H_2 molecules is placed in a larger evacuated chamber. The entire system is maintained at constant temperature T . The ratio of V_{rms} of O_2 molecules to that of the V_{rms} of H_2 molecules, found in the chamber outside the box after a short interval is
- (a) $\frac{1}{2\sqrt{2}}$
(b) $\frac{1}{4}$
(c) $\frac{1}{\sqrt{2}}$
(d) $\sqrt{2}$

17. Two stretched wires are in unison. If the tension in one of the wire is increased by 1%, 3beats are produced in 2s. The initial frequency of each wire is
(a) 150 Hz (b) 200 Hz (c) 300 Hz (d) 450 Hz

18. Figure given below shows two identical parallel plate capacitors connected to a battery with switch S closed. The switch is now opened and the free space between the plate of capacitors is filled with a dielectric of dielectric constant 2. What will be the ratio of total electrostatic energy stored in both capacitors before and after the introduction of the dielectric?



- (a) 2 : 1 (b) 5 : 1 (c) 4 : 5 (d) 5 : 4
19. A bullet of mass 10 g moving horizontally at a speed of 140 m/s strikes a block of mass 100 g attached to a string like a simple pendulum. The bullet penetrates the block and emerges then on the other side. If the block rises by 80 cm, then find the final velocity of bullet.
(a) 80 m/s (b) 100 m/s
(c) 120 m/s (d) 140 m/s
20. Three blocks A , B and C each of mass 2 kg, are hanging over a fixed pulley as shown in the figure. The tension in the string connecting B and C is



- (a) zero (b) 3.3 N (c) 13.3 N (d) 19.6 N

21. Two balls of masses m and $2m$ are attached to the ends of a light rod of length L . The rod rotates with an angular speed ω about an axis passing through the centre of mass of system and perpendicular to the plane. Find the angular momentum of the system about the axis of rotation.

- (a) $\frac{2}{3} m \omega L^2$ (b) $\frac{1}{3} \omega^2 L m$
(c) $\frac{2}{3} \omega^2 L m$ (d) $\frac{1}{3} L m$

22. A ray of light is incident on a surface of glass slab at an angle 45° . If the lateral shift produced per unit thickness is $1/\sqrt{3}$, then the angle of refraction produced is

- (a) $\tan^{-1}\left(\frac{\sqrt{3}}{2}\right)$ (b) $\tan^{-1}\left(1 - \sqrt{\frac{2}{3}}\right)$
(c) $\sin^{-1}\left(1 - \sqrt{\frac{2}{3}}\right)$ (d) $\tan^{-1}\left(\sqrt{\frac{2}{3-1}}\right)$

23. A shell bursts on contact with the ground and pieces from it fly in all directions with velocities upto 60 m/s. Find the time for which a man 180 m away is in danger.

- (a) $2\sqrt{3}$ s (b) $6\sqrt{2}$ s
(c) $4\sqrt{3}$ s (d) None of these

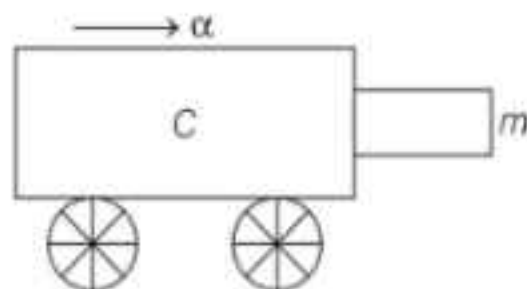
24. Two straight long conductors AOB and COD are perpendicular to each other and carry currents i_1 and i_2 . The magnitude of the magnetic induction at a point P at a distance a from the point O in a direction perpendicular to the plane $ABCD$ is

- (a) $\frac{\mu_0}{2\pi a} (i_1 + i_2)$ (b) $\frac{\mu_0}{2\pi a} (i_1 - i_2)$
(c) $\frac{\mu_0}{2\pi a} (i_1^2 + i_2^2)^{1/2}$ (d) $\frac{\mu_0}{2\pi a} \frac{i_1 i_2}{(i_1 + i_2)}$

25. The mean lives of a radioactive substance are 1620 yr and 405 yr for α -emission and β -emission, respectively. Find out the time during which three-fourth of a sample will decay, if it is decaying both by α -emission and β -emission simultaneously.

- (a) 643 yr (b) 449 yr
(c) 528 yr (d) 279 yr

26. A block of mass m is in contact with the cart C as shown in the figure.



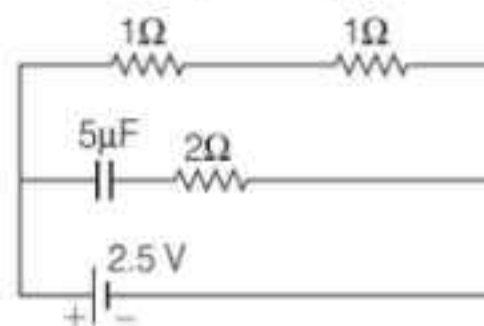
The coefficient of static friction between the block and the cart is μ . The acceleration α of the cart that will prevent the block from falling satisfies.

- (a) $\alpha > \frac{mg}{\mu}$ (b) $\alpha > \frac{g}{2\mu}$ (c) $\alpha \geq \frac{g}{\mu}$ (d) $\alpha < \frac{g}{\mu}$
27. Velocity of sound in a gaseous medium is 330 ms^{-1} . If the pressure is increased by 4 times without change in temperature, the velocity of sound in the gas is
(a) 330 ms^{-1} (b) 660 ms^{-1}
(c) 156 ms^{-1} (d) 990 ms^{-1}
28. Kepler's third law states that the square of period of revolution (T) of a planet around the sun, is proportional to third power of average distance, r between the sun and the planet
i.e. $T^2 = Kr^3$
Here, K is constant.
If masses of the sun and the planet are M and m respectively, then as per Newton's law of gravitation, force of attraction between them is $F = \frac{GMm}{r^2}$, where G is gravitational constant.
The relation between G and K is described as
(a) $GK = 4\pi^2$ (b) $GK = 4\pi^2$
(c) $K = G$ (d) $K = 1/G$

29. Two positive ions, each carrying a charge q are separated by a distance d . If F is the force of repulsion between the ions, the number of electrons missing from each ion will be (e being the charge on an electron)

(a) $\frac{4\pi\epsilon_0 Fd^2}{e^2}$ (b) $\sqrt{\frac{4\pi\epsilon_0 Fd^2}{e^2}}$
(c) $\sqrt{\frac{4\pi\epsilon_0 Fd^2}{e^2}}$ (d) $\frac{4\pi\epsilon_0 Fd^2}{q^2}$

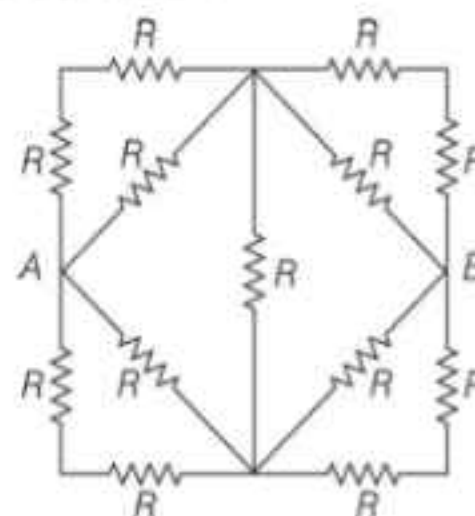
30. A capacitor of capacitance $5 \mu\text{F}$ is connected as shown in the figure. The internal resistance of the cell is 0.5Ω . The amount of charge on the capacitor plate is



- (a) zero (b) $5 \mu\text{C}$ (c) $10 \mu\text{C}$ (d) $25 \mu\text{C}$

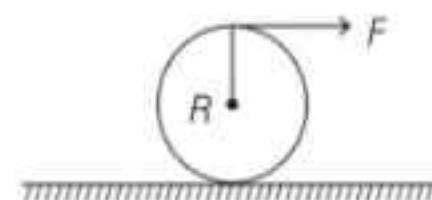
31. If pressure of CO_2 (real gas) in a container is given by $P = \frac{RT}{2v-b} - \frac{a}{4b^2}$, then mass of the gas in container is
(a) 11 g (b) 22 g (c) 33 g (d) 44 g

32. Thirteen resistances each of resistance R ohm are connected in the circuit as shown in the figure below. The effective resistance between A and B is



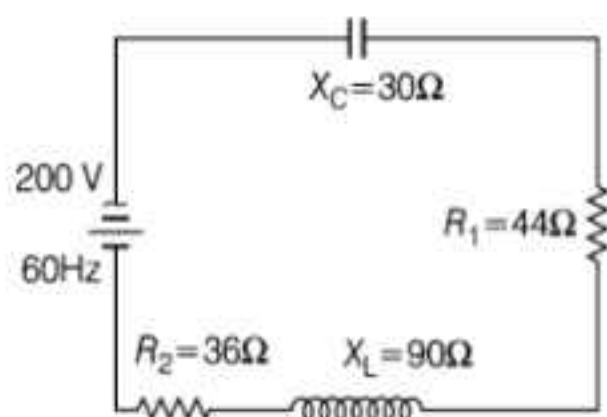
- (a) $R \Omega$ (b) $\frac{2R}{3} \Omega$
(c) $\frac{4R}{3} \Omega$ (d) $2R \Omega$

33. A tangential force F acts at the top of a thin spherical shell of mass ' m ' and radius R . The acceleration of the shell, if it rolls without slipping is



- (a) $\frac{5F}{6m}$ (b) $\frac{6F}{5m}$ (c) $\frac{7m}{2F}$ (d) $\frac{2m}{7F}$

34. As given in the figure a series circuit connected across a 200 V, 60 Hz line consists of a capacitor of capacitive reactance $30\ \Omega$, a non-inductive resistor of resistance $44\ \Omega$, a coil of inductive reactance $90\ \Omega$ and another resistance of resistance $36\ \Omega$. The power dissipated in the circuit is



- (a) 320 W (b) 176 W (c) 144 W (d) 0 W
35. A cylindrical vessel of radius r containing a liquid is rotating about a vertical axis through the centre of circular base. If the vessel is rotating with angular velocity ω then what is difference of the height of liquid at the centre of vessel and edge?
- (a) $\frac{r\omega}{2g}$ (b) $\frac{r^2\omega^2}{2g}$ (c) $\sqrt{2gr\omega}$ (d) $\frac{\omega^2}{2gr^2}$
36. Two water pipes of diameters 2 cm and 4 cm are connected with the main supply line. The velocity of flow of water in the pipe of 2 cm diameter is
- (a) 4 times that in the other pipe
(b) $\frac{1}{4}$ times that in the other pipe
(c) 2 times that in the other pipe
(d) $\frac{1}{2}$ times that in the other pipe
37. A coil in the shape of an equilateral triangle of side l is suspended between two pole pieces of a permanent magnet, such that magnetic field, B is in plane of the coil. If due to a current I in the triangle, a torque τ acts on it, the side l of the triangle is

- (a) $2\left(\frac{\tau}{\sqrt{3}Bl}\right)^{\frac{1}{2}}$ (b) $\frac{2}{\sqrt{3}}\left(\frac{\tau}{Bl}\right)$
(c) $2\left(\frac{\tau}{Bl}\right)^{\frac{1}{2}}$ (d) $\frac{1}{\sqrt{3}}\frac{\tau}{Bl}$

38. Two polaroids are crossed. If now one of them is rotated through an angle of 30° and unpolarised light of intensity I_0 is incident on the first polaroid, then the intensity of transmitted light will be

- (a) $\frac{I_0}{4}$ (b) $\frac{3I_0}{4}$ (c) $\frac{3I_0}{8}$ (d) $\frac{I_0}{8}$

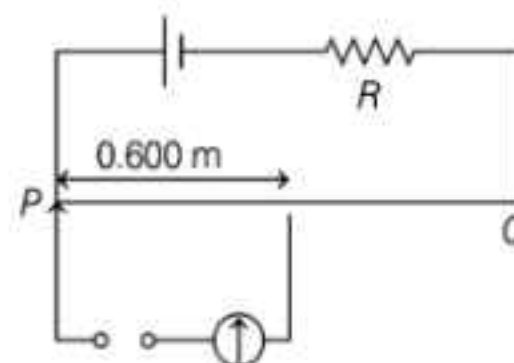
39. If a body coated black at 600 K surrounded by atmosphere at 300 K has cooling rate r_0 , the same body at 900 K, surrounded by the same atmosphere will have cooling rate equal to

- (a) $\frac{16}{3}r_0$ (b) $\frac{8}{16}r_0$ (c) $16r_0$ (d) $4r_0$

40. If force (F), length (L) and time (T) be considered fundamental units, then the units of mass will be

- (a) $[F L T^{-2}]$ (b) $[F L^{-2} T^{-1}]$
(c) $[F L^{-1} T^2]$ (d) $[F^2 L T^{-2}]$

41. Figure shows a simple potentiometer circuit for measuring a small emf produced by a thermocouple



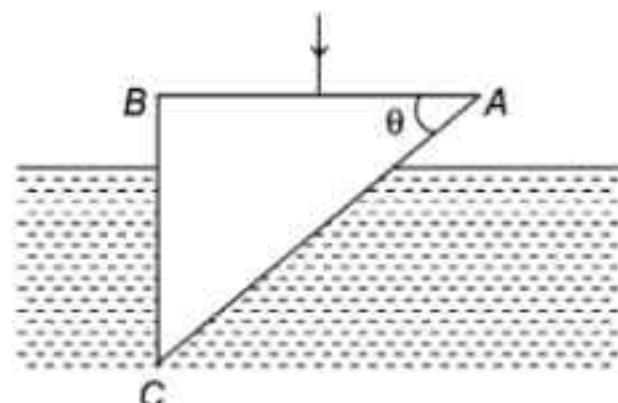
The meter wire PQ has a resistance of $5\ \Omega$ and the driver cell has an emf of 2.00 V. If a balance point is obtained at 0.600 m along PQ , when measuring an emf of 6.00 mV, then what is the value of resistance R ?

- (a) $95\ \Omega$ (b) $995\ \Omega$ (c) $195\ \Omega$ (d) 1995

42. A beam of light ($\lambda = 600\text{ nm}$) from a distant source, falls on a single slit 1 mm wide and the resulting diffraction pattern is observed on a screen 2 m away. The distance between the first dark fringes on either side of the central bright fringe is

- (a) 1.2 cm (b) 1.2 mm
(c) 2.4 cm (d) 2.4 mm

43. A glass prism ABC (refractive index 1.5), immersed in water (refractive index $\frac{4}{3}$). A ray of light is incident normally on face AB . If it is totally reflected at face AC , then



- (a) $\sin \theta \geq \frac{8}{9}$ (b) $\sin \theta \geq \frac{2}{3}$
 (c) $\sin \theta > \frac{\sqrt{3}}{2}$ (d) $\frac{2}{3} < \sin \theta < \frac{8}{9}$

44. An ideal gas is taken through a cyclic thermodynamical process through four steps. The amounts of heat involved in these steps are $Q_1 = 5960 \text{ J}$, $Q_2 = -5585 \text{ J}$, $Q_3 = -2980 \text{ J}$ and $Q_4 = 3645 \text{ J}$, respectively. The corresponding works involved are $W_1 = 2200 \text{ J}$, $W_2 = -825 \text{ J}$, $W_3 = -1100 \text{ J}$ and W_4 , respectively. The value of W_4 is
 (a) 1315 J (b) 275 J (c) 765 J (d) 675 J

45. If the series limit wavelength of the Lyman series of hydrogen atom is 912 \AA , then the series limit wavelength of the Balmer series of the hydrogen atom is

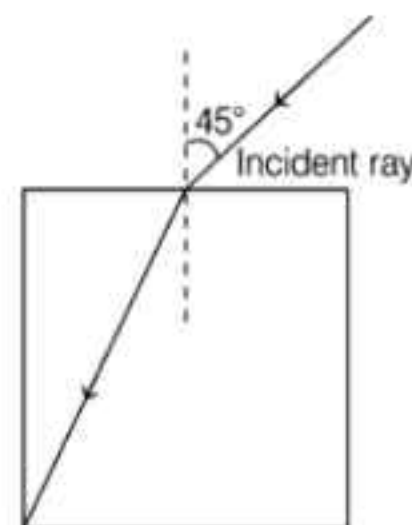
- (a) 912 \AA (b) $912 \times 2 \text{ \AA}$
 (c) $912 \times 4 \text{ \AA}$ (d) $\frac{912}{2} \text{ \AA}$

46. A transformer having efficiency of 90% is working on 200 V and 3 kW power supply. If the current in the secondary coil is 6 A the voltage across the secondary coil and the current in the primary coil respectively are
 (a) 300 V, 15 A (b) 450 V, 15 A
 (c) 450 V, 13.5 A (d) 600 V, 15 A

47. A beam of light consisting of red, green and blue colours, is incident on a right-angled prism. The refractive indices of the material of the prism for the above red, green and blue wavelengths are 1.39, 1.44 and 1.47, respectively. The prism will

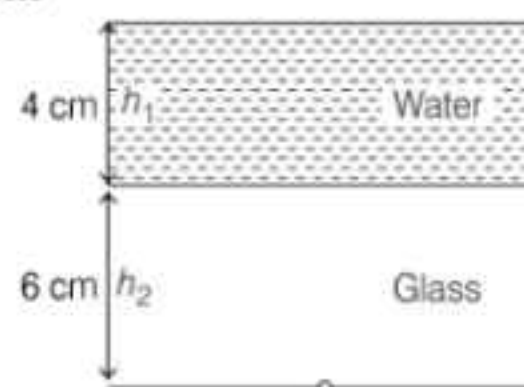
- (a) separated part of the red colour from the green and blue colours
 (b) separate part of the blue colour from the red and green colours
 (c) separate all the three colours from one another
 (d) not separate even partially any colour from the other two colours

48. A light ray falls on a square glass slab as shown in the figure. The index of refraction of the glass, if total internal reflection is occur at vertical face, is equal to



- (a) $\frac{(\sqrt{2} + 1)}{2}$ (b) $\sqrt{\frac{5}{2}}$ (c) $\frac{3}{2}$ (d) $\sqrt{\frac{3}{2}}$

49. A 4 cm thick layer of water covers a 6 cm thick glass slab. A coin is placed at the bottom of the slab and is being observed from the air side along the normal to the surface. Find the apparent position of the coin from



- (a) 7.0 cm (b) 8.0 cm
 (c) 10 cm (d) 5 cm

50. A train of 150 m length is going towards North direction at a speed of 10 ms^{-1} . A parrot flies at a speed of 5 ms^{-1} towards South direction parallel to the railway track. The time taken by the parrot to cross the train is equal to
 (a) 12 s (b) 8 s (c) 15 s (d) 10 s

Chemistry

51. If 1.4 g of $N_2(g)$ react with 1 g of $H_2(g)$ to form ammonia (NH_3), then amount of $NH_3(g)$ formed and number of atoms present in NH_3 respectively are (in moles)

(a) 0.5 and 0.1 (b) 0.1 and 0.1
(c) 0.1 and 0.5 (d) 0.5 and 0.5

52. Which one among the following is not correct as per indicated property?

(a) $Br_2 < Cl_2 < F_2$ (Oxidising power)
(b) $Br_2 < F_2 < Cl_2$ (Electron gain enthalpy)
(c) $Br_2 < Cl_2 < F_2$ (Electronegativity)
(d) $Br_2 < Cl_2 < F_2$ (Bond energy)

53. Which of the following will form 1° alcohol?

(a) $R Mg X + HCHO$ (followed by hydrolysis)
(b) $R Mg X + CH_3COCH_3$ (followed by hydrolysis)
(c) $R X + Mg$ (in the presence of water)
(d) Amine + $CHCl_3 \longrightarrow$ in the presence of KOH

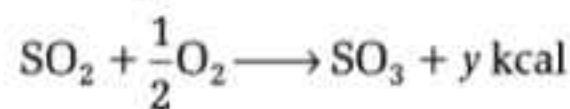
54. For three gases A , B and C , the values of their critical temperatures (T_c) are such that

$$T_c(A) > T_c(B) > T_c(C)$$

assuming identical value of ' b '. Which gas can be most easily liquefied?

(a) A (b) B
(c) C
(d) All at same temperature

55. Given, $S + \frac{3}{2} O_2 \longrightarrow SO_3 + 2x \text{ kcal}$



with the help of above reactions, find out the heat of formation of SO_2 .

