### **BITSAT 2015 Question Paper with Answer Key**

Birla Institute of Technology and Science Admission Test

# **BITSAT : SOLVED PAPER 2015**

### (memory based)

This question paper contains total  $\Im \Phi$ questions divided into four parts Part & Physics Q No 🔅 to Part .... ihemistry Q No 🔅 to Part יליליל 꾀序 쟼 nglish Proficien cy Q No <u>``</u>` to 序 ogical Reasoning Q No 黨 to 🏤 🕹 Part 🗸 V Mathematics Q No 🔅 to 🎲 🕹

- 꾀II questions are multiple choice questions with four options only one of them
- 쟼ach correct answer awarded 🏽 marks and –ૣ૽ૢ for each incorrect answer
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#### PART - I: PHYSICS

An artificial satellite is moving in a circular orbit 1. around the earth with a speed equal to half the 4. magnitude of the escape velocity from the earth. The height (h) of the satellite above the

Selface is (Take radius of earth as Re)

(a) 
$$h = 2R_e$$
 (b)  $h \equiv R_e$ 

- $h = 2R_e$
- (c)  $n = 2\pi_e$ In figure, two blocks are separated by a uniform 2. strut attached to each block with frictionless pins. Block A weighs 400N, block B weighs 300N, and the strut AB weigh 200N. If  $\mu = 0.25$  under B, determine the minimum coefficient of friction under A to prevent motion.



(b) 0.2 (c) 0.8 (a) 0.4 (d) 0.1 Two tuning forks with natural frequencies 340 3. Hz each move relative to a stationary observer. One fork moves away from the observer, while the other moves towards the observer at the same speed. The observer hears beats of

frequency 3 Hz. Find the speed of the tuning forks.

(d) 2.5.5m/s/s(b) 2 diss(a) cement/of a particle is given at time t, by:

 $x = A\sin(-2wt) + B\sin 2wt$  Then.

(a) the motion of the particle is SHM with an

amplitude of 
$$\sqrt{A2+\frac{B2}{4}}$$

(b) the motion of the particle is not SHM, but oscillatory with a time period of T = p/w

- the motion of the particle is oscillatory with (c)
- a time period of T = p/2w(d) the motion of the particle is a periodic.
- A ray parallel to principal axis is incident at 30° 5. from normal on concave mirror having radius of curvature R. The point on principal axis where rays are focussed is O such that PO is



6. A solid sphere of radius *R* has a charge *Q* distributed in its volume with a charge density r = kra, where *k* and *a* are constants and *r* is the distance from its centre. If the electric field at  $r = \frac{R}{r} = \frac{1}{r}$ 

$$\frac{2}{2}$$
 is  $\frac{2}{3}$  times that at  $r = R$ , the value of a is  
(a) 3 (b) 5 (c) 2 (d) 7  
A charged particle maying in a uniform product

- A charged particle moving in a uniform magnetic field and losses 4% of its kinetic energy. The radius of curvature of its path changes by
- (a) 2% (b) 4% (c) 10% (d) 12%
  8. Calculate the wavelength of light used in an interference experiment from the following data : Fringe width = 0.03 cm. Distance between the slits and eyepiece through which the interference pattern is observed is 1m. Distance between the images of the virtual source when a convex lens of focal length 16 cm is used at a distance of 80 cm from the eyepiece is 0.8 cm.

9. The masses of blocks A and B are m and M respectively. Between A and B, there is a constant frictional force F and B can slide on a smooth horizontal surface. A is set in motion with velocity while B is at rest. What is the distance moved by A relative to B before they move with the same velocity?



- 10. An elastic string of unstretched length L and force constant k is stretched by a small length x. It is further stretched by another small length y. The work done in the second stretching is (a) 1/2 Ky2 (b) 1/2 Ky(2x + y) (c) 1/2 K(x2 + y2) (d) 1/2 k (x + y)2
- 11. A body is thrown vertically upwards from A, the top of the tower, reaches the ground in time **1**. If it is thrown vertically downwards from A with

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(a) 
$$t = \frac{t_1 + t_2}{2}$$
 (b)  $t = \frac{t_1 - t_2}{2}$   
(c)  $t = \sqrt{t1t2}$  (d)  $t = \sqrt{\frac{t_1}{t^2}}$ 

12. 0.5 mole of an ideal gas at constant temperature 27°C kept inside a cylinder of length *L* and cross-section area A closed by a massless piston.