(a) $(2x - y)$ (b) $(x + y)$ (c) $(2x + y)$ (d) $(2x / y)$

56. Match the Lists I and II and pick the correct matching from the codes given below.

List I	List II
(i) Peroxy acetyl nitrate	1. Carcinogens
(ii) Polycyclic aromatic hydrocarbons	2. Global warming
(iii) IR active molecules	3. Photochemical smog
(iv) Dioxins	4. Waste incineration

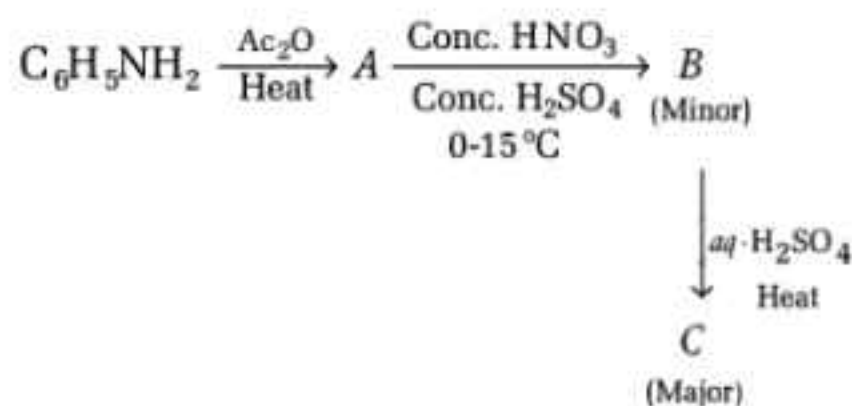
Codes

(a) (i)-3, (ii)-1, (iii)-4, (iv)-2
(b) (i)-3, (ii)-2, (iii)-4, (iv)-1
(c) (i)-3, (ii)-1, (iii)-2, (iv)-4
(d) (i)-4, (ii)-2, (iii)-1, (iv)-3

57. For the gaseous reaction involving complete combustion of isobutane (assuming all products and reactants are in gaseous state), the relation between ΔH and ΔE will be

(a) $\Delta H > \Delta E$ (b) $\Delta H = \Delta E$
(c) $\Delta H < \Delta E$ (d) $\Delta H = 0$ and $\Delta E = \infty$

58. Consider the following sequence of reactions.



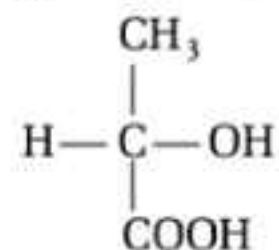
The major product (C) is

(a) 2, 4, 6-trinitroaniline (b) p -nitroacetanilide
(c) p -nitroaniline (d) m -nitroaniline

59. Moist hydrogen cannot be dried over (conc.) H_2SO_4 because

(a) it catches fire
(b) it is reduced by H_2SO_4
(c) it is oxidised by H_2SO_4
(d) it decomposes H_2SO_4

60. Calculate the number of optical isomers in the following compound.

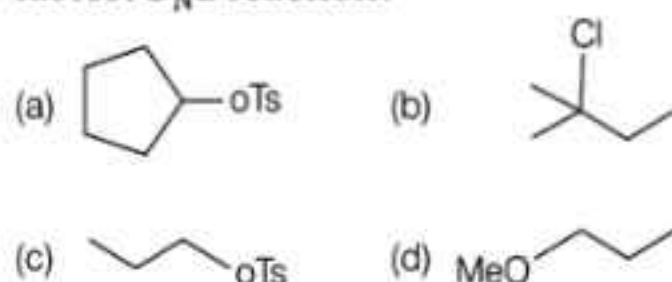


(a) 1
(b) 2
(c) 3
(d) None of these

61. The correct order of increasing covalent character is
 (a) $\text{LiCl} < \text{NaCl} < \text{BeCl}_2$ (b) $\text{BeCl}_2 < \text{NaCl} < \text{LiCl}_2$
 (c) $\text{NaCl} < \text{LiCl} < \text{BeCl}_2$ (d) $\text{BeCl}_2 < \text{LiCl} < \text{NaCl}$

62. H_3BO_3 is a
 (a) monobasic and Lewis acid
 (b) monobasic and Bronsted acid
 (c) tribasic and Lewis acid
 (d) tribasic and Bronsted acid

63. In the following compounds which gives fastest $\text{S}_{\text{N}}2$ reaction?



64. Among the following, achiral amino acid is
 (a) ethylalanine
 (b) methylglycine
 (c) 2-hydroxymethyl serine
 (d) tryptophan

65. Correct sequence of acidic character is
 (a) $\text{N}_2\text{O}_5 > \text{CO}_2 > \text{CO} > \text{SO}_2$
 (b) $\text{N}_2\text{O}_5 > \text{SO}_2 > \text{CO}_2 > \text{CO}$
 (c) $\text{CO} > \text{CO}_2 > \text{SO}_2 > \text{N}_2\text{O}_5$
 (d) $\text{SO}_2 > \text{CO}_2 > \text{CO} > \text{N}_2\text{O}_5$

66. Which reaction represents the oxidising behaviour of H_2SO_4 ?
 (a) $\text{NaCl} + \text{H}_2\text{SO}_4 \longrightarrow \text{NaHSO}_4 + \text{HCl}$
 (b) $2\text{NaOH} + \text{H}_2\text{SO}_4 \longrightarrow \text{Na}_2\text{SO}_4 + 2\text{H}_2\text{O}$
 (c) $2\text{HI} + \text{H}_2\text{SO}_4 \longrightarrow \text{I}_2 + \text{SO}_2 + 2\text{H}_2\text{O}$
 (d) $2\text{PCl}_5 + \text{H}_2\text{SO}_4 \longrightarrow 2\text{POCl}_3 + \text{SO}_2\text{Cl}_2 + 2\text{HCl}$

67. The highest magnetic moment is shown by the transition metal ion with outer electronic configuration
 (a) d^9 (b) d^7
 (c) d^5 (d) d^3

68. Which complex ion has no d -electron in the central metal atom?
 (a) $[\text{MnO}_4]^-$
 (b) $[\text{Co}(\text{NH}_3)_6]^{3+}$
 (c) $[\text{Fe}(\text{CN})_6]^{3-}$
 (d) $[\text{Cr}(\text{H}_2\text{O})_6]^{3+}$

69. Which of the following liquid on electrolysis produce H_2 at cathode and Cl_2 at anode?

- (a) NaCl solution in water
 (b) CuCl_2 solution in water
 (c) Pure water
 (d) H_2SO_4 solution

70. The standard reduction potentials of Cu^{2+}/Cu and $\text{Cu}^{2+}/\text{Cu}^+$ are 0.337 and 0.153 volts respectively. The standard electrode potential for Cu^{2+}/Cu half cell will be

- (a) 0.490 V (b) 0.980 V
 (c) 0.827 V (d) 0.521 V

71. For the reaction,

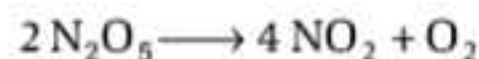


on the basis of the following data, find the order of reaction.

Exp. No.	[A] mol L ⁻¹	[B] mol L ⁻¹	Initial rate (mol L ⁻¹ min ⁻¹)
1.	0.1	0.1	6×10^{-3}
2.	0.3	0.2	7.2×10^{-2}
3.	0.3	0.4	2.88×10^{-1}
4.	0.4	0.1	2.40×10^{-2}

- (a) 1 (b) 2 (c) 3 (d) 4

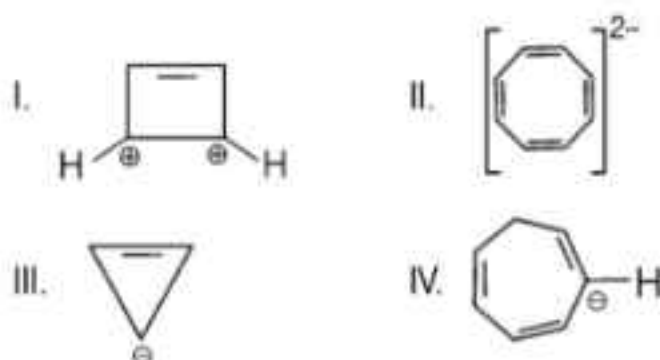
72. For the reaction,



the values of rate constant and rate of reaction are respectively $3 \times 10^{-5}\text{s}^{-1}$ and $2.4 \times 10^{-5}\text{mol L}^{-1}\text{s}^{-1}$. The concentration of N_2O_5 (in mol L⁻¹) will be

- (a) 0.4 (b) 0.8
 (c) 1.2 (d) 0.6

73. In the following compounds



which is the correct pair of aromatic compound?

- (a) I, III and IV (b) I and II
(c) III and IV (d) I and III

74. In which of the following compound, cations occupy alternate tetrahedral voids in cubic closed packing (ccp)?

- (a) ZnS (b) NaCl (c) Na₂O (d) CaF₂

75. Which of the following does not undergo Hell-Volhard-Zelinsky reaction?

- (a) HCOOH (b) CCl₃COOH
(c) C₆H₅COOH (d) All of the above

76. Which of the following transition of an electron in H-atom will emit maximum energy?

- (a) $n_5 \rightarrow n_5$ (b) $n_1 \rightarrow n_2$
(c) $n_3 \rightarrow n_2$ (d) $n_4 \rightarrow n_3$

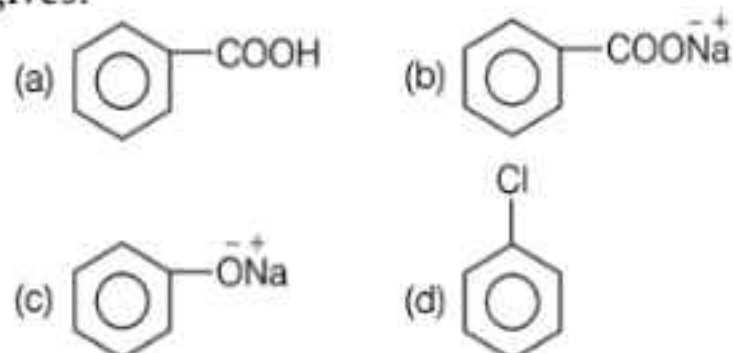
77. The correct set of quantum numbers for an element (Z=17) for the unpaired electron will be

- (a) 3, 1, 1, $\pm 1/2$ (b) 2, 0, 0, $\pm 1/2$
(c) 3, 0, 0, $\pm 1/2$ (d) 2, 1, 1, 0

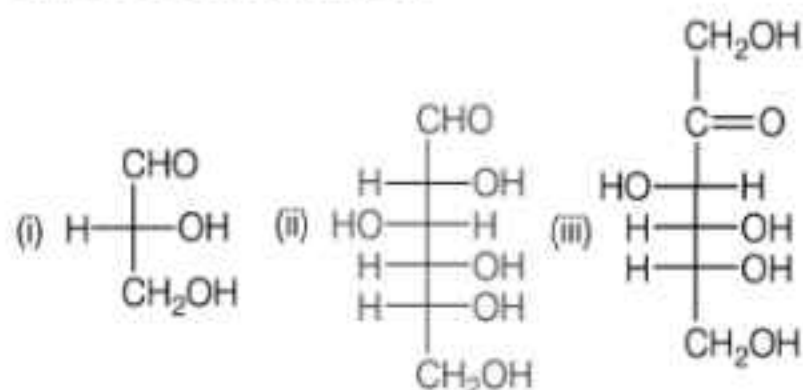
78. Which of the following is an energy releasing process?

- (a) $X(s) \rightarrow X(g)$ (b) $O^-(g) \xrightarrow{e^-} O^{2-}(g)$
(c) $O(g) \rightarrow O^+(g) + e^-$ (d) $O(g) \xrightarrow{e^-} O^-(g)$

79. Toluene reacts with excess of Cl₂ in the presence of sunlight to give a product which on hydrolysis followed by reaction with NaOH gives:



80. Among all the given compounds, which will have D-configuration?



- (a) (i), (ii) and (iii) (b) (ii) and (iii)
(c) (i) and (ii) (d) Only (iii)

81. Volume of an ideal gas is decreased by 5% at constant temperature such that there is an increase in pressure by $x\%$. The increase in pressure (in %) will be:

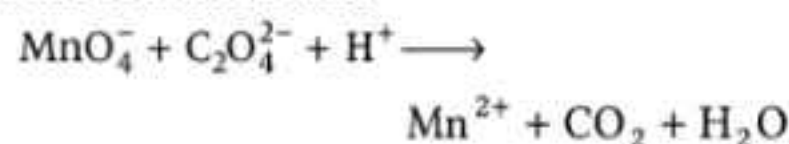
- (a) 5% (b) 4.7%
(c) 5.26% (d) 95%

82. For the following equilibrium

$N_2O_4 \rightleftharpoons 2NO_2$ in gaseous phase, NO₂ is 50% of the total volume, when equilibrium is set up. Hence, percent dissociation of N₂O₄ is:

- (a) 50% (b) 25%
(c) 66.66% (d) 33.33%

83. In the redox reaction



The correct coefficients of C₂O₄²⁻ and H⁺ ions in the balanced equation are

- (a) 5 and 15 (b) 5 and 16
(c) 2 and 16 (d) 2 and 15

84. Substances used in bringing down the body temperature in high fever is called

- (a) antiseptics (b) Pyretics
(c) antibiotics (d) antipyretics

85. The reagent(s) used in the preparation of aspirin from salicylic acid is/are.

- (a) SOCl₂ (b) CH₃COOH, HCl
(c) CHCl₃, AlCl₃ (d) (CH₃CO)₂O, H⁺

86. Terylene is a condensation polymer of ethylene glycol and

- (a) benzoic acid
(b) phthalic acid
(c) salicylic acid
(d) terephthalic acid

87. The correct increasing order of acidic strength of boron trihalides is

- (a) BI₃ < BBr₃ < BCl₃ < BF₃
(b) BF₃ < BCl₃ < BBr₃ < BI₃
(c) BF₃ < BI₃ < BBr₃ < BCl₃
(d) BI₃ < BF₃ < BBr₃ < BCl₃

88. Sulphur(s) when react with HNO_3 (conc.) mainly gives

- (a) H_2SO_4 , NO_2 and H_2O
- (b) H_2S , N_2O_5 and SO_2
- (c) H_2SO_3 , NO_2 and SO_2
- (d) SO_2 , NO_2 and H_2O

89. Which of the following is the correct representation of molecular orbitals?

- (a)
- (b)
- (c)
- (d)

90. On combustion of x -g of ethanol in bomb calorimeter, y -joules of heat energy is produced. The heat of combustion of ethanol (ΔH_{comb}) is

- (a) $\Delta H_{\text{comb}} = -x \cdot y$
- (b) $\Delta H_{\text{comb}} = -yJ$
- (c) $\Delta H_{\text{comb}} = -\frac{x}{y} \times 44 \text{ J mol}^{-1}$
- (d) $\Delta H_{\text{comb}} = -\frac{y}{x} \times 44 \text{ J mol}^{-1}$

91. 0.005 mol of $\text{Ba}(\text{OH})_2$ is dissolved in 100mL of water. Assuming complete ionisation of $\text{Ba}(\text{OH})_2$ the pOH of the solution will be

- (a) 1
- (b) 5
- (c) 2
- (d) 14

92. Which of the following is used as a food preservative?

- (a) Sodium benzoate
- (b) Potassium chloride
- (c) Sodium bicarbonate
- (d) (b) and (c) both

93. Bakelite is obtained by reaction of phenol with

- (a) acetaldehyde
- (b) acetal
- (c) formaldehyde
- (d) chlorobenzene

94. When propyne is treated with $\text{H}_2\text{SO}_4(aq)$ in presence of HgSO_4 , the major product is

- (a) propanal
- (b) n -propyl hydrogen sulphate
- (c) acetone
- (d) propanol

95. The Magnetic moment (spin only) of $[\text{NiCl}_4]^{2-}$ is

- (a) 1.82 BM
- (b) 5.46 BM
- (c) 2.82 BM
- (d) 1.41 BM

96. In aqueous solution $\text{Cu}(+1)$ salts are unstable because

- (a) $\text{Cu}(+1)$ has $3d^{10}$ configuration.
- (b) They disproportionate easily to Cu and Cu^{2+} states.
- (c) They disproportionate easily to Cu^{2+} and Cu^{3+} states
- (d) Its change in free energy is zero

97. The atomic number of elements A , B , C and D are $Z-1$, Z , $Z+1$, $Z+2$ respectively. If B is a noble gas, choose the correct option

- (1) A has higher electron affinity.
- (2) C exists in +2 oxidation state.
- (3) D is an alkaline earth metal.
- (a) (1) and (2)
- (b) (2) and (3)
- (c) (1) and (3)
- (d) (1), (2) and (3)

98. Select the incorrect statement

- (a) Physical adsorption is reversible, while chemical is irreversible.
- (b) High pressure favours physical adsorption while low pressure favours chemical adsorption.
- (c) Physical adsorption is not specific, while chemical adsorption is highly specific.
- (d) High activation energy is required in chemical adsorption.

99. The chemical reaction $2\text{O}_3 \longrightarrow 3\text{O}_2$,

proceeds as follows $\text{O}_3 \rightleftharpoons \text{O}_2 + \text{O}$ (fast)

$\text{O} + \text{O}_3 \longrightarrow 2\text{O}_2$ (slow)

the rate law for the above reaction can be

- (a) $r = k'[\text{O}_3]^2$
- (b) $r = k'[\text{O}_3]^2 [\text{O}_2]^{-1}$
- (c) $r = k' [\text{O}_3] [\text{O}_2]$
- (d) $r = k'[\text{O}_2] [\text{O}]$

100. Ionic product of water at 310 K is 2.7×10^{-14} .

What is the pH of neutral water at this temperature?

- (a) 7.00
- (b) 5.98
- (c) 6.78
- (d) 4.58

Mathematics

- 101.** If α, β, γ are the angles which a directed line makes with the positive directions of the coordinate axes, then $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma$ is equal to
 (a) 1 (b) 4 (c) 3 (d) 2
- 102.** If \mathbf{a} and \mathbf{b} are two non-collinear vectors such that $|\mathbf{a}| = 3, |\mathbf{b}| = 4$ and $\mathbf{a} - \mathbf{b} = \hat{\mathbf{i}} + 2\hat{\mathbf{j}} + 3\hat{\mathbf{k}}$, then the value of $\left\{ \frac{\mathbf{a}}{|\mathbf{a}|} - \frac{\mathbf{b}}{|\mathbf{b}|} \right\}^2$ is equal to
 (a) $\frac{1}{24}$ (b) $\frac{5}{72}$ (c) $\frac{7}{72}$ (d) $\frac{7}{48}$
- 103.** The acute angle between the lines whose direction ratios are given by $l + m - n = 0$ and $l^2 + m^2 - n^2 = 0$, is
 (a) 0 (b) $\pi/6$ (c) $\pi/4$ (d) $\pi/3$
- 104.** The number of 6-digit numbers that can be made with the digits 1, 2, 3 and 4 and having exactly two pairs of digits, is
 (a) 480 (b) 540 (c) 1080 (d) 2040
- 105.** Area of the region bounded by the curves $y = 2^x, y = 2x - x^2, x = 0$ and $x = 2$ is given by
 (a) $\frac{3}{\log 2} - \frac{4}{3}$ (b) $\frac{3}{\log 2} + \frac{4}{3}$
 (c) $3 \log 2 - \frac{4}{3}$ (d) $3 \log 2 + \frac{4}{3}$
- 106.** The lengths of tangent, subtangent, normal and subnormal for the curve $y = x^2 + x - 1$ at $(1, 1)$ are A, B, C and D respectively, then their increasing order is
 (a) B, D, A, C (b) B, A, C, D
 (c) A, B, C, D (d) B, A, D, C
- 107.** Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be defined by

$$f(x) = \begin{cases} k - 2x, & \text{if } x \leq -1 \\ 2x + 3, & \text{if } x > -1 \end{cases}$$
 If f has a local minimum at $x = -1$, then a possible value of k is
 (a) $-1/2$ (b) -1 (c) 1 (d) 0
- 108.** If a point $P(a, b, c)$ perpendiculars PA, PB are drawn to YZ and ZX planes, then the equation of the plane OAB is
 (a) $bcx + cay + abz = 0$ (b) $bcx + cay - abz = 0$
 (c) $bcx - cay + abz = 0$ (d) $-bcx + cay + abz = 0$
- 109.** A circular ring of radius 3 cm is suspended horizontally from a point 4 cm vertically above the centre by 4 strings attached at equal intervals to its circumference. If the angle between two consecutive strings be θ , then $\cos \theta$ is equal to
 (a) $\frac{4}{5}$ (b) $\frac{4}{25}$
 (c) $\frac{16}{25}$ (d) None of these
- 110.** The value of $\sin^{-1} \left[\cot \left(\sin^{-1} \sqrt{\frac{2-\sqrt{3}}{4}} \right) + \cos^{-1} \frac{\sqrt{12}}{4} + \sec^{-1} \sqrt{2} \right]$ is
 (a) 0 (b) $\frac{\pi}{2}$
 (c) $\frac{\pi}{3}$ (d) None of these
- 111.** 900 distinct n -digit positive numbers are to be formed using only the digits 2, 5 and 7. The smallest value of x for which this is possible, is
 (a) 9 (b) 8 (c) 7 (d) 6
- 112.** If the non-zero numbers x, y, z are in AP and $\tan^{-1} x, \tan^{-1} y, \tan^{-1} z$ are also in AP, then
 (a) $xy = yz$ (b) $z^2 = xy$
 (c) $x = y = z$ (d) $x^2 = yz$
- 113.** If n is odd, then the sum of n terms of the series $1^2 - 2^2 + 3^2 - 4^2 + 5^2 - 6^2 + \dots$ is
 (a) $\frac{n(n-1)}{2}$ (b) $\frac{n(n+1)}{2}$
 (c) $\frac{-n(n-1)}{2}$ (d) $\frac{-n(n+1)}{2}$
- 114.** A rectangle $ABCD$, where $A \equiv (0, 0)$
 $B \equiv (4, 0), C \equiv (4, 2), D \equiv (0, 2)$, undergoes the following transformation successively

- (i) $f_1(x, y) \rightarrow (y, x)$
 (ii) $f_2(x, y) \rightarrow (x + 3y, y)$
 (iii) $f_3(x, y) \rightarrow (x - y) / 2, (x + y) / 2$

The final figure will be

- (a) a square (b) a parallelogram
 (c) a rhombus (d) a rectangle

115. The order and degree of the differential

equation $P = \frac{\left(1 + \left(\frac{dy}{dx}\right)^2\right)^{3/2}}{\frac{d^2y}{dx^2}}$ are respectively

- (a) 2, 2 (b) 2, 3
 (c) 2, 1 (d) None of these

116. If $f(\theta) = 5 \cos \theta + 3 \cos \left(\theta + \frac{\pi}{3}\right) + 3$, then

range of $f(\theta)$ is

- (a) $[-5, 11]$ (b) $[-3, 9]$ (c) $[-2, 10]$ (d) $[-4, 10]$

117. The coordinates of the foot of the perpendicular drawn from the point $A(1, 0, 3)$ to the join of the points $B(4, 7, 1)$ and $C(3, 5, 3)$ are

- (a) $(5, 7, 17)$ (b) $\left(\frac{-5}{7}, \frac{7}{3}, \frac{-17}{3}\right)$
 (c) $\left(\frac{5}{7}, \frac{-7}{3}, \frac{17}{3}\right)$ (d) $\left(\frac{5}{3}, \frac{7}{3}, \frac{17}{3}\right)$

118. If $x = \cos \theta$, $y = \sin 5\theta$, then

$$(1 - x^2) \frac{d^2y}{dx^2} - x \frac{dy}{dx} =$$

- (a) $-5y$ (b) $5y$ (c) $25y$ (d) $-25y$

119. If the period of the function

$$f(x) = \frac{\sin(\sin(nx))}{\tan\left(\frac{x}{n}\right)}, n \in N, \text{ is } 6\pi, \text{ then } n \text{ is}$$

equal to

- (a) 3 (b) 2
 (c) 1 (d) None of these

120. The set of points where the function $f(x) = [x] + |1 - x|$, $-1 \leq x \leq 3$, where $[.]$ denotes the greatest integer function, is not differentiable, is

- (a) $\{-1, 0, 1, 2, 3\}$ (b) $\{-1, 0, 2\}$
 (c) $\{0, 1, 2, 3\}$ (d) $\{-1, 0, 1, 2\}$

121. If $I_n = \int_0^{\pi/2} \frac{\cos^2 n x}{\sin x} dx$, then $I_2 - I_1, I_3 - I_2,$

$I_4 - I_3$ are in

- (a) GP (b) AP
 (c) HP (d) None of these

122. If the coefficient of the 5th term is the numerically the greatest coefficient in the expansion of $(1 - x)^n$, then the positive integral value of n is

- (a) 10 (b) 9 (c) 8 (d) 7

123. $\sim(p \Leftrightarrow \sim q)$ is equivalent to

- (a) $p \Leftrightarrow \sim q$ (b) $p \Rightarrow q$
 (c) $p \Leftrightarrow q$ (d) None of these

124. If the tangent at the point $P(2, 4)$ to the parabola $y^2 = 8x$ meets the parabola $y^2 = 8x + 5$ at Q and R , then the mid-point of QR is

- (a) $(4, 2)$ (b) $(2, 4)$
 (c) $(7, 9)$ (d) $(9, 7)$

125. The locus of the centres of the circles passing through the intersection of the circles $x^2 + y^2 = 1$ and $x^2 + y^2 - 2x + y = 0$, is

- (a) $2x - y = 1$ (b) $x + 2y = 0$
 (c) a circle (d) a pair of lines

126. The value of $\lim_{x \rightarrow 0} \frac{\int_0^{x^2} \sec^2 t dt}{x \sin x}$ is

- (a) 0 (b) 3 (c) 2 (d) 1

127. The number of real roots of

$$(6 - x)^4 + (8 - x)^4 = 16 \text{ is}$$

- (a) 0 (b) 2 (c) 4 (d) 6

128. $10^{2n-1} + 1$ for all $n \in N$ is divisible by

- (a) 2 (b) 3 (c) 7 (d) 11

129. If $f(x) = \begin{cases} \frac{1 - \sqrt{2} \sin x}{\pi - 4x}, & x \neq \pi/4 \\ a, & x = \pi/4 \end{cases}$ is continuous

at $x = \frac{\pi}{4}$, then $a =$

- (a) 4 (b) 2
 (c) 1 (d) $1/4$

130. If $f(x) = a \log|x| + bx^2 + x$ has its extremum values at $x = -1$ and $x = 2$, then

- (a) $a=2, b=-1$ (b) $a=2, b=-1/2$
(c) $a=-2, b=\frac{1}{2}$ (d) None of these

131. Let $P = \{\theta : \sin\theta - \cos\theta = \sqrt{2}\cos\theta\}$ and, $Q = \{\theta : \sin\theta + \cos\theta = \sqrt{2}\sin\theta\}$ be two sets. Then,

- (a) $P \subset Q$ and $Q - P \neq \emptyset$ (b) $Q \subset P$
(c) $P \not\subset Q$ (d) $P = Q$

132. Let the straight line $x = b$ divide the area enclosed by $y = (1-x)^2$, $y = 0$ and $x = 0$ into two parts R_1 ($0 \leq x \leq b$) and R_2 ($b \leq x \leq 1$) such that $R_1 - R_2 = \frac{1}{4}$. Then b equals.

- (a) $\frac{3}{4}$ (b) $\frac{1}{2}$ (c) $\frac{1}{3}$ (d) $\frac{1}{4}$

133. $\int_{-1}^{10} \text{sgn}(x - [-x]) dx$ equal to

- (a) 10 (b) 11 (c) 9 (d) $\frac{11}{2}$

134. The solution set of the equation $\cos^{-1} x - \sin^{-1} x = \sin^{-1}(1-x)$, is

- (a) $\{-1, 1\}$ (b) $\{0, 1/2\}$
(c) $\{-1, 0\}$ (d) None of these

135. Let $\mathbf{a} = \mathbf{i} + \mathbf{j} + \mathbf{k}$, $\mathbf{c} = \mathbf{j} - \mathbf{k}$. If \mathbf{b} is a vector satisfying $\mathbf{a} \times \mathbf{b} = \mathbf{c}$ and $\mathbf{a} \cdot \mathbf{b} = 3$, then \mathbf{b} is

- (a) $\frac{1}{3}(5\mathbf{i} + 2\mathbf{j} + 2\mathbf{k})$ (b) $\frac{1}{3}(5\mathbf{i} - 2\mathbf{j} - 2\mathbf{k})$
(c) $3\mathbf{i} - \mathbf{j} - \mathbf{k}$ (d) None of these

136. Let T_n denote the number of triangles which can be formed using the vertices of a regular polygon of n sides. If $T_{n+1} - T_n = 21$, then n equals

- (a) 5 (b) 7 (c) 6 (d) 4

137. The length of the shadows of a vertical pole of height h , thrown by the sun's rays at three different moments are h , $2h$ and $3h$. The sum of the angles of elevation of the rays at these three moments is equal to

- (a) $\frac{\pi}{2}$ (b) $\frac{\pi}{3}$ (c) $\frac{\pi}{4}$ (d) $\frac{\pi}{6}$

138. If the arithmetic mean of the following data is 7, then $a + b =$

x_i	4	6	7	9
f_i	a	4	b	5

- (a) 4 (b) 2
(c) 3 (d) cannot be determined

139. A straight line through the origin meets the parallel lines $4x + 2y = 9$ and $2x + y + 6 = 0$ at point P and Q respectively. Then, the point O divides the segment PQ in the ratio

- (a) 1:2 (b) 3:4 (c) 2:1 (d) 4:3

140. The eccentricity of the ellipse, if the distance between the foci is equal to the length of the latusrectum, is

- (a) $\frac{\sqrt{5}-1}{2}$ (b) $\frac{\sqrt{5}+1}{4}$ (c) $\frac{\sqrt{5}-1}{4}$ (d) $\frac{\sqrt{5}+1}{2}$

141. Gas is being pumped into a spherical balloon at the rate of $30 \text{ ft}^3 / \text{min}$. Then, the rate at which the radius increases when it reaches the value 15ft, is

- (a) $\frac{1}{30\pi} \text{ ft/min}$ (b) $\frac{1}{15\pi} \text{ ft/min}$
(c) $\frac{1}{20} \text{ ft/min}$ (d) $\frac{1}{25} \text{ ft/min}$

142. In a ΔABC , medians AD and BE are drawn. If $AD = 4$, $\angle DAB = \pi/6$ and $\angle ABE = \pi/3$, then the area of ΔABC is

- (a) $\frac{64}{3\sqrt{3}}$ (b) $\frac{8}{3\sqrt{3}}$ (c) $\frac{16}{3\sqrt{3}}$ (d) $\frac{32}{3\sqrt{3}}$

143. The sum of the series.

$$1 + \frac{1}{3^2} + \frac{1}{1^2} \cdot \frac{4}{2} \cdot \frac{1}{3^4} + \frac{1}{1^2} \cdot \frac{4}{2} \cdot \frac{7}{2} \cdot \frac{1}{3^6} + \dots \text{ is}$$

- (a) $\sqrt{\frac{3}{2}}$ (b) $\left(\frac{3}{2}\right)^{1/3}$ (c) $\sqrt{\frac{1}{3}}$ (d) $\left(\frac{1}{3}\right)^{1/3}$

144. If $f(1) = 3$, $f'(1) = -\frac{1}{3}$, then the derivative of

$$\{x^{11} + f(x)\}^{-2} \text{ at } x = 1, \text{ is}$$

- (a) $-\frac{1}{2}$ (b) -1 (c) 1 (d) $f'(1)$

145. Let $R = \{(1,3), (4,2), (2,4), (2,3), (3,1)\}$ be a relation on the set $A = \{1,2,3,4\}$. The relation R is

- (a) reflexive (b) transitive
(c) not symmetric (d) a function

146. If $[\cdot]$ denotes the greatest integer function, then

$$f(x) = [x] + \left[x + \frac{1}{2} \right]$$

- (a) is continuous at $x = \frac{1}{2}$
 (b) is discontinuous at $x = \frac{1}{2}$
 (c) $\lim_{x \rightarrow \frac{1}{2}^+} f(x) = 2$
 (d) $\lim_{x \rightarrow \frac{1}{2}^-} f(x) = 1$

147. $\lim_{x \rightarrow \infty} \frac{\cot^{-1}(\sqrt{x+1} - \sqrt{x})}{\sec^{-1}\left\{\left(\frac{2x+1}{x-1}\right)^x\right\}}$ is equal to

- (a) 1
 (c) $\frac{\pi}{2}$
 (b) 0
 (d) Non-existent

148. If $y = \cos^{-1}(\cos x)$, then $\frac{dy}{dx}$ at $x = \frac{5\pi}{4}$, is

- (a) 1
 (c) $\frac{1}{\sqrt{2}}$
 (b) -1
 (d) None of these

149. The median of 100 observations grouped in classes of equal width is 25. If the median class interval is 20 – 30 and the number of observations less than 20 is 45, then the frequency of median class is

- (a) 20
 (c) 10
 (b) 12
 (d) 15

150. Every term of G.P. is positive and also every term is the sum of two preceding terms. Then, the common ratio of the G.P. is

- (a) $\frac{1-\sqrt{5}}{2}$
 (c) $\frac{\sqrt{5}-1}{2}$
 (b) $\frac{\sqrt{5}+1}{2}$
 (d) 1

Answers

Physics

1.	(d)	2.	(a)	3.	(b)	4.	(a)	5.	(c)	6.	(b)	7.	(c)	8.	(d)	9.	(c)	10.	(d)
11.	(b)	12.	(b)	13.	(d)	14.	(d)	15.	(b)	16.	(b)	17.	(c)	18.	(c)	19.	(b)	20.	(c)
21.	(a)	22.	(b)	23.	(b)	24.	(c)	25.	(b)	26.	(c)	27.	(a)	28.	(b)	29.	(c)	30.	(c)
31.	(b)	32.	(b)	33.	(b)	34.	(a)	35.	(b)	36.	(a)	37.	(a)	38.	(d)	39.	(a)	40.	(c)
41.	(b)	42.	(d)	43.	(a)	44.	(c)	45.	(c)	46.	(b)	47.	(a)	48.	(d)	49.	(a)	50.	(d)

Chemistry

51.	(b)	52.	(d)	53.	(a)	54.	(a)	55.	(a)	56.	(c)	57.	(a)	58.	(c)	59.	(c)	60.	(b)
61.	(c)	62.	(a)	63.	(c)	64.	(c)	65.	(b)	66.	(c)	67.	(c)	68.	(a)	69.	(a)	70.	(d)
71.	(c)	72.	(b)	73.	(b)	74.	(a)	75.	(d)	76.	(c)	77.	(a)	78.	(d)	79.	(b)	80.	(a)
81.	(c)	82.	(d)	83.	(b)	84.	(d)	85.	(d)	86.	(d)	87.	(b)	88.	(a)	89.	(b)	90.	(d)
91.	(a)	92.	(a)	93.	(c)	94.	(c)	95.	(c)	96.	(b)	97.	(c)	98.	(b)	99.	(b)	100.	(c)

Mathematics

101.	(d)	102.	(c)	103.	(d)	104.	(c)	105.	(a)	106.	(d)	107.	(b)	108.	(d)	109.	(c)	110.	(a)
111.	(c)	112.	(c)	113.	(b)	114.	(b)	115.	(a)	116.	(d)	117.	(d)	118.	(d)	119.	(a)	120.	(c)
121.	(c)	122.	(c)	123.	(c)	124.	(b)	125.	(b)	126.	(d)	127.	(d)	128.	(d)	129.	(d)	130.	(b)
131.	(d)	132.	(b)	133.	(b)	134.	(b)	135.	(a)	136.	(b)	137.	(a)	138.	(d)	139.	(b)	140.	(a)
141.	(a)	142.	(d)	143.	(b)	144.	(d)	145.	(c)	146.	(b)	147.	(a)	148.	(b)	149.	(c)	150.	(b)

Answer with Solutions

Physics

1. (d) We know that, $f = \frac{1}{2\pi\sqrt{LC}}$

$\therefore \frac{C}{L}$ does not represent the dimensions of frequency.

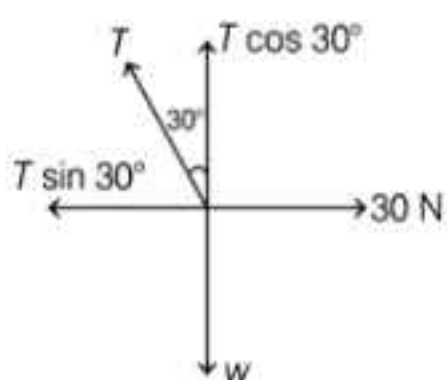
2. (a) If coefficient of volume expansion is α and rise in temperature is $\Delta\theta$, then $\Delta V = V \alpha \Delta\theta$

$$\Rightarrow \frac{\Delta V}{V} = \alpha \Delta\theta$$

$$\therefore \text{Volume elasticity, } \beta = \frac{p}{\Delta V/V} = \frac{p}{\alpha \Delta\theta}$$

$$\Rightarrow \Delta\theta = \frac{p}{\alpha \beta}$$

3. (b) Horizontal and vertical components of tension are shown in the figure.



$$\text{From the figure, } T \sin 30^\circ = 30 \quad \dots (i)$$

$$T \cos 30^\circ = w \quad \dots (ii)$$

By solving Eqs. (i) and (ii), we get

$$w = 30\sqrt{3} \text{ N and } T = 60 \text{ N}$$

4. (a) Given, $v = 10 \text{ m/s}$ $\mu = 0.5$

We know that $v_{\max} = \sqrt{\mu g R}$

On squaring both sides, we get

$$\begin{aligned} R &= \frac{v^2}{\mu g} \\ &= \frac{100}{0.5 \times 10} = 20 \end{aligned}$$

5. (c) When a spring is in equilibrium, its extension $= \frac{mg}{k}$

At the highest point of block, spring is in its natural length.

$$\text{Hence, amplitude, } A = \frac{mg}{k}$$

Given, $f = 10 \text{ Hz}$

$$\omega = 2\pi f = 20\pi \text{ rad/s}$$

$$\therefore \omega = \sqrt{\frac{k}{m}}$$

On squaring both sides, we get

$$\frac{k}{m} = \omega^2$$

$$\Rightarrow v_{\max} = A\omega$$

$$= \frac{m}{k} g \omega = \frac{g \omega}{\omega^2}$$

$$= \frac{g}{\omega} = \frac{\pi^2}{20\pi} = \frac{\pi}{20} \text{ m/s}$$

$$\therefore A = \frac{mg}{k} = \frac{g}{\omega^2}$$

$$= \frac{\pi^2}{400 \pi^2} = \frac{0.25}{100} \text{ m} = 0.25 \text{ cm}$$

Now, when extension is 0.20 cm, then displacement from equilibrium position

$$= 0.25 - 0.20 = 0.05 \text{ cm}$$

$$x = 0.05 \text{ cm}$$

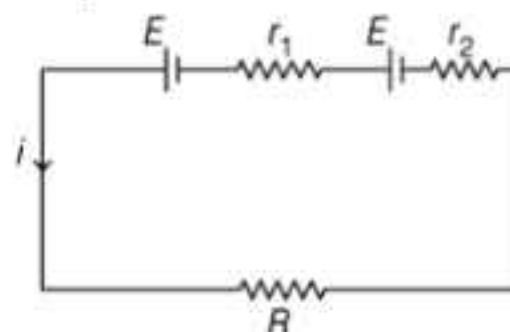
$$\therefore v = \omega \sqrt{A^2 - x^2}$$

$$= 20\pi \sqrt{(0.25)^2 - (0.05)^2}$$

$$= 2\pi\sqrt{6} \text{ cm/s}$$

$$= 15.4 \text{ cm/s}$$

6. (b) The required circuit is shown below.



$$i = \frac{2E}{R + r_1 + r_2}$$

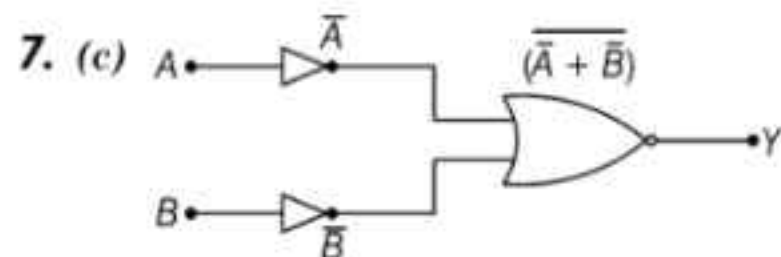
Potential difference across first cell,

$$V_1 = E - ir_1$$

$$0 = E - \frac{2E}{R + r_1 + r_2} \cdot r_1$$

$$R + r_1 + r_2 = 2r_1$$

$$R = r_1 - r_2$$

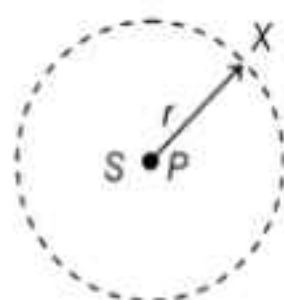


Truth table

A	B	\bar{A}	\bar{B}	$\bar{A} + \bar{B}$	$\overline{(\bar{A} + \bar{B})}$
0	0	1	1	1	0
0	1	1	0	1	0
1	0	0	1	1	0
1	1	0	0	0	1

(i.e., AND Gate)

8. (d) Let r be the distance between the points S and X .