The cylinder is attached with a conducting rod of length L, the strength time direct ((1)(9) k) and dose other end is maintained at 0°C. If piston is moved such that rate of heat flow through the conducing rod is constant then velocity of piston when it is at height L/2 from the bottom of cylinder is : [Neglect any kind of heat loss from system]

(a) 
$$c \stackrel{a}{e} \stackrel{k}{R} \stackrel{o}{\sigma} ^{m/sec}$$
 (b)  $c \stackrel{a}{c} \stackrel{k}{I} \stackrel{o}{R} \stackrel{m/sec}{\sigma} \stackrel{m/sec}{\tau}$   
 $a \stackrel{k}{e} \stackrel{o}{R} \stackrel{c}{\sigma} \stackrel{m/sec}{\tau} \stackrel{m/sec}{\tau}$   
(b)  $c \stackrel{a}{c} \stackrel{k}{r} \stackrel{o}{\sigma} \stackrel{m/sec}{\tau}$ 

- 13. A conducting square loop is placed in a magnetic field *B* with its plane perpendicular to the field. The sides of the loop start shrinking at a constant rate a. The induced emf in the loop at an instant when its side is 'a' is
- (a) 2aaB (b) a2aB (c) 2a2aB (d) aaB
  14. The beam of light has three wavelengths 4144Å,4972Å and 6216 Å with a total intensity of 3.6 × 10−3 Wm2 equally distributed amongst the three wavelengths. The beam falls normally on the area 1 cm2 of a clean metallic surface of work function 2.3 eV. Assume that there is no loss of light by reflection and that each energetically capable photon ejects one electron. Calculate the number of photoelectrons liberated in 2s.

15. A square gate of size 1 m × 1m is hinged at its mid-point. A fluid of density r fills the space to the left of the gate. The force F required to hold the gate stationary is



16. When 0.50 Å X-rays strike a material, the photoelectrons from the k shell are observed to move in a circle of radius 23 mm in a magnetic field of 2 × 10-2 tesla acting perpendicularly to

the direction of emission of photoelectrons. What js the binding energy of k-shell 22. electrons? (a) (c) (d) keV

- In C2:9transistor amplifier,5.5he audio signal voltage across the collector restance of 2 kW is 2 V. If the base resistance is 1kW and the current amplification of the transistor is 100, the input signal voltage is
  - (a) 2 mV (b) 3 mV (c) 10 mV(d)0.1 mV
- 18. At the corners of an equilateral triangle of side a (1 metre), three point charges are placed (each of 0.1 C). If this system is supplied energy at the rate of 1 kw, then calculate the time required to move one of the mid-point of the line joining the other two.



(a) 50 h (b)60 h (c) 48 h (d)54 h

- 19. A vessel of volume 20L contains a mixture of hydrogen and helium at temperature of 27°C and pressure 2 atm. The mass of mixture is 5g. Assuming the gases to be ideal, the ratio of mass of hydrogen to that of helium in the given mixture will be
- (a) 1:2 (b)2:3 (c) 2:1 (d)2:5
  20. The resistance of a wire is *R*. It is bent at the middle by 180° and both the ends are twisted together to make a shorter wire. The resistance of the new wire is

(a) 
$$2R$$
 (b) $R/2$  (c)  $R/4$  (d) $R/8$ 

 In a YDSE, the light of wavelength l = 5000 Å is used, which emerges in phase from two slits a distance d = 3 × 10–7m apart. A transparent sheet of thickness t =  $1.5 \times 10-7m$  refractive index m = 1.17 is placed over one of the slits. what is the new angular position of the central maxima of the interference pattern, from the centre of the screen? Find the value of y.



The position of a projectile launched from the origin at t = 0 is given by F=40i<sup>+</sup>+50j<sup>+</sup>m at t = 2s. If the projectile was launched at an angle q from the horizontal, then q is (take g = 10 ms-2)

(a) 
$$\tan \frac{-12}{3}$$
 (b)  $\tan -1\frac{3}{2}$   
(c)  $\tan -1\frac{7}{4}$   $\tan -1\frac{4}{5}$ 

23. Water is flowing on a horizontal fixed surface, such that its flow velocity varies with *y* (vertical direction) as

$$v = \frac{\frac{2}{k_{c}^{2}}}{k_{c}^{2}} - \frac{y_{3}^{3}\ddot{o}}{a \div a}$$
 If coefficient of viscosity for

water is h, what will be shear stress between layers of water at y = a.

(a)  $\frac{hk}{a}$  (b)  $\frac{h}{ka}$ 

(c) 
$$-\frac{1}{k}$$
 (d) None of these

24. A load of mass m falls from a height h on to the scale pan hung from the spring as shown in the figure. If the spring constant