Intensity at distance r from a point source,

$$I = \frac{P}{4\pi r^2}$$

$$\therefore \text{Efficiency, } \eta = \frac{\text{Output}}{\text{Input}} = \frac{P}{P'}$$

$$P = \eta P'$$

$$= \left(\frac{10}{100}\right)(30\pi) = 3\pi \text{ W}$$

$$I = \frac{P}{4\pi r^2} = \frac{3\pi}{4\pi(3)^2}$$

$$= \frac{1}{12} \frac{\text{W}}{\text{m}^2} = \frac{1}{2} \epsilon_0 E_0^2 c$$

$$\frac{1}{12} = \frac{1}{2} \epsilon_0 E_0^2 \times 3 \times 10^8$$

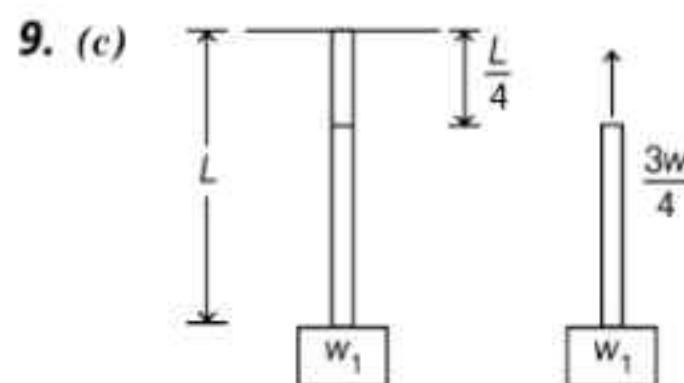
$$E_0^2 = \frac{10^{-8}}{18\epsilon_0} = \frac{10^{-8}}{18 \times 8.85 \times 10^{-12}}$$

$$= \frac{10^4}{18 \times 8.85}$$

$$\Rightarrow E_0 = \frac{10^2}{\sqrt{18 \times 8.85}} = 7.92 \text{ V/m}$$

$$\therefore B_0 = \frac{E_0}{c} = \frac{292}{3 \times 10^8}$$

$$= 2.64 \times 10^{-6} \text{ T}$$



$$T = w_1 + \frac{3w}{4}$$

$$\therefore \sigma = \frac{T}{A} = \frac{w_1 + (3w/4)}{S}$$

10. (d) Possible frequencies of B : $100 \pm 2 = 102 \text{ Hz}$ or 98 Hz . Frequency of A : 100 Hz .

When wax is used on B , $f_B \downarrow$ beat frequency decreases, this is possible at $f_B = 102 \text{ Hz}$.

11. (b) Given, $C' = 0.014 \mu\text{F/km}$

$$f = 50 \times 10^3 \text{ Hz}$$

Total capacitance,

$$C = C' \times 200 = 0.014 \mu\text{F} \times 200 = 28 \mu\text{F}$$

For impedance to be minimum

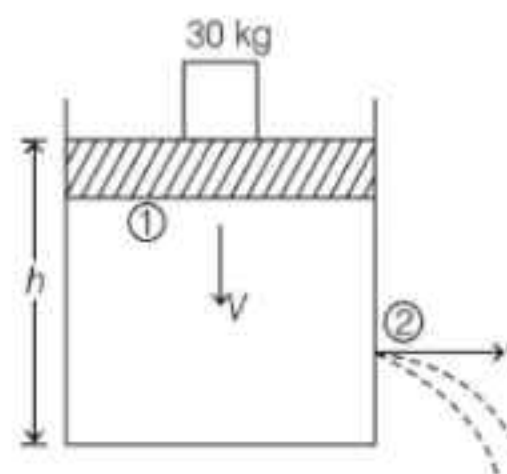
$$X_L = X_C, \text{ i.e. } \omega L = \frac{1}{\omega C}$$

$$L = \frac{1}{\omega^2 C} = \frac{1}{4\pi^2 f^2 C}$$

$$= \frac{1}{4\pi^2 \times (50 \times 10^3)^2 \times 28 \times 10^{-6}}$$

$$= 0.36 \times 10^{-3} \text{ H} = 0.36 \times 10^{-2} \text{ mH}$$

12. (b) Let the velocity of efflux at point 2 is v .



$$\text{Given, } a = 1 \text{ cm}^2, A = 0.5 \text{ m}^2 = 0.5 \times 10^4 \text{ cm}^2$$

Applying continuity equation,

$$AV = av$$

$$V = \frac{a}{A} v$$

Since, $a \ll A$, $V \ll v$, V^2 is negligible.

Pressure at 1,
$$p_1 = p_0 + \frac{mg}{A}$$
$$= p_0 + \frac{30 \times 10}{0.5} = p_0 + 600$$

Pressure at (2),

$$p_2 = p_0$$

where, p_0 is atmospheric pressure.

Applying Bernoulli's equation between (1) and (2),

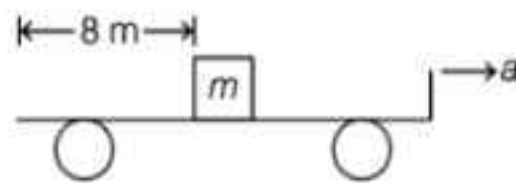
$$p_1 + \rho gh + \frac{1}{2}\rho V^2 = p_2 + \frac{1}{2}\rho v^2$$

V^2 is negligible, then

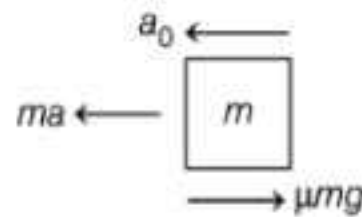
$$p_0 + 600 + 1200 \times 10 \times 0.75$$
$$= p_0 + \frac{1}{2} \times 1200 v^2$$

$$600 v^2 = 9600 \Rightarrow v^2 = 16 \Rightarrow v = 4 \text{ m/s}$$

13. (d) Let a be the acceleration of truck.



For block,



$$ma - \mu mg = ma_0$$

$$a_0 = a - \mu g = 2 - 0.1 \times 10 = 1 \text{ m/s}^2$$

$$8 = \frac{1}{2} a_0 t^2 = \frac{1}{2} \times 1 \times t^2$$

$$\Rightarrow t = 4 \text{ s}$$

The block will fall off the truck after 4 s.

For truck,

Distance travelled by the truck in this time.

$$s = \frac{1}{2} at^2 = \frac{1}{2} \times 2 \times 4^2 = 16 \text{ m}$$

14. (d) Given, $a_1 = 2a_2$

$$I_1 = 4I', I_2 = I'$$

We know that, $I_m = (\sqrt{I_1} + \sqrt{I_2})^2$

$$= (\sqrt{4I'} + \sqrt{I'})^2 = 9I'$$

$$\therefore I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$$

$$= 4I' + I' + 2\sqrt{4I' \cdot I'} \cos \phi$$

$$= 4I' + I' + 4I' \cos \phi$$

$$= 5I' + 4I' \cos \phi$$

$$= I'(5 + 4 \cos \phi)$$

$$= \frac{I_m}{9} \left[5 + 4(2 \cos^2 \frac{\phi}{2} - 1) \right]$$

$$= \frac{I_m}{9} \left[5 + 8 \cos^2 \frac{\phi}{2} - 4 \right]$$

$$= \frac{I_m}{9} \left[1 + 8 \cos^2 \frac{\phi}{2} \right]$$

15. (b) $T = 2\pi \sqrt{\frac{I}{MB}} = 2$

Moment of inertia of each part = $\frac{I}{27}$ and

magnetic moment = $\frac{M}{3}$

New moment of inertia, $I' = 3 \times \frac{I}{27} = \frac{I}{9}$

New magnetic moment, $M' = 3 \times \frac{M}{3} = M$

$$\therefore T' = 2\pi \sqrt{\frac{I/9}{MB}} = \frac{2}{3} \text{ s}$$

16. (b) According to question, $\frac{(V_{rms})_{O_2}}{(V_{rms})_{H_2}}$

$$= \sqrt{\frac{(M_0)_{H_2}}{(M_0)_{O_2}}} = \sqrt{\frac{2}{32}} = \frac{1}{4}$$

17. (c) $n_1 = k\sqrt{T}$, $n_2 = k\sqrt{1.01T}$

$$\therefore n_2 - n_1 = \frac{3}{2}$$

$$k(\sqrt{1.01T} - \sqrt{T}) = 1.5$$

$$k\sqrt{T} [(1 + 0.01)^{1/2} - 1] = 1.5$$

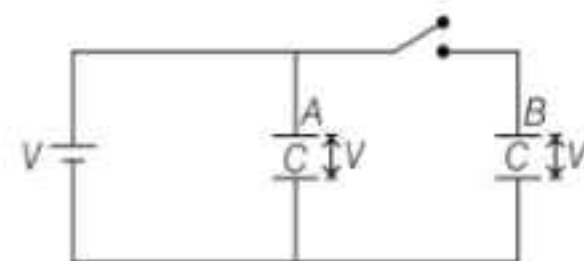
$$k\sqrt{T} [1 + \frac{1}{2} \times 0.01 - 1] = 1.5$$

$$k\sqrt{T} = \frac{1.5 \times 2}{0.01}$$

$$\therefore n_1 = k\sqrt{T} = \frac{1.5 \times 2}{0.01} = 300 \text{ Hz}$$

We know that beat frequency is the difference of two frequencies, i.e. $f_1 - f_2$.

18. (c) When switch (S) is closed,



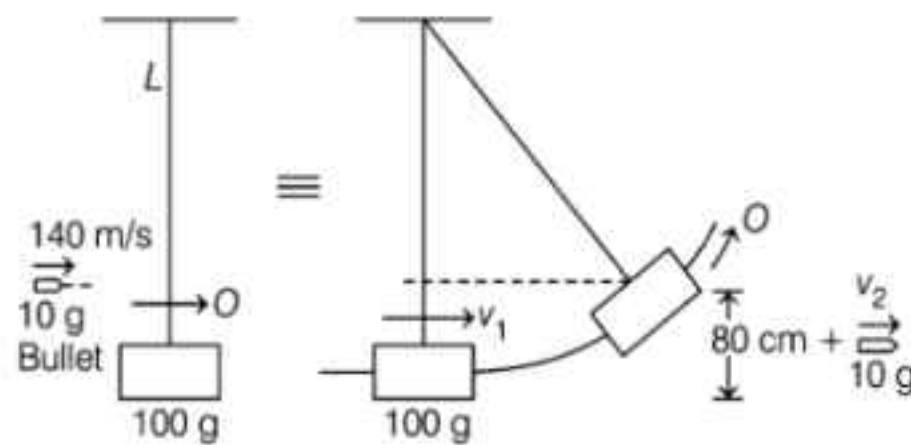
$$U_i = \frac{1}{2} CV^2 + \frac{1}{2} CV^2 = CV^2$$

Charge on B, $Q = CV$

When switch (S) is open and dielectric ($K = 2$) is inserted in both capacitors, potential of A remains same while charge on B remains same.

$$\begin{aligned} U_f &= \frac{1}{2} \cdot 2C \cdot V^2 + \frac{Q^2}{2 \cdot 2C} \\ &= CV^2 + \frac{C^2 V^2}{4C} \\ &= \frac{5}{4} CV^2 \\ \frac{U_i}{U_f} &= \frac{4}{5} \end{aligned}$$

19. (b)



Let the speed of the bullet be v_1 . Let the common velocity of the bullet and the block, after the bullet is attached like a simple pendulum is v_2 .

By the principle of conservation of linear momentum

$$\begin{aligned} \frac{10}{1000} \times 140 + \frac{100}{1000} \times 0 &= \frac{100}{1000} v_1 + \frac{10}{1000} v_2 \\ 140 &= 10v_1 + v_2 \quad \dots (i) \end{aligned}$$

For the block, $0 = v_1^2 - 2g \left(\frac{80}{100} \right)$

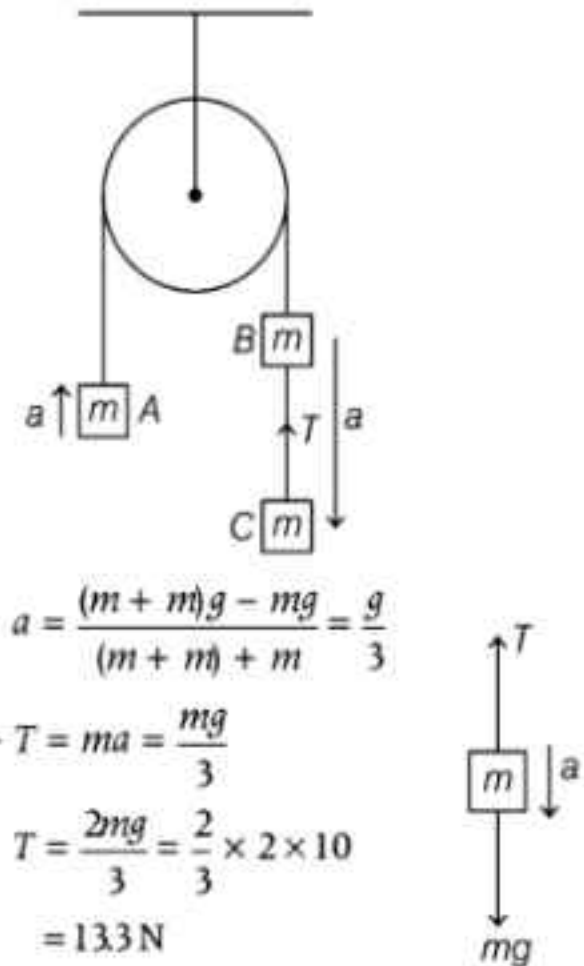
$$\Rightarrow v_1 = 4 \text{ m/s}$$

$$\Rightarrow 140 = 10 \times 4 + v_2 \quad [\text{from Eq. (i)}]$$

$$\Rightarrow v_2 = 100 \text{ m/s}$$

Final velocity of bullet = 100 m/s

20. (c) The combination of blocks A, B and C is shown in figure.

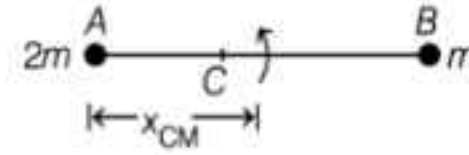


$$a = \frac{(m+m)g - mg}{(m+m) + m} = \frac{g}{3}$$

$$mg - T = ma = \frac{mg}{3}$$

$$\begin{aligned} T &= \frac{2mg}{3} = \frac{2}{3} \times 2 \times 10 \\ &= 13.3 \text{ N} \end{aligned}$$

21. (a)



Location of CM,

$$x_{CM} = \frac{2m \times 0 + m \times L}{2m + m} = \frac{L}{3}$$

The velocity of ball A w.r.t. the centre of mass C is

$$v_A = \omega x_{CM} = \frac{\omega L}{3}$$

$$v_B = \omega(L - x_{CM}) = \frac{2\omega L}{3}$$

Thus, angular momentum of a system about C,

$$\begin{aligned} L &= 2mv_A x_{CM} + mv_B(L - x_{CM}) \\ &= 2m \times \frac{\omega L}{3} \times \frac{L}{3} + m \times \frac{2\omega L}{3} \times \frac{2L}{3} \\ &= \frac{2m\omega L^2}{3} \end{aligned}$$

22. (b) Lateral shift, $Y = \frac{t \sin(i - r)}{\cos r}$

$$\frac{Y}{t} = \frac{\sin(i - r)}{\cos r} = \frac{\sin i \cos r - \cos i \sin r}{\cos r}$$

[using identity,

$$\begin{aligned} \sin(A - B) &= \sin A \cdot \cos B - \cos A \cdot \sin B \\ &= \sin i - \cos i \tan r \end{aligned}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \sin 45^\circ - \cos 45^\circ$$

$$\tan r = \frac{1}{\sqrt{2}} (1 - \tan r)$$

$$\Rightarrow \sqrt{\frac{2}{3}} = 1 - \tan r \Rightarrow \tan r = 1 - \sqrt{\frac{2}{3}}$$

$$\therefore r = \tan^{-1} \left(1 - \sqrt{\frac{2}{3}} \right)$$

23. (b) Given, $u = 60 \text{ m/s}$, $R = 180 \text{ m}$

$$\therefore R = \frac{u^2}{g} \sin 2\theta$$

$$180 = \frac{(60)^2}{10} \sin 2\theta$$

$$\Rightarrow \sin 2\theta = \frac{1}{2}$$

$$\Rightarrow \theta = 15^\circ$$

As there are always two directions of projections θ and $(90^\circ - \theta)$ for the given range, hence two directions of projection, i.e. 15° and $90^\circ - 15^\circ$, i.e. 15° and 75° .

Let T_1 and T_2 be the times of flight in the two cases, where

$$T_1 = \frac{2u \sin 15^\circ}{g}$$

and $T_2 = \frac{2u \sin 75^\circ}{g}$

The man is in danger for a time

$$T_2 - T_1 = \frac{2u}{g} (\sin 75^\circ - \sin 15^\circ)$$

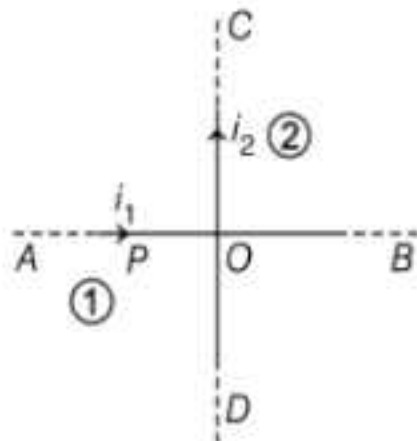
$$= \frac{2u}{g} (2 \cos 45^\circ \sin 30^\circ)$$

[using identity,

$$\sin C - \sin D = 2 \cos \frac{C+D}{2} \sin \frac{C-D}{2}]$$

$$= \frac{2 \times 60}{10} \times 2 \times \frac{1}{\sqrt{2}} \times \frac{1}{2} = 6\sqrt{2} \text{ s}$$

24. (c) Conductors AOB and COD are perpendicular to each other shown in figure.



At distance a above O ,

$$B_1 = \frac{\mu_0 i_1}{2\pi a} \quad \text{and} \quad B_2 = \frac{\mu_0 i_2}{2\pi a}$$

B_1 is perpendicular to B_2 .

Resultant of B_1 and B_2 ,

$$B = \sqrt{B_1^2 + B_2^2} = \frac{\mu_0}{2\pi a} \sqrt{i_1^2 + i_2^2}$$

25. (b)

$$\lambda = \lambda_\alpha + \lambda_\beta$$

$$= \frac{1}{T_\alpha} + \frac{1}{T_\beta} \quad \left[\because \lambda = \frac{1}{T} \right]$$

$$= \frac{1}{1620} + \frac{1}{405}$$

[given, $T_\alpha = 1620 \text{ yr}$ and $T_\beta = 405 \text{ yr}$]

$$= \frac{5}{1620} \text{ yr}^{-1}$$

$\frac{3}{4}$ th sample will decay, i.e. remaining $1/4$ th,

$$N = N_0 \left(\frac{1}{2} \right)^n$$

$$\frac{N_0}{4} = N_0 \left(\frac{1}{2} \right)^n$$

\Rightarrow

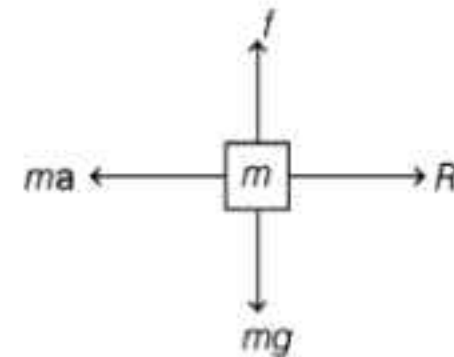
$$n = 2$$

\therefore

$$t = nT_{1/2} = n \frac{\ln 2}{\lambda}$$

$$= 2 \times \frac{0.693}{5/1620} = 449 \text{ yr}$$

26. (c) When cart moves with some acceleration towards right then a pseudo force (ma) acts on block towards left



This force ($m\alpha$) is action force by a block on cart. Now, block will remain static with respect to the cart, if frictional force

$$f = mg$$

$$\therefore f \leq \mu R \Rightarrow \mu R \geq mg$$

$$\Rightarrow \mu m\alpha \geq mg \quad [R = m\alpha]$$

$$\alpha \geq \frac{g}{\mu}$$

27. (a) We know the velocity of sound in a gaseous medium is given by

$$V = \sqrt{\frac{\gamma P}{\rho}}$$

At constant temperature $pV = \text{constant}$

$$\text{Volume of gas, } V = \frac{M}{\rho}$$

$$\Rightarrow \frac{PM}{\rho} = \text{Constant}$$

As M is constant, therefore $\frac{P}{\rho} = \text{Constant}$

Hence, change in pressure has no effect on velocity of sound.

28. (b) As, $\frac{GMm}{r^2} = \frac{mv^2}{r} = \text{Centripetal force}$

$$\Rightarrow v^2 = \frac{GM}{r} \Rightarrow T = \frac{2\pi r}{v}$$

$$\Rightarrow T^2 = \frac{4\pi^2 r^3}{v^2}$$

On putting the value of v^2 , we get

$$T^2 = \frac{4\pi^2 r^3}{\left(\frac{GM}{r}\right)} \Rightarrow T^2 = \frac{4\pi^2 r^3}{GM} \Rightarrow T^2 = Kr^3$$

Here, K is given by,

$$\frac{4\pi^2}{GM} = K \Rightarrow GMK = 4\pi^2$$

29. (c) From Coulomb's law force of repulsion is

$$F = k \frac{qq}{d^2} \Rightarrow F = \frac{1}{4\pi\epsilon_0} \frac{qq}{d^2}$$

where, $q = ne$

$$\therefore F = \frac{1}{4\pi\epsilon_0} \frac{n^2 e^2}{d^2} \Rightarrow n = \sqrt{\frac{4\pi\epsilon_0 F d^2}{e^2}}$$

30. (c) We know that capacitor offers infinite resistance for DC source (Battery is DC source).

Current taken from the cell.

$$I = \frac{E}{R+r} = \frac{2.5}{1+1+0.5} = 1 \text{ A}$$

Potential drop across capacitance

$$V = E - Ir = 2.5 - 1 \times 0.5 = 2 \text{ V}$$

The current in 2Ω resistor is zero charge on capacitor

$$Q = CV = 5 \times 2 = 10 \mu\text{C}$$

31. (b) van der Waal's gas equation for μ mole of real gas

$$\left(P + \frac{\mu^2 a}{V^2}\right)(V - \mu b) = \mu RT$$

$$\Rightarrow P = \left(\frac{\mu RT}{V - \mu b}\right) - \frac{\mu^2 a}{V^2}$$

$$\text{Given equation } P = \left(\frac{RT}{2V - b} - \frac{a}{4b^2}\right)$$

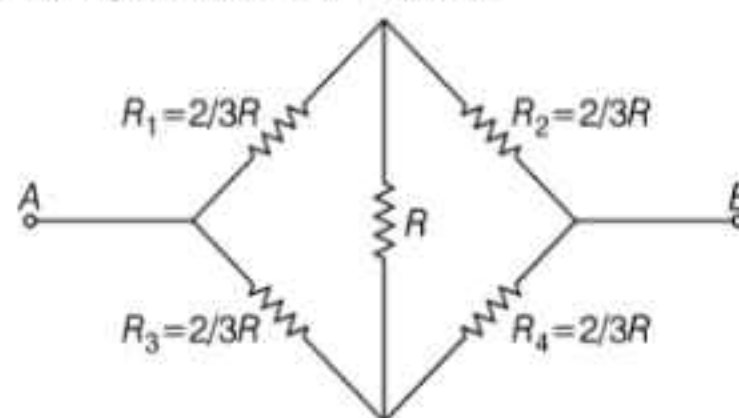
On comparing the given equation with this standard equation, we get $\mu = \frac{1}{2}$

$$\therefore \mu = \frac{m}{M}$$

\therefore Mass of gas

$$m = \mu M = \frac{1}{2} \times 44 = 22 \text{ g}$$

32. (b) Equivalent circuit will be



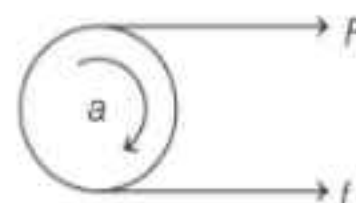
Now above circuit is a wheat stone's bridge.

By solving we get.

$$R_{AB} = \frac{\frac{4}{3}R \times \frac{4}{3}R}{\frac{4}{3}R + \frac{4}{3}R} = \frac{2}{3}R$$

33. (b) Let f be force of friction between the shell and horizontal surface

For translation motion we have,



$$F + f = ma \quad \dots(i)$$

For rotational motion,

$$FR - fR = I\alpha = I \frac{a}{R} \quad [\because a = R\alpha \text{ for pure rolling}]$$

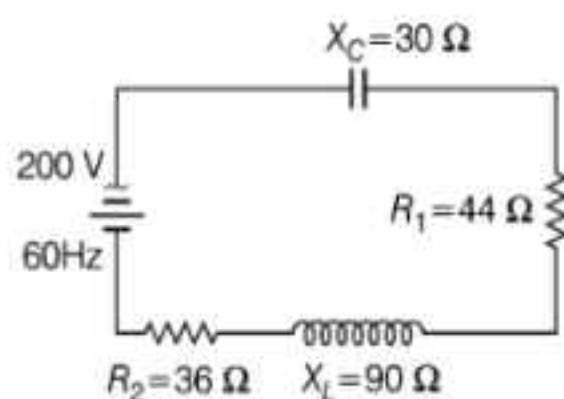
$$\Rightarrow F - f = I \frac{a}{R^2} \quad \dots(ii)$$

On adding Eqs. (i) and (ii), we get

$$2F = \left(m + \frac{I}{R^2}\right)a = \left(m + \frac{2}{3}m\right)a = \frac{5}{3}ma$$

$$\Rightarrow F = \frac{5}{6}ma \Rightarrow a = \frac{6F}{5m}$$

34. (a) Consider the given circuit as shown below,



Given $R_1 = 44 \Omega$

$R_2 = 36 \Omega$

$X_L = 90 \Omega$

$X_C = 30 \Omega$

Total resistance of the circuit is

$$R = R_1 + R_2 \\ = 44 + 36 = 80 \Omega$$

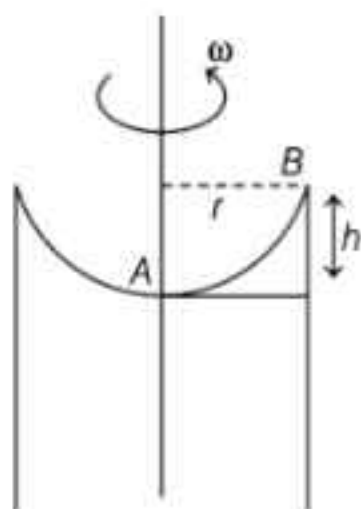
Impedance of the circuit,

$$Z = \sqrt{R^2 + (X_L - X_C)^2} \\ \Rightarrow Z = \sqrt{(80)^2 + (60)^2} \\ \Rightarrow Z = \sqrt{6400 + 3600} = 100 \Omega$$

Current, $I = \frac{V}{Z} = \frac{200}{100} = 2A$

Power dissipated in the coil, $P_{av} = I^2 R$
 $= (2)^2 \times 80 = 320 \text{ watt}$

35. (b) From Bernoulli's theorem we have,



$$P_A + \frac{1}{2} dV_A^2 + dgh_A = P_B + \frac{1}{2} dV_B^2 + dgh_B \\ \Rightarrow P_A + \frac{1}{2} dV_A^2 = P_B + \frac{1}{2} dB^2 \\ \Rightarrow P_A - P_B = \frac{1}{2} d(V_B^2 - V_A^2) \\ \text{Now, } v_A = 0, v_B = r\omega \\ P_A - P_B = hdg \\ \Rightarrow hdg = \frac{1}{2} dr^2\omega^2 \Rightarrow h = \frac{r^2\omega^2}{2g}$$

36. (a) Given, $d_A = 2 \text{ cm}$ and $d_B = 4 \text{ cm}$

$$\therefore r_A = 1 \text{ cm and } r_B = 2 \text{ cm}$$

From equation of continuity

$$av = \text{constant}$$

$$\therefore \frac{v_A}{v_B} = \frac{a_B}{a_A} = \frac{\pi (r_B)^2}{\pi (r_A)^2} = \left(\frac{2}{1}\right)^2$$

$$\Rightarrow v_A = 4v_B$$

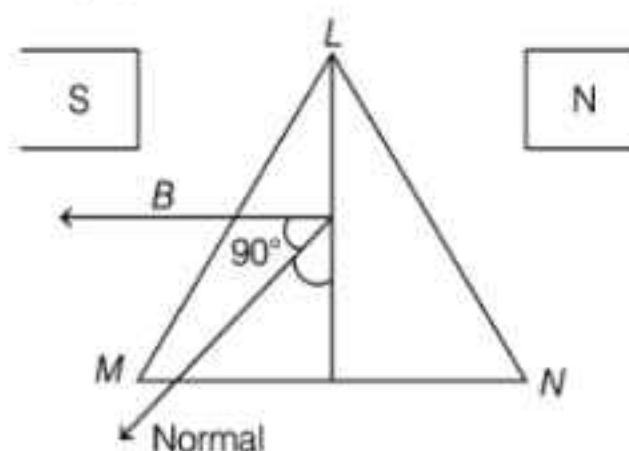
37. (a) Torque acting on an equilateral triangle in a magnetic field B is

$$\tau = IAB \sin \theta$$

Area of ΔLMN : $A = \frac{\sqrt{3}}{4} l^2$

and $\theta = 90^\circ$

Substituting the given values in the expression for torque, we have



$$\tau = I \times \frac{\sqrt{3}}{4} l^2 B \sin 90^\circ = \frac{\sqrt{3}}{4} I l^2 B$$

$$\therefore l = 2 \left(\frac{\tau}{\sqrt{3} BI} \right)^{\frac{1}{2}}$$

38. (d) Intensity through first polaroid,

$$I_1 = \frac{I_0}{2}$$

$$\therefore \text{Intensity of transmitted light, } I = I_1 \cos^2 0^\circ$$

$$= \frac{I_0}{2} \cos^2 (90^\circ - 30^\circ) = \frac{I_0}{2} \cos^2 60^\circ = \frac{I_0}{8}$$

39. (a) Cooling rate $\propto T^4 - T_0^4$

$$\Rightarrow r = \left[\frac{(900)^4 - (300)^4}{(600)^4 - (300)^4} \right] r_0$$

$$\Rightarrow r = \frac{16}{3} r_0$$

40. (c) Let $M \propto [F^a L^b T^c]$

Writing dimensions on both sides and using the principle of homogeneity of dimensions we have,

$$[M^1 L^0 T^0] = k[M^a L^b T^c]$$

on comparing the power on both sides we get

$$a = 1, a + b = 0$$

and $-2a + c = 0$

on solving we have

$$b = -1, c = 2, a = 1$$

\therefore units of mass is $[F L^{-1} T^2]$

41. (b) The voltage per unit length on the meter wire PQ is $\frac{6.00 \text{ mV}}{0.60 \text{ m}} = 10 \text{ mV/m}$

Hence potential across the meter wire PQ is 10 mV. Current drawn from the drives cell is.

$$I = \frac{10 \text{ mV}}{5 \Omega} = 2 \text{ mA}$$

Value of resistance is,

$$R = \frac{2V - 10 \text{ mV}}{2 \text{ mA}} = \frac{1990 \text{ mV}}{2 \text{ mA}} = 995 \Omega$$

42. (d) Distance between 1st order dark fringes = width of principle maximum

$$\begin{aligned} X &= \frac{2\lambda D}{d} = \frac{2 \times 600 \times 10^{-9} \times 2}{10^{-3}} \\ &= 2400 \times 10^{-6} = 24 \times 10^{-3} \text{ m} \\ &= 2.4 \text{ mm} \end{aligned}$$

43. (a) For total internal reflection at face AC

$$\begin{aligned} \sin i &> \frac{\mu_w}{\mu_g} \\ \Rightarrow \sin \theta &\geq \frac{4}{3 \times 1.5} \Rightarrow \sin \theta \geq \frac{8}{9} \end{aligned}$$

44. (c) As, $\Delta Q = Q_1 + Q_2 + Q_3 + Q_4$
 $= 5960 - 5585 - 2980 + 3645$
 $= 1040 \text{ J}$

$$\begin{aligned} \text{Also, } \Delta W &= W_1 + W_2 + W_3 + W_4 \\ &= 2200 - 825 - 1100 + W_4 \\ &= 275 + W_4 \end{aligned}$$

For a cyclic process, $\Delta U = 0$

$$\text{i.e., } U_f - U_i = 0,$$

From first law of thermodynamics,

$$\Delta Q = \Delta U + \Delta W$$

$$1040 = 0 + 275 + W_4 \text{ or } W_4 = 765 \text{ J}$$

45. (c) For series limit of Balmer series,

$$\begin{aligned} n_2 &= 2, n_1 = \infty \\ \frac{1}{\lambda} &= R \left[\frac{1}{n_2^2} - \frac{1}{n_1^2} \right] \end{aligned}$$

$$= \left[\frac{1}{(2)^2} - \frac{1}{(\infty)^2} \right] = \frac{R}{4}$$

$$\begin{aligned} \therefore \lambda &= \frac{4}{R} = \frac{4}{10967800} \text{ m} \\ &= 4 \times 912 \times 10^{-10} \text{ m} = 4 \times 912 \text{ \AA} \end{aligned}$$

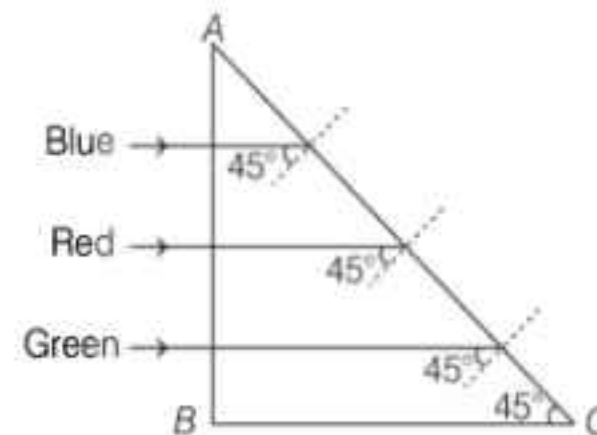
46. (b) Power output $= 3 \text{ kW} \times \frac{90}{100} = 27 \text{ kW}$

$$I_s = 6 \text{ A}$$

$$\therefore V_s = \frac{2.7 \text{ kW}}{6 \text{ A}} = 450 \text{ V}$$

$$\Rightarrow I_p = \frac{3 \text{ kW}}{200 \text{ V}} = 15 \text{ A}$$

47. (a) The situation is shown in figure



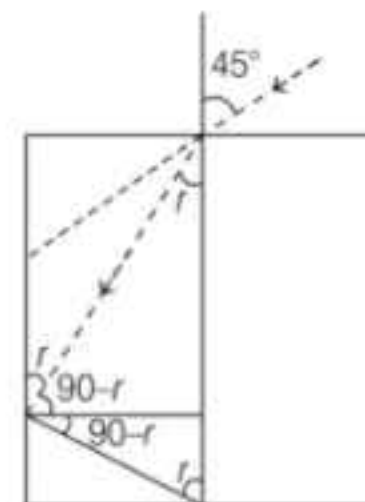
At face AB, $i = 0$. So, $r = 0$, i.e., light will be incident on face AC at an angle of incidence 45° . The face AC will not transmit the light for which $i > C$.

$$\text{i.e., } \sin i > \sin C$$

$$\Rightarrow \sin 45^\circ > \frac{1}{\mu} \text{ or } \frac{1}{\sqrt{2}} > \frac{1}{\mu} \Rightarrow \mu > \sqrt{2}$$

As refractive index for red colour is 1.39 which is less than $\sqrt{2}$, so red will be transmitted through face AC while green and blue will be reflected.

48. (d) From figure, we get



$$r = \sin^{-1} \left(\frac{1}{\sqrt{3}} \right)$$

For critical angle, $\sin C = \frac{1}{\mu}$

Now, by Snell's law, we have

$$\frac{\mu}{1} = \frac{\sin i}{\sin r} = \frac{\sin 45^\circ}{\sin\left(\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)\right)} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow \mu = \sqrt{\frac{3}{2}}$$

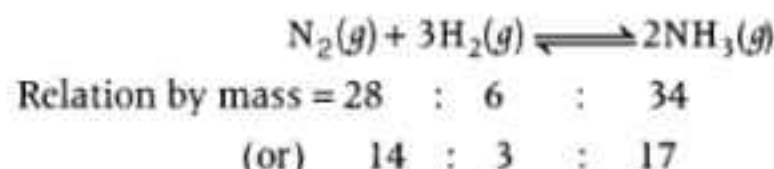
49. (a) Using equation, the total apparent shift is

$$s = h_1 \left(1 - \frac{1}{\mu_1}\right) + h_2 \left(1 - \frac{1}{\mu_2}\right)$$

or $s = 4 \left(1 - \frac{1}{4/3}\right) + 6 \left(1 - \frac{1}{3/2}\right) = 3.0 \text{ cm}$

Chemistry

51. (b) The relation used for formation of ammonia is



Given, $\text{N}_2(g) = 1.4 \text{ g} \Rightarrow \text{H}_2(g) = 1 \text{ g}$

Thus, $\text{N}_2(g)$ behave as a limiting reagent and $\text{NH}_3(g)$ will formed as per amount of N_2 used.

Therefore, 14 g of N_2 give $\text{NH}_3 = 17 \text{ g}$

$$\therefore 1.4 \text{ g of } \text{N}_2 \text{ give } \text{NH}_3 = \frac{17 \times 1.4}{14}$$

Amount of $\text{NH}_3(g) = 1.7 \text{ g}$

No. of moles of NH_3 , $n = \frac{w}{M}$

$$n = \frac{1.7}{17} = 0.1 \text{ mol.}$$

Also No. of moles of $\text{NH}_3 = \text{No. of atoms of N in } \text{NH}_3$

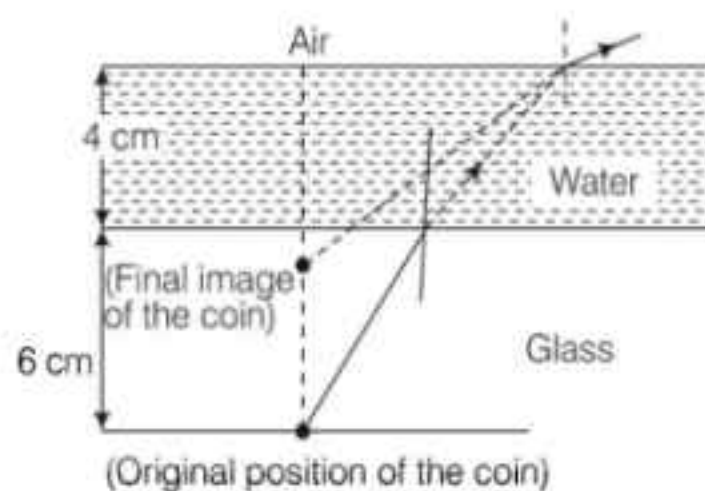
\therefore If no. of moles of $\text{NH}_3 = 0.1$

Then, no. of moles of N-atoms in $\text{NH}_3 = 0.1 \text{ mol}$

Hence, No. of moles of $\text{NH}_3 = 0.1 \text{ mol}$

No. of moles of N-atoms = 0.1 mol

52. (b) Due to small size and high electron density, electron-electron repulsion between two F-atom, causes increase in bond-length and thus decrease in bond energy. Hence, correct order is $\text{F}_2 < \text{Br}_2 < \text{Cl}_2$.

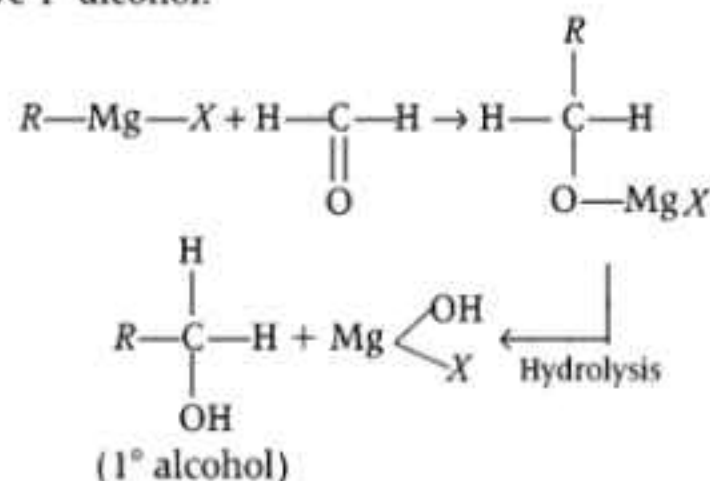


Thus, $h = h_1 + h_2 - s$
 $= 4 + 6 - 3 = 7.0 \text{ cm}$

50. (d) Relative velocity of the parrot w.r.t the train
 $= [10 - (-5)] \text{ ms}^{-1} = 15 \text{ ms}^{-1}$

Time taken by the parrot to cross then train
 $= \frac{150}{15} = 10 \text{ s}$

53. (a) RMgX with HCHO followed by hydrolysis will give 1° alcohol.



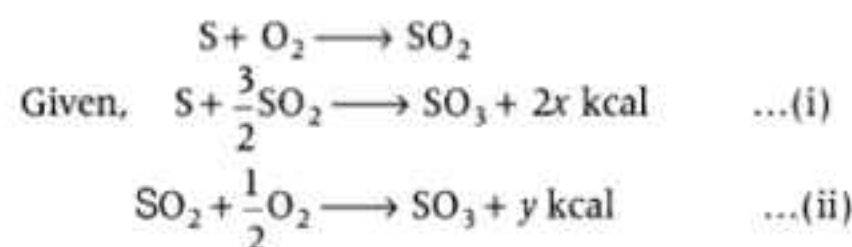
54. (a) Relation used $T_c = \frac{8a}{27Rb}$

where, a and b are van der Waals' constant.

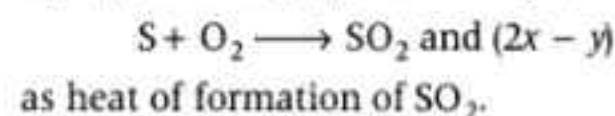
Keeping value of b constant, we have, $T_c \propto a$

As we know, more be the value of ' a ', more easily we can liquefy the gas. Hence, more be the value of T_c , more easily that gas will be liquefied i.e. A

55. (a) Our required equation will be



So, to get the required equation, we will subtract Eq. (ii) from Eq. (i), thus we get,



56. (c) (i) -3, (ii) -1, (iii) -2, (iv) -4

57. (a) Equation of combustion of isobutane will be as follows:



$$\therefore \Delta H = \Delta E + \Delta nRT$$

where, Δn = no. of gaseous moles (products) -

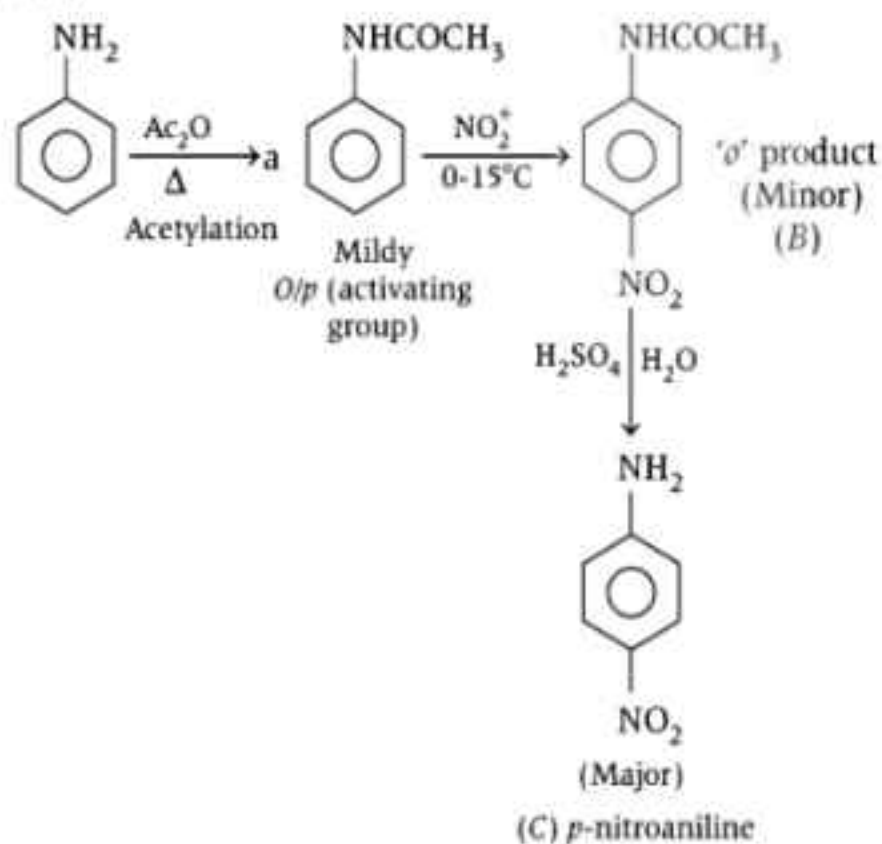
$\Delta n = (4 + 5) - \left(1 + \frac{13}{2}\right)$ number of moles of gaseous reactants.

$$\Delta n = +\frac{3}{2} (+ve)$$

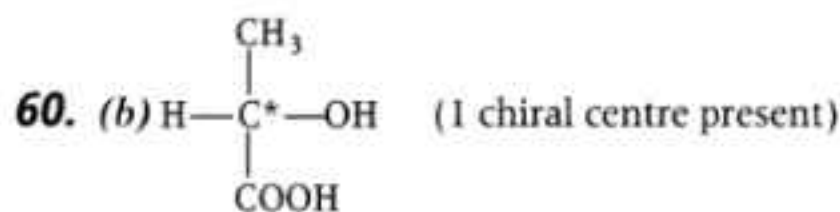
Since, Δn is +ve ΔH must be greater than ΔE .

$$\therefore \Delta H > \Delta E.$$

58. (c)



59. (c) Moist hydrogen cannot be dried over conc. H_2SO_4 because it is oxidised by H_2SO_4 and catches fire.



When $n = 1$ and no element of symmetry d and l forms = $2^n = 2$

meso form = 0

Total optical isomers = 2

61. (c) As per Fajan's rule

(i) More be the charge on cation/anion, more be the covalent nature.

(ii) For similar charges, smaller be the size of cation, more be the covalent nature.

Thus, correct order of covalent nature is



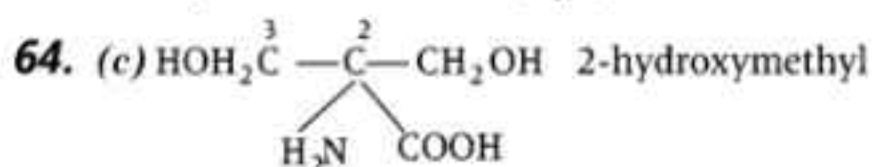
62. (a) H_3BO_3 accepts OH^- ion and acts as a weak monobasic Lewis acid.



$$K_a = 10^{-9}$$

Since, value of K_a is very small hence, H_3BO_3 is a weak acid.

63. (c) $CH_3CH_2OTs + \bar{C}N \longrightarrow CH_3CH_2CH_2CN + O^-Ts$
 $[O^-Ts]$ is a best leaving group and this reaction is 1° displacement reaction (S_N2).



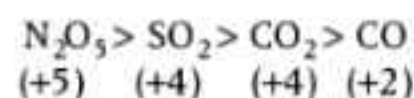
serine does not containing chiral carbon and hence is optically inactive.

65. (b)

(i) Higher be the positive oxidation value of non-metal oxide, higher be the acidic nature.

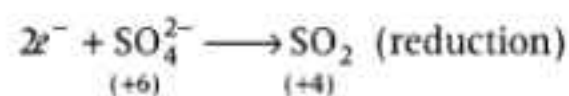
(ii) For same value of oxidation number, more electronegative element associated with oxygen shows more acidic nature.

Thus, correct order of acidic character is



Note CO is a neutral oxide.

66. (c) $2I^- \longrightarrow I_2 + 2e^-$ (oxidation)



67. (c) More be the number of unpaired electrons, more be the value of magnetic moment.

d^5 -configuration contains maximum number of unpaired electrons i.e. (= 5).

Thus, show maximum dipole moment as per the following relation,

$$\mu = \sqrt{n(n+2)} \text{ BM}$$

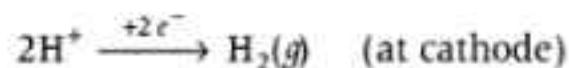
(Magnetic moment)

where, n = no. of unpaired electrons.

68. (a) In MnO_4^- , oxidation number of Mn is +7 means all the 3 d and 4 s electrons are lost to form $[MnO_4]^-$ complex.

Hence, has no d -electron.

69. (a) NaCl solution in water gives H_2 at cathode and Cl_2 at anode because of low discharge potential of H^+ ions as compared to Na^+ (at cathode) and of Cl^- as compared to OH^- ions (due to over voltage).



70. (d) Required relation

$$E_3 = \frac{n_1 E_1 - n_2 E_2}{n_3}$$

$$\therefore \text{Given,} \quad +2 \rightarrow 0 \quad \dots(i)$$

$$+2 \rightarrow +1 \quad \dots(ii)$$

Required, $+1 \rightarrow 0$

\therefore Subtract Eq. (ii) from Eq. (i).

$$\text{Here, } n_1 = 2, \quad E_1 = 0.337 \text{ V} \quad \dots(iii)$$

$$n_2 = 1, \quad E_2 = 0.153 \text{ V} \quad \dots(iv)$$

$$n_3 = 1,$$

$$\therefore E_3 = \frac{2 \times 0.337 - 1 \times 0.153}{1}$$

$$E_3 = 0.521 \text{ V}$$

71. (c) Relation used, $r \propto [\text{conc.}]^x$

(i) From exp. no. 1 and 4,

$$r_A \propto [\text{conc.}]^x \Rightarrow 4 \propto (4)^1$$

\therefore Order of reaction for reactant A = 1

(ii) From exp no. 2 and 3,

$$r_B \propto [\text{conc.}]^x \Rightarrow 4 \propto (2)^x$$

Order of reaction for reactant B = 2

Thus, order of reaction = $1 + 2 = 3$

72. (b) Since, unit of rate constant is $3.0 \times 10^{-5} \text{ s}^{-1}$, means order of reaction is one.

Thus, our rate law will be

$$r = k[N_2O_5]^1$$

$$\text{Given,} \quad r = 2.4 \times 10^{-5}$$

$$k = 3 \times 10^{-5}$$

$$\begin{aligned} \therefore [N_2O_5] &= \frac{r}{k} \\ &= \frac{2.4 \times 10^{-5}}{3 \times 10^{-5}} \\ &= 0.8 \text{ mol L}^{-1} \end{aligned}$$

73. (b) Compounds I and II have 2π -system and 10π system respectively. Both follow Huckel's rule $(4n + 2)\pi e^-$ ($n = 0, 1, 2, \dots$).

But III and IV system does not follow Huckel's rule.

74. (a) Zns has fcc (ccp) type structure, in which S^{2-} ions occupy corner and face centre positions, while Zn^{2+} ions are placed at alternate tetrahedral voids.

75. (d) None of these contain α -H atom hence, (d) is correct.

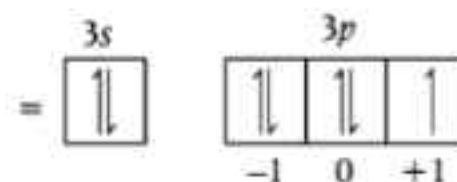
76. (c) An electron in hydrogen atom will only emit energy when it jumps from higher energy level to a lower energy level.

Order of energy change i.e. emission of energy is follows :

$$n_2 \rightarrow n_1 > n_3 \rightarrow n_2 > n_4 \rightarrow n_3 > n_5 \rightarrow n_4 > n_6 \rightarrow n_5 \dots\dots$$

Hence, among the given options, maximum energy emitted by an electron during its transition from $n_3 \rightarrow n_2$.

77. (a) For $Z = 17$, outer most electronic configuration is $\rightarrow 3s^2, 3p^5$. ($n = 3$)



Therefore, set of quantum number

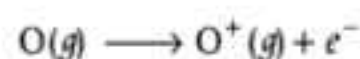
$$n = 3, \quad l = +1$$

$$m = \pm 1 \text{ i.e. } 1 \text{ (in this case) and } s = \pm \frac{1}{2}$$

Hence, correct option is (a).

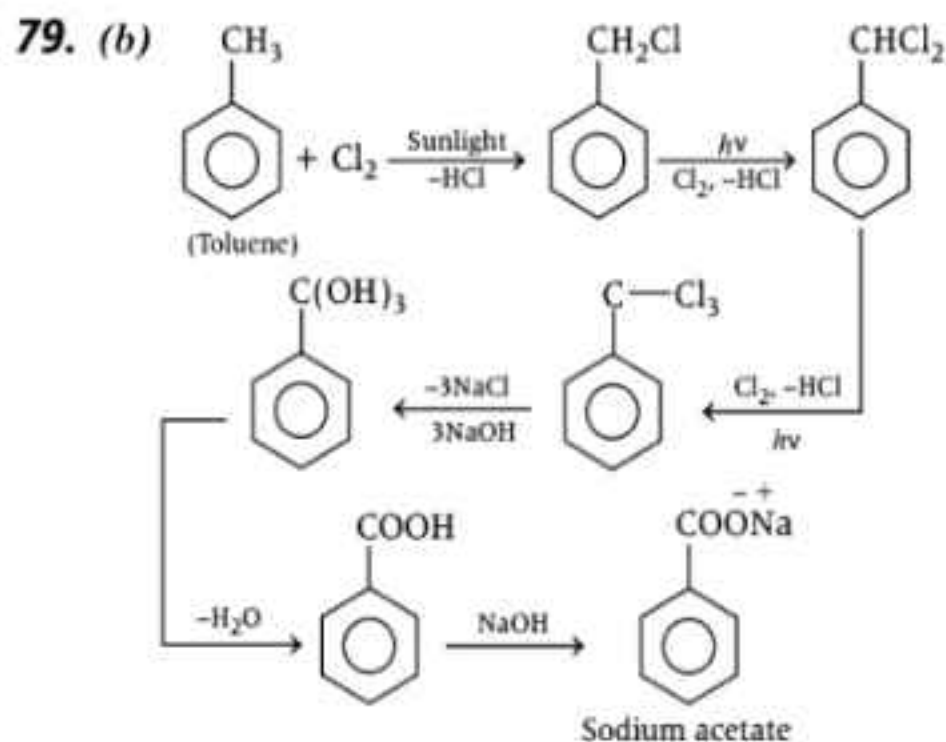
78. (d) $X(s) \rightarrow X(g)$, requires energy to change the state from solid to gas.

$O^-(g)$ has already one electron more than protons in nucleus. Therefore, it will repel the next incoming electron. So, energy is required to make



is an endothermic process. It requires energy to remove the electron from $O(g)$.

Only option (d) indicates release of energy due to electron gain enthalpy $[\Delta H = (-) \text{ ve}]$.



80. (a) In all the given three structures [(i), (ii) and (iii)], —OH group at second-last position is on the right hand side of chiral C-atom. Therefore, all have D-configuration.

81. (c) Let initial pressure = p
and initial volume = 100 unit.
Then, final volume = 95 unit
final pressure = ?
∴ The relation for an ideal gas is:

$$p_1 V_1 = p_2 V_2$$

$$p \times 100 = p_2 \times 95$$

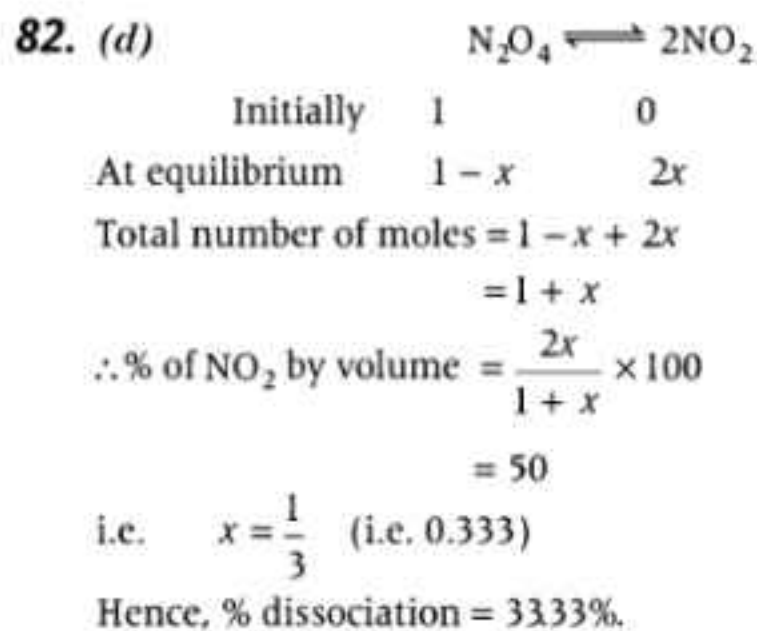
$$p_2 = \frac{p \times 100}{95}$$

$$= 1.0526 p$$

$$\therefore \text{Increase in pressure} = 1.0526 p - p$$

$$= 1.0526 \times 100 \text{ (for \%)} - 100$$

$$= 105.26 - 100 = 5.26\%$$



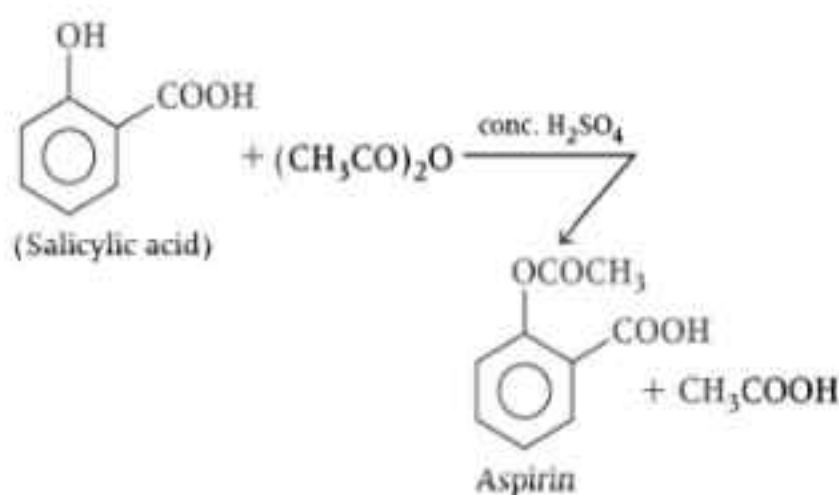
83. (b) The correct balanced chemical equation is

$$2\text{MnO}_4^- + 5\text{C}_2\text{O}_4^{2-} + 16\text{H}^+ \longrightarrow 2\text{Mn}^{2+} + 10\text{CO}_2 + 8\text{H}_2\text{O}$$

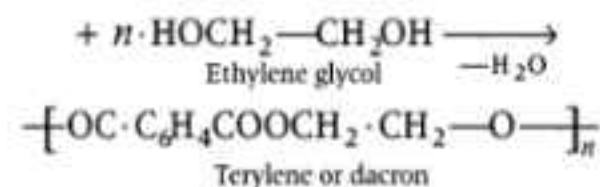
Hence, correct coefficients for $\text{C}_2\text{O}_4^{2-}$ and H^+ ions are 5 and 16 respectively.

84. (d) The chemical substances (drugs) used to bring down the body temperature in case of high fever are called antipyretics.
e.g., phenacetin, paracetamol etc.

85. (d) Preparation of aspirin from salicylic acid

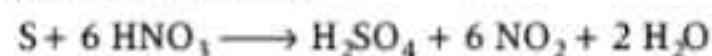


86. (d) $n\text{HOOC}-\text{C}_6\text{H}_4-\text{COOH}$
Terephthalic acid



87. (b) Boron trihalides are Lewis acids. The order of their acidic strength is $\text{BF}_3 < \text{BCl}_3 < \text{BBr}_3 < \text{BI}_3$
In boron halides, a $p\pi-p\pi$ back bonding arises due to empty orbital of boron and filled orbitals of halogen. This $p\pi-p\pi$ bonding has maximum effect in BF_3 as the size of B and F atoms are comparative. This effect decreases as the size of halogen atom increases. Due to this effect, tendency of accepting lone pair of electron of boron decreases, i.e. Lewis acid character decreases.

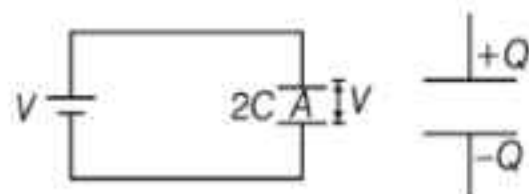
88. (a) The reaction between HNO_3 (conc.) and sulphur (s) is as follows:



Here, sulphur oxidised as H_2SO_4 and HNO_3 reduced to NO_2 .

Hence, we get, H_2SO_4 , NO_2 and H_2O as main products.

89. (b) When two waves are in same phase i.e. (+, +) or (-, -) overlap over each other they form bonding molecular orbitals while when they are in opposite phase i.e. (+, - or -, +), they form antibonding molecular orbitals as follows:



90. (d) Molar mass of ethanol (CH_3CHO)

$$= 12 + (3 \times 1) + 12 + 1 + (16 \times 1) \\ = 12 + 3 + 12 + 1 + 16 = 44$$

Heat of combustion is the heat produced due to combustion of 1 mol (44 g) of ethanol.

As x g of ethanol give y J of heat energy

$$\therefore 44 \text{ g of ethanol gives heat energy} = \frac{y \times 44}{x} \text{ J mol}^{-1}$$

As combustion is an exothermic process.

$$\text{Heat of combustion of ethanol} = -\frac{y}{x} \times 44 \text{ J mol}^{-1}$$

91. (a) 100 mL of solution contain 0.005 moles of $\text{Ba}(\text{OH})_2$.

\therefore 1 L (1000 mL) of solution contain

$$= 10 \times 0.005 \text{ mole of } \text{Ba}(\text{OH})_2$$

Concentration of $\text{Ba}(\text{OH})_2$ (i.e., moles in litres.)

$$= 0.05 \text{ M}$$

Each $\text{Ba}(\text{OH})_2$ give 2OH^- ions.

Thus, moles of OH^- (per L.) = $2 \times 0.05 = 0.1$

$$\text{(iii) } \therefore \text{pOH} = -\log [\text{OH}^-]$$

$$\text{pOH} = -\log [0.1] = -\log 10^{-1}$$

$$\text{pOH} = \log 10 = 1$$

92. (a) Food preservations prevent spoilage of food due to microbial growth. Sodium benzoate can be used as food preservative.

93. (c) Bakelite is condensed polymer of phenol ($\text{C}_6\text{H}_5 - \text{OH}$) and formaldehyde (HCHO)

94. (c) $\text{CH}_3\text{C}\equiv\text{CH} + \text{H}_2\text{O} \xrightarrow[\text{MgSO}_4]{\text{H}_2\text{SO}_4} [\text{CH}_3\text{C}(\text{OH})=\text{CH}_2]$
 \downarrow Tautomerisation
 CH_3COCH_3
 Acetone

95. (c) $[\text{NiCl}_4]^{2-}$; Oxidation state of Ni is $x - 4 = -2$
 $x = +2$

$$\text{Ni (28)} = [\text{Ar}] 3d^8 4s^2$$

$\therefore [\text{NiCl}_4]^{2-}$ has two unpaired electrons.

$$\text{Magnetic moment } (\mu) = \sqrt{n(n+2)} \text{ BM}$$

where, n = number of unpaired electrons.

$$\mu = \sqrt{2(2+2)} = \sqrt{8} = 2.82 \text{ BM}$$

96. (b) $\text{Cu}(+1)$ salts are unstable because Cu^+ salts disproportionate to Cu and Cu^{2+} salts, in aqueous solution.

97. (c) Atomic number of (B) = Z and is a noble gas.
 Atomic No. of (A) = $Z - 1$ (i.e., is a Halogen)
 Atomic No. of (C), = $Z + 1$ (i.e., is a alkaliu metal)
 At No. of (D) = $Z + 2$ (i.e., alkaline earth metal)
 Hence, element (A) must be a Halogen, so has highest electron affinity among the given species.
 (C) is an alkali metal and (D) is an alkaline earth metal.

98. (b) Physical as well as chemical, both type of adsorption are favoured by high pressure.
 Decrease in pressure causes de sorption in case of physical adsorption while not in case of chemical adsorption.

99. (b) As $r = k[\text{O}][\text{O}_3]$... (i)

To eliminate $[\text{O}]$ from fast step

$$K_c = \frac{[\text{O}][\text{O}_2]}{[\text{O}_3]} \text{ or, } [\text{O}] = \frac{K_c [\text{O}_3]}{[\text{O}_2]}$$

Substituting this value in Eq. (i) we have

$$r = \frac{K \cdot K_c \cdot [\text{O}_3][\text{O}_3]}{[\text{O}_2]}$$

Let, $K \cdot K_c = K'$

$$r = K' [\text{O}_3]^2 \cdot [\text{O}_2]^{-1}$$

100. (c) $K_w = [\text{H}^+] \cdot [\text{OH}^-]$ and for neutral water,

$$[\text{H}^+] = [\text{OH}^-], \text{ therefore } K_w = [\text{H}^+]^2$$

$$[\text{H}^+] = \sqrt{K_w} = \sqrt{27 \times 10^{-14}} = 1.63 \times 10^{-7} \text{ M}$$

$$\therefore \text{pH} = -\log [\text{H}^+] = -\log [1.643 \times 10^{-7}] = 6.78$$

Mathematics

101. (d) The direction cosines of the line are

$$l = \cos \alpha, m = \cos \beta, n = \cos \gamma$$

$$\text{Now, } l^2 + m^2 + n^2 = 1$$

$$\Rightarrow \cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$$

$$\Rightarrow 1 - \sin^2 \alpha + 1 - \sin^2 \beta + 1 - \sin^2 \gamma = 1$$

$$\Rightarrow \sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma = 2$$

102. (c) We know that,

$$\begin{aligned} \left\{ \frac{a}{|a|} - \frac{b}{|b|} \right\}^2 &= \left\{ \frac{a-b}{|a||b|} \right\}^2 = \frac{|a-b|^2}{|a|^2 |b|^2} \\ &= \frac{1+4+9}{9 \times 16} = \frac{14}{9 \times 16} = \frac{7}{72} \end{aligned}$$

103. (d) We have,

$$l + m - n = 0$$

$$\text{and } l^2 + m^2 - n^2 = 0$$

$$\Rightarrow l + m = n \text{ and } l^2 + m^2 = n^2$$

$$\Rightarrow l^2 + m^2 = (l + m)^2$$

$$\Rightarrow 2lm = 0$$

$$\Rightarrow l = 0 \text{ or } m = 0$$

$$\text{If } l = 0, \text{ then } m = n$$

$$\therefore \frac{l}{0} = \frac{m}{1} = \frac{n}{1}$$

$$\text{If } m = 0, \text{ then}$$

$$l = n$$

$$\therefore \frac{l}{1} = \frac{m}{0} = \frac{n}{1}$$

Thus, the dr's of the lines are proportional to 0, 1, 1 and 1, 0, 1.

Therefore, angle θ between them is given by

$$\cos \theta = \frac{0 \times 1 + 1 \times 0 + 1 \times 1}{\sqrt{0+1+1} \sqrt{1+0+1}} = \frac{1}{2} \Rightarrow \theta = \frac{\pi}{3}$$

104. (c) The number of 6-digits has two pairs of digits and 2 different digits.

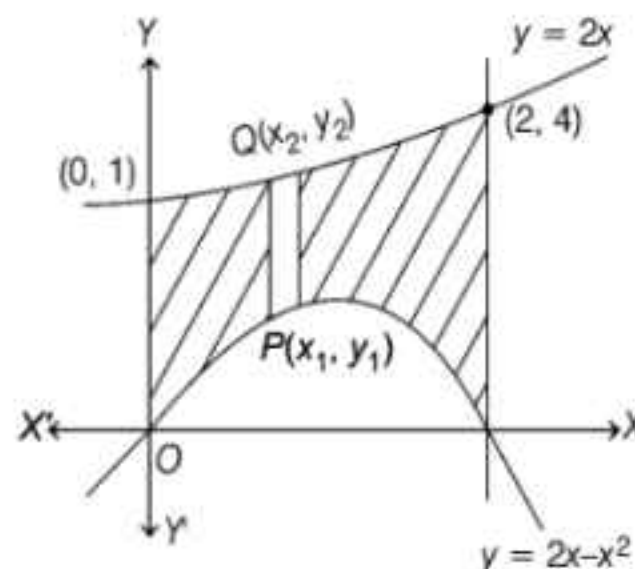
The number of ways of selecting 2 digits for two pairs and 2 other digits = ${}^4C_2 \times {}^2C_2$.

Now, we arrange these six digits which consists of two pairs and 2 different digits. This can be done in $\frac{6!}{2! 2!}$ ways.

\therefore Required number of numbers

$$= {}^4C_2 \times {}^2C_2 \times \frac{6!}{2! 2!} = 1080$$

105. (a)



Let the required area be A sq units. Then,

$$\begin{aligned} A &= \int_0^2 (y_2 - y_1) dx \\ &= \int_0^2 [2x - (2x - x^2)] dx \\ &= \left[\frac{2x^2}{2} - x^2 + \frac{x^3}{3} \right]_0^2 \\ &= \frac{4}{\log 2} - 4 + \frac{8}{3} - \frac{1}{\log 2} \\ &= \frac{3}{\log 2} - \frac{4}{3} \text{ sq units} \end{aligned}$$

106. (d) The equation of the curve is

$$y = x^2 + x - 1$$

$$\therefore \frac{dy}{dx} = 2x + 1$$

$$\Rightarrow \left(\frac{dy}{dx} \right)_{(1,1)} = 3$$

Now, A = Length of the tangent at $(1, 1)$

$$= \frac{\sqrt{1 + \left(\frac{dy}{dx} \right)^2}}{\frac{dy}{dx}} = \frac{\sqrt{1 + 3^2}}{3} = \frac{\sqrt{10}}{3}$$

B = Length of the subtangent at $(1, 1)$

$$= \frac{y}{\left(\frac{dx}{dy} \right)} = \frac{1}{3}$$

C = Length of the normal at $(1, 1)$

$$= \sqrt{1 + \left(\frac{dy}{dx} \right)^2} = \sqrt{1 + 3^2} = \sqrt{10}$$

D = Length of the subnormal at $(1, 1)$

$$\Rightarrow D = y \frac{dy}{dx} = 1 \times 3 = 3$$

Thus, we have $B < A < D < C$.

107. (b) If $f(x)$ has a local minimum at $x = -1$, then

$$\begin{aligned}\lim_{x \rightarrow -1^+} f(x) &= \lim_{x \rightarrow -1^-} f(x) \\ \Rightarrow \lim_{x \rightarrow -1^+} 2x + 3 &= \lim_{x \rightarrow -1^-} k - 2x \\ \Rightarrow -2 + 3 &= k + 2 \Rightarrow k = -1\end{aligned}$$

108. (d) The coordinates of A and B are $(0, b, c)$ and $(a, 0, c)$ respectively.

The equation of a plane passing through $O(0, 0, 0)$ is

$$Px + Qy + Rz = 0 \quad \dots(i)$$

It passes through A and B

$$\therefore P \times 0 + Q \times b + R \times c = 0$$

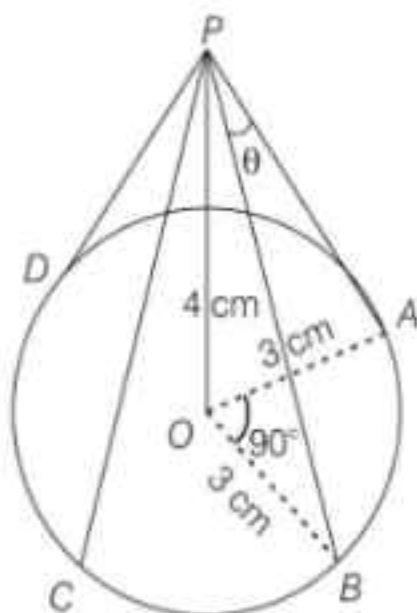
$$\text{and } P \times a + Q \times 0 + R \times c = 0$$

$$\Rightarrow \frac{P}{bc} = \frac{Q}{ac} = \frac{R}{-ab}$$

Substituting the values of P, Q and R in Eq. (i), we get

$$bcx + acy - abz = 0.$$

109. (c) Let O be the centre of the circular ring which is suspended by the strings PA, PB, PC and PD in such a way that P is just above the point O and $\text{arc } AB = \text{arc } BC = \text{arc } CD = \text{arc } AD$.



$$\therefore \angle AOB = 90^\circ$$

Also, in $\triangle AOP$, we have

$$AP = \sqrt{OA^2 + OP^2} = \sqrt{3^2 + 4^2} = 5 \text{ cm}$$

$$\Rightarrow BA = AP = 5 \text{ cm}$$

In $\triangle APB$, we have

$$\begin{aligned}\cos \theta &= \frac{AP^2 + BP^2 - AB^2}{2AP \cdot BP} = \frac{5^2 + 5^2 - (3\sqrt{2})^2}{2 \times 5 \times 5} \\ &\quad [\text{In } \triangle AOB, AB^2 = OA^2 + OB^2]\end{aligned}$$

$$\Rightarrow \cos \theta = \frac{16}{25}$$

110. (a)

$$\begin{aligned}&\sin^{-1} \left(\cot \left(\sin^{-1} \sqrt{\frac{2-\sqrt{3}}{4}} + \cos^{-1} \frac{\sqrt{12}}{4} + \sec^{-1} \sqrt{2} \right) \right) \\ &= \sin^{-1} \left(\cot \left(\sin^{-1} \left(\frac{\sqrt{3}-1}{2\sqrt{2}} \right) + \cos^{-1} \frac{\sqrt{3}}{2} + \cos^{-1} \frac{1}{\sqrt{2}} \right) \right) \\ &= \sin^{-1} [\cot(15^\circ + 30^\circ + 45^\circ)] \\ &= \sin^{-1} (\cot(90^\circ)) = \sin^{-1}(0) = 0\end{aligned}$$

111. (c) There are three ways to fill up each place. So, n places can be filled in 3^n ways.

Therefore, total number of n digit numbers $= 3^n$.

$$\text{Now, } 3^n \geq 900 \Rightarrow n \geq 7$$

Hence, the smallest value of n is 7.

112. (c) We have, x, y, z are in AP.

$$\Rightarrow 2y = x + z \quad \dots(i)$$

Also,

$\tan^{-1} x, \tan^{-1} y, \tan^{-1} z$ are in AP.

$$\Rightarrow 2 \tan^{-1} y = \tan^{-1} x + \tan^{-1} z$$

$$\Rightarrow \tan^{-1} \left(\frac{2y}{1-y^2} \right) = \tan^{-1} \left(\frac{x+z}{1-xz} \right)$$

$$\Rightarrow \frac{2y}{1-y^2} = \frac{x+z}{1-xz}$$

$$\Rightarrow 1 - y^2 = 1 - xz \quad [\text{using Eq. (i)}]$$

$$y^2 = xz$$

$$\Rightarrow x, y, z \text{ are in GP} \quad \dots(ii)$$

Using Eqs. (i) and (ii), we get $x = y = z$

113. (b) If n is odd, then required sum is given by

$$\begin{aligned}&1^2 - 2^2 + 3^2 - 4^2 + 5^2 - 6^2 + \dots \\ &\quad + \{(n-2)^2 - (n-1)^2\} + n^2 \\ &= (1-2)(1+2) + (3-4)(3+4) + (5-6)(5+6) + \dots \\ &\quad + \{(n-2)-(n-1)\} \{(n-2)+(n-1)\} + n^2 \\ &= -(1+2+3+\dots+(n-2)+(n-1)) + n^2 \\ &= -\frac{n(n-1)}{2} + n^2 = \frac{n(n+1)}{2}\end{aligned}$$

114. (b) Clearly, A will remain as $(0, 0)$; f_1 will make B as $(0, 4)$, f_2 will make it $(12, 4)$ and f_3 will make it $(4, 8)$; f_1 will make C as $(2, 4)$, f_2 will make it $(14, 4)$, and f_3 will make it $(5, 9)$. Finally, f_1 will make D as $(2, 0)$, f_2 will make it $(2, 0)$ and f_3 will make it $(1, 1)$. So, finally we get $A \equiv (0, 0)$, $B \equiv (4, 8)$, $C \equiv (5, 9)$ and $D \equiv (1, 1)$. Therefore,

$$m_{AB} = \frac{8}{4}, m_{BC} = \frac{9-8}{5-4} = 1,$$

$$m_{CD} = \frac{9-1}{5-1} = \frac{8}{4}$$

$$m_{AD} = 1, m_{AC} = \frac{9}{5}, m_{BD} = \frac{8-1}{4-1} = \frac{7}{3}$$

Hence, the final figure will be a parallelogram.

- 115. (a)** The given equation when expressed as a polynomial in derivatives is

$$p^2 \left(\frac{d^2 y}{dx^2} \right)^2 = \left\{ 1 + \left(\frac{dy}{dx} \right)^2 \right\}^3$$

Clearly, it is a second order differential equation of degree 2.

- 116. (d)** We have,

$$f(\theta) = 5 \cos \theta + 3 \cos \left(\theta + \frac{\pi}{3} \right) + 3$$

$$= 5 \cos \theta + \frac{3}{2} \cos \theta - \frac{3\sqrt{3}}{2} \sin \theta + 3$$

$$= \frac{13}{2} \cos \theta - \frac{3\sqrt{3}}{2} \sin \theta + 3$$

$$= \sqrt{\frac{169}{4} + \frac{27}{4}} \sin(\theta - \alpha) + 3$$

$$= 7 \sin(\theta - \alpha) + 3$$

Thus, the range of $f(\theta)$ is $[-4, 10]$.

- 117. (d)** Let D be the foot of the perpendicular and let it divide BC in the ratio $\lambda : 1$. Then, the coordinates of D are

$$\left(\frac{3\lambda + 4}{\lambda + 1}, \frac{5\lambda + 7}{\lambda + 1}, \frac{3\lambda + 1}{\lambda + 1} \right)$$

Now, $AD \perp BC$

$$\Rightarrow AD \cdot BC = 0$$

$$\Rightarrow -(2\lambda + 3) - 2(5\lambda + 7) - 4 = 0$$

$$\Rightarrow \lambda = -\frac{7}{4}$$

So, the coordinates of D are $\left(\frac{5}{3}, \frac{7}{3}, \frac{17}{3} \right)$.

- 118. (d)** We have,

$$x = \cos \theta, y = \sin 5\theta$$

$$\therefore \frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = -\frac{5 \cos 5\theta}{\sin \theta}$$

$$\Rightarrow \frac{d^2 y}{dx^2} = -5 \frac{d}{d\theta} \left(\frac{\cos 5\theta}{\sin \theta} \right) \cdot \frac{d\theta}{dx}$$

$$= \frac{-25 \sin \theta \sin 5\theta - 5 \cos \theta \cos 5\theta}{\sin^3 \theta}$$

$$\therefore (1 - x^2) \frac{d^2 y}{dx^2} - x \frac{dy}{dx}$$

$$= (1 - \cos^2 \theta) \left[\frac{-25 \sin \theta \sin 5\theta - 5 \cos \theta \cos 5\theta}{\sin^3 \theta} \right]$$

$$- \cos \theta \left[\frac{-5 \cos 5\theta}{\sin \theta} \right]$$

$$= -25 \sin 5\theta = -25y$$

- 119. (a)** Period of $\sin(\sin(nx))$ is $\frac{2\pi}{n}$ and that of $\tan\left(\frac{x}{n}\right)$ is $n\pi$.

For $n = 3$ we find that

Period of $\sin(\sin(nx))$ is $\frac{2\pi}{3}$ and that of $\tan\left(\frac{x}{n}\right)$ is 3π .

\therefore Period of $f(x)$ is 6π .

- 120. (c)** We have,

$$f(x) = \begin{cases} -x, & -1 \leq x < 0 \\ 1-x, & 0 \leq x < 1 \\ x, & 1 \leq x < 2 \\ 1+x, & 2 \leq x < 3 \\ 5, & x = 3 \end{cases}$$

Clearly, $f(x)$ is discontinuous at $x = 0, 1, 2$ and 3 . So, it is not differentiable at these points.

At $x = -1$, we have

$$\lim_{x \rightarrow -1^+} f(x) = \lim_{x \rightarrow -1^+} -x = 1 = f(-1)$$

So, it is continuous at $x = -1$.

Also, (RHD at $x = -1$) = -1 (a finite number).

Therefore, $f(x)$ is differentiable at $x = -1$.

- 121. (c)** We have,

$$I_n - I_{n-1} = \int_0^{\pi/2} \frac{\cos^2 nx - \cos^2 (n-1)x}{\sin x} dx$$

$$= \int_0^{\pi/2} \frac{\sin^2(n-1)x \sin^2 nx}{\sin x} dx$$

$$= \int_0^{\pi/2} \sin(2n-1)x dx$$

$$= \frac{1}{2n-1} [\cos(2n-1)x]_0^{\pi/2} = \frac{-1}{2n-1}$$

$$\therefore I_2 - I_1 = -\frac{1}{3}$$

$$I_3 - I_2 = -\frac{1}{5}$$

$$I_4 - I_3 = -\frac{1}{7}$$

Clearly, $I_2 - I_1, I_3 - I_2, I_4 - I_3$ are in HP.

- 122. (c)** We know that, the coefficient of the middle term is the numerically greatest coefficient in the expansion of $(1-x)^n$ or $(1+x)^n$ and its value is ${}^nC_{n/2}$ or $\frac{{}^nC_{n+1}}{2} = \frac{{}^nC_{n-1}}{2}$ according as n is even or odd.

It is given that the coefficient of the 5th term is the greatest. Therefore, 5th term is the middle term. Thus, there are 9 terms. Hence, $n = 8$.

- 123. (c)** Let r_1 be the statement $\sim(p \leftrightarrow \sim q)$. Then,
 $r_1 = \sim(p \leftrightarrow \sim q)$
 $\Rightarrow r_1 = \sim\{(\sim p \vee \sim q) \wedge (p \vee q)\}$
 $\quad [\because p \leftrightarrow q = (p \vee \sim q) \wedge (q \vee \sim p)]$
 $\Rightarrow r_1 = \sim\{(\sim(p \wedge q) \wedge (p \vee q))\}$
 $\Rightarrow r_1 = (p \wedge q) \vee (\sim p \wedge \sim q)$
 $\Rightarrow r_1 = \{(p \wedge q) \vee \sim p\} \wedge \{(p \wedge q) \vee \sim q\}$
 $\Rightarrow r_1 = \{(p \vee \sim p) \wedge (q \vee \sim p)\} \wedge \{(p \vee \sim q) \wedge (q \vee \sim q)\}$
 $\Rightarrow r_1 = \{t \wedge (q \vee \sim p)\} \wedge \{(p \vee \sim q) \wedge t\}$
 $\Rightarrow r_1 = (q \vee \sim p) \wedge (p \vee \sim q)$
 $\Rightarrow r_1 = (p \leftrightarrow q)$

- 124. (b)** The equation of the tangent $y^2 = 8x$ at $P(2, 4)$ is

$$4y = 4(x + 2) \\ \Rightarrow x - y + 2 = 0 \quad \dots(i)$$

Let (x_1, y_1) be the mid-point of chord QR. Then, equation of QR is

$$yy_1 - 4(x + x_1) - 5 = y_1^2 - 8x_1 - 5 \\ \Rightarrow 4x - yy_1 - 4x_1 + y_1^2 = 0 \quad \dots(ii)$$

Clearly, Eqs. (i) and (ii) represent the same line.

$$\therefore \frac{4}{1} = \frac{-y_1}{-1} = \frac{-4x_1 + y_1^2}{2}$$

$$\Rightarrow y_1 = 4 \text{ and } 8 = -4x_1 + y_1^2 \\ \Rightarrow y_1 = 4 \text{ and } x_1 = 2$$

- 125. (b)** The equation of a family of circles passing through the intersection of given circle is

$$x^2 + y^2 - 2x + y + \lambda(2x - y - 1) = 0 \\ \text{or } x^2 + y^2 - 2(1 - \lambda)x + (1 - \lambda)y - \lambda = 0$$

Let $C(h, k)$ be its centre. Then, $h = 1 - \lambda$

$$\text{and } k = -\left(\frac{1 - \lambda}{2}\right)$$

$$\Rightarrow h = -2k$$

Hence, the locus of (h, k) is $x = -2y$

$$\text{or } x + 2y = 0$$

$$\begin{aligned} \text{126. (d) We have, } \lim_{x \rightarrow 0} \frac{\int_0^{x^2} \sec^2 t \, dt}{x \sin x} \\ = \lim_{x \rightarrow 0} \frac{2x \sec^2 x^2}{x \cos x + \sin x} \quad [\text{using L's Hospital's Rule}] \\ = \lim_{x \rightarrow 0} \frac{2 \sec^2 x^2}{\cos x + \frac{\sin x}{x}} = 2 \left(\frac{1}{1+1} \right) = 1 \end{aligned}$$

- 127. (d)** Let $y = 7 - x$. Then, the given equation becomes

$$\begin{aligned} (y+1)^4 + (y-1)^4 &= 16 \\ y^4 + 6y^2 - 7 &= 0 \\ \Rightarrow (y^2-1)(y^2+7) &= 0 \\ \Rightarrow y^2-1 &= 0 \quad [\because y^2+7 \neq 0] \\ \Rightarrow y &= \pm 1 \\ \Rightarrow 7-x &= \pm 1 \Rightarrow x = 6, 8 \end{aligned}$$

- 128. (d)** For $n=1$, we have

$$10^{2n-1} + 1 = 10 + 1 = 11, \text{ which is divisible by 11.}$$

For $n=2$, we have

$$10^{2n-1} + 1 = 10^3 + 1 = 1001, \text{ which is divisible by 11.}$$

$$\therefore 10^{2n-1} + 1 \text{ is divisible by 11.}$$

- 129. (d)** Since, $f(x)$ is continuous at $x = \pi/4$

$$\begin{aligned} \therefore \lim_{x \rightarrow \pi/4} f(x) &= f(\pi/4) \\ \Rightarrow \lim_{x \rightarrow \pi/4} \frac{1 - \sqrt{2} \sin x}{\pi - 4x} &= a = \lim_{x \rightarrow \pi/4} \frac{-\sqrt{2} \cos x}{-4} = a \\ &\quad [\text{using De L'Hospital's Rule}] \\ \Rightarrow \frac{1}{2\sqrt{2}} \cos \frac{\pi}{4} &= a \Rightarrow a = \frac{1}{4} \end{aligned}$$

- 130. (b)** We have,

$$\begin{aligned} f(x) &= a \log|x| + bx^2 + x \\ \Rightarrow f'(x) &= \frac{a}{x} + 2bx + 1 \end{aligned}$$

Since, $f(x)$ attains its extremum values at $x = -1, 2$

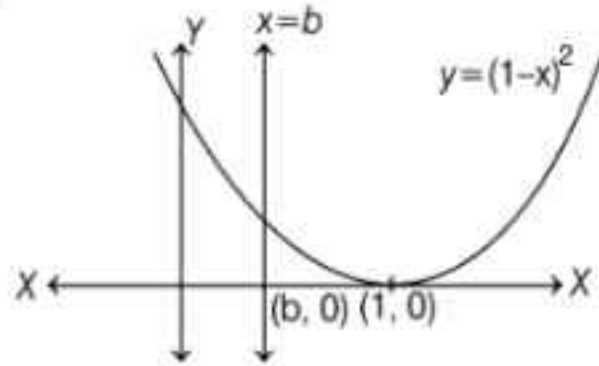
$$\begin{aligned} \therefore f'(-1) &= 0 \text{ and } f'(2) = 0 \\ \Rightarrow -a - 2b + 1 &= 0 \text{ and } \frac{a}{2} + 4b + 1 = 0 \\ \Rightarrow a &= 2 \text{ and } b = -\frac{1}{2} \end{aligned}$$

- 131. (d)** Let, $Q \in P$

$$\begin{aligned} \Rightarrow \sin \theta - \cos \theta &= \sqrt{2} \cos \theta \\ \Rightarrow (\sin \theta - \cos \theta)^2 &= 2 \cos^2 \theta \\ \Rightarrow \sin^2 \theta + \cos^2 \theta - 2 \sin \theta \cos \theta &= 2 \cos^2 \theta \end{aligned}$$

$$\begin{aligned}
 &\Rightarrow \cos^2 \theta + 2 \sin \theta \cos \theta + \sin^2 \theta = 2 \sin^2 \theta \\
 &\Rightarrow (\cos \theta + \sin \theta)^2 = 2 \sin^2 \theta \\
 &\Rightarrow \cos \theta + \sin \theta = \sqrt{2} \sin \theta \\
 &\Rightarrow \theta \in Q \\
 &\therefore P = Q
 \end{aligned}$$

132. (b)



$$\begin{aligned}
 \therefore R_1 &= \int_0^b (1-x)^2 dx \text{ and } R_2 = \int_b^1 (1-x)^2 dx \\
 \Rightarrow R_1 &= \left[\frac{(x-1)^3}{3} \right]_0^b \text{ and } R_2 = \left[\frac{(x-1)^3}{3} \right]_b^1 \\
 \Rightarrow R_1 &= \frac{(b-1)^3}{3} + \frac{1}{3} \text{ and } R_2 = \frac{-(b-1)^3}{3} \\
 \therefore R_1 - R_2 &= \frac{1}{4} \\
 \Rightarrow \frac{2}{3}(b-1)^3 + \frac{1}{3} &= \frac{1}{4} \\
 \Rightarrow \frac{2}{3}(b-1)^3 &= \frac{-1}{12} \\
 \Rightarrow (b-1)^3 &= \frac{-1}{8} \\
 \Rightarrow b-1 &= \frac{-1}{2} \Rightarrow b = \frac{1}{2}
 \end{aligned}$$

133. (b) We have,

$$\begin{aligned}
 \operatorname{sgn}(x - [x]) &= \begin{cases} 1, & \text{if } x \text{ is not an integer} \\ 0, & \text{if } x \text{ is an integer} \end{cases} \\
 \therefore \int_{-1}^{10} \operatorname{sgn}(x - [x]) dx &= 11(1 - 0) = 11
 \end{aligned}$$

134. (b) We have,

$$\begin{aligned}
 \cos^{-1} x - \sin^{-1} x &= \sin^{-1}(1-x) \\
 \Rightarrow \frac{\pi}{2} - 2\sin^{-1} x &= \sin^{-1}(1-x) \\
 \Rightarrow \frac{\pi}{2} - \sin^{-1}(1-x) &= 2\sin^{-1} x \\
 \Rightarrow \cos^{-1}(1-x) &= \cos^{-1}(1-2x^2) \\
 \Rightarrow 1-x-1-2x^2 & \\
 \Rightarrow 2x^2 - x &= 0 \Rightarrow x = 0, \frac{1}{2}
 \end{aligned}$$

135. (a) Let $\mathbf{b} = x\hat{i} + y\hat{j} + z\hat{k}$. Then,

$$\begin{aligned}
 \mathbf{a} \cdot \mathbf{b} &= 3 \Rightarrow x + y + z = 3 \\
 \text{and } \mathbf{a} \times \mathbf{b} &= \mathbf{c} \\
 \Rightarrow (z-y)\hat{i} + (x-z)\hat{j} + (y-x)\hat{k} &= j - k \\
 \Rightarrow z-y=0, x-z=1 \text{ and } y-x &= -1 \\
 \text{Solving these equations, we get} \\
 x = \frac{5}{3}, y = \frac{2}{3}, z = \frac{2}{3} \\
 \therefore \mathbf{b} &= \frac{1}{3}(5\hat{i} + 2\hat{j} + 2\hat{k})
 \end{aligned}$$

136. (b) We have,

$$\begin{aligned}
 T_n &= {}^n C_3 \\
 \therefore T_{n+1} - T_n &= 21 \\
 \Rightarrow {}^{n+1} C_3 - {}^n C_3 &= 21 \\
 \Rightarrow {}^n C_2 + {}^n C_3 - {}^n C_3 &= 21 \quad [\because {}^n C_r + {}^n C_3 - {}^n C_3 = 21] \\
 \Rightarrow {}^n C_2 &= 21 \\
 \Rightarrow \frac{n(n-1)}{2} &= 21 \\
 \Rightarrow n^2 - n - 42 &= 0 \\
 \Rightarrow (n-7)(n+6) &= 0 \Rightarrow n=7 \quad [\because n \geq 1]
 \end{aligned}$$

137. (a) Let OA be the vertical pole of height h and OP_1, OP_2, OP_3 be the lengths of shadow.

In $\triangle AOP_1$ we have

$$\tan \theta_1 = \frac{OA}{OP_1} = \frac{h}{h} = 1 \Rightarrow \theta_1 = \frac{\pi}{4}$$

In $\triangle AOP_2$ we have,

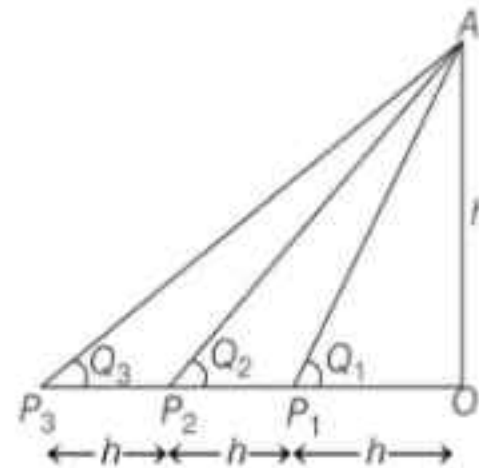
$$\tan \theta_2 = \frac{OA}{OP_2} = \frac{2}{2h} = \frac{1}{2} \Rightarrow \theta_2 = \tan^{-1} \frac{1}{2}$$

Similarly, $\tan \theta_3 = \frac{OA}{OP_3} = \frac{h}{3h} = \frac{1}{3}$

$$\theta_3 = \tan^{-1} \frac{1}{3}$$

\therefore Sum of the angles

$$= \theta_1 + \theta_2 + \theta_3 = \frac{\pi}{4} + \tan^{-1} \frac{1}{2} + \tan^{-1} \frac{1}{3}$$



$$= \frac{\pi}{4} + \tan^{-1} \left(\frac{1/2 + 1/3}{1 - 1/2 \times 1/3} \right)$$

$$= \frac{\pi}{4} + \tan^{-1} 1 = \frac{\pi}{4} + \frac{\pi}{4} = \frac{\pi}{2}$$

138. (d) We have

$$7 = \frac{4a + 24 + 7b + 45}{a + 4 + b + 5}$$

$$\Rightarrow 4a + 7b + 69 = 7a + 7b + 63$$

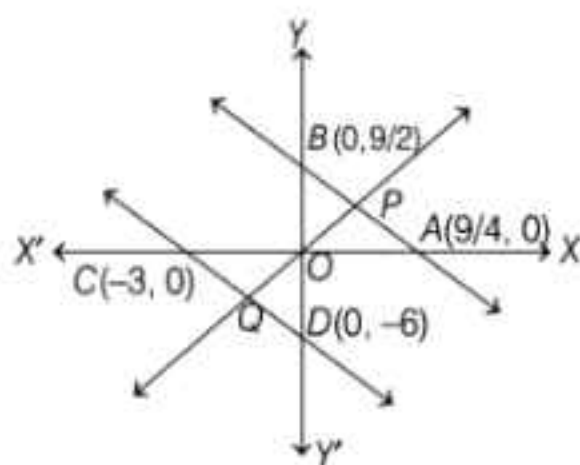
$$\Rightarrow a = 2$$

But b cannot be determined.

139. (b) Clearly, triangles OPA and OQC are similar

$$\Rightarrow \frac{OP}{OQ} = \frac{OA}{OC}$$

$$\Rightarrow \frac{OP}{OQ} = \frac{9/4}{3} = \frac{3}{4}$$



140. (a) We have,

$$2ae = \frac{2b^2}{a} \Rightarrow a^2e = b^2$$

$$\Rightarrow a^2e = a^2(1-e)^2$$

$$\Rightarrow e^2 + e - 1 = 0$$

$$\Rightarrow e = \frac{\sqrt{5}-1}{2}$$

141. (a) Let r be the radius of the spherical balloon and v be its volume.

$$\text{It is given that } \frac{dv}{dt} = 30 \text{ ft}^3 / \text{min}$$

$$\text{Now, } V = \frac{4}{3} \pi r^3$$

$$\Rightarrow \frac{dv}{dt} = 4\pi r^2 \frac{dr}{dt}$$

$$\Rightarrow 30 = 4\pi (15)^2 \frac{dr}{dt}$$

$$\Rightarrow \frac{dr}{dt} = \frac{1}{30\pi} \text{ ft/min}$$

142. (d) In $\triangle ABG$, we have

$$\cos \frac{\pi}{6} = \frac{AG}{AB} = \frac{\sqrt{3}}{2} = \frac{8}{3AB}$$

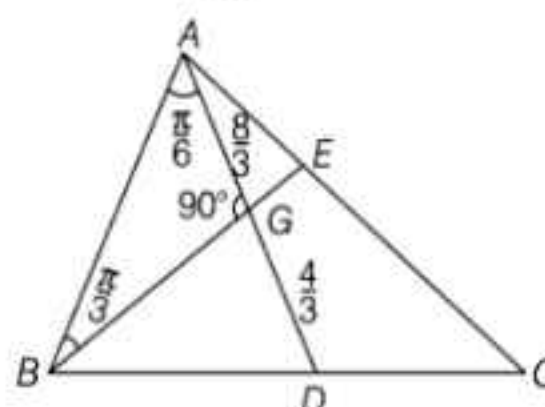
$$\Rightarrow AB = \frac{16}{3\sqrt{3}}$$

$$\therefore \text{Area of } \triangle ABD = \frac{1}{2} AB \cdot AD \sin \frac{\pi}{6}$$

$$= \frac{1}{2} \times \frac{16}{3\sqrt{3}} \times 4 \times \frac{1}{2} = \frac{16}{3\sqrt{3}} \text{ sq units}$$

$$\therefore \text{Area of } \triangle ABC = 2 \text{ Area of } \triangle ABD$$

$$= \frac{32}{3\sqrt{3}} \text{ sq units.}$$



143. (b) Comparing the given series with

$$1 + nx + \frac{n(n-1)}{2!} x^2 + \dots, \text{ we get}$$

$$nx = \frac{1}{9} \text{ and } \frac{n(n-1)}{2!} x^2 = \frac{4}{162}$$

$$\therefore \frac{n-1}{2n} = 2 \Rightarrow n-1 = 2n$$

$$\Rightarrow n = -\frac{1}{3}$$

$$\text{and } \frac{-1}{3} \cdot x = \frac{1}{9} \Rightarrow x = -\frac{1}{3}$$

\therefore Sum of series

$$= \left(\frac{1-1}{3} \right)^{-1/3} = \left(\frac{2}{3} \right)^{-1/3} = \left(\frac{3}{2} \right)^{1/3}$$

144. (d) Let $g(x) = \{x^{11} + f(x)\}^{-2}$. Then,

$$g'(x) = -2\{x^{11} + f(x)\}^{-3} \{11x^{10} + f'(x)\}$$

$$\Rightarrow g'(1) = -2\{1 + f(1)\}^{-3} \{11 + f'(1)\}$$

$$\Rightarrow g'(1) = -2(1+3)^{-3} \left(11 - \frac{1}{3} \right) = \frac{-1}{3} = f'(1)$$

145. (c) Clearly, $(1, 1)$, $(2, 2)$, $(3, 3)$ and $(4, 4)$ are not in R .

So, it is not reflexive

We observe that $(2, 3) \in R$ but $(3, 2) \notin R$, it is not symmetric.

Clearly, $(1, 3) \in R$ and $(3, 1) \in R$ but $(1, 1) \notin R$.
So, it is not transitive.
Since, $(2, 4)$ and $(2, 3)$ are in R . So, it is not a function.

146. (b) We have,

$$f(x) = [x] + \left[x + \frac{1}{2} \right] = \begin{cases} 0, & 0 < x < \frac{1}{2} \\ 1, & x = \frac{1}{2} \\ 1, & \frac{1}{2} < x < 1 \end{cases}$$

Clearly, $f(x)$ is discontinuous at $x = \frac{1}{2}$

Also, $\lim_{x \rightarrow \frac{1}{2}^-} f(x) = 0$ and $\lim_{x \rightarrow \frac{1}{2}^+} f(x) = 1$

147. (a)
$$\lim_{x \rightarrow \infty} \frac{\cot^{-1}(\sqrt{x+1} - \sqrt{x})}{\sec^{-1}\left\{\left(\frac{2x+1}{x-1}\right)^x\right\}}$$

$$= \lim_{x \rightarrow \infty} \frac{\cot^{-1}\left(\frac{1}{\sqrt{x+1} + \sqrt{x}}\right)}{\sec^{-1}\left\{\left(2 + \frac{3}{x-1}\right)^x\right\}}$$

$$= \frac{\cot^{-1}(0)}{\sec^{-1}(\infty)} = \frac{\frac{\pi}{2}}{\frac{\pi}{2}} = 1$$

148. (b) We have,

$$y = \cos^{-1}(\cos x) = \begin{cases} x, & \text{if } 0 \leq x \leq \pi \\ 2\pi - x, & \text{if } \pi \leq x \leq 2\pi \end{cases}$$

$$\therefore \left(\frac{dy}{dx}\right)_{x=\frac{5\pi}{4}} = \left(\frac{d}{dx}(2\pi - x)\right)_{x=\frac{5\pi}{4}} = -1$$

149. (c) We have,

$N = 100, F = 45, l = 20, h = 10$ and Median = 25

Let f be the frequency of the mediana class.

$$\text{Then, Median} = l + \frac{\frac{N}{2} - F}{f} \times h$$

$$\Rightarrow 25 = 20 + \frac{50 - 45}{f} \times 10$$

$$\Rightarrow 5 = \frac{50}{f} \Rightarrow f = 10$$

150. (b) Let a be the first term and r be the common ratio of the G.P. Then, $a > 0$ and $r > 0$.

Now,

$$a_n = a_{n-1} + a_{n-2}, n > 2$$

$$\Rightarrow ar^{n-1} = ar^{n-2} + ar^{n-3}$$

$$\Rightarrow r^2 = r + 1 \Rightarrow r^2 - r - 1 = 0$$

$$\Rightarrow r = \frac{1 \pm \sqrt{5}}{2} \Rightarrow r = \frac{1 + \sqrt{5}}{2} \quad [\because r > 0]$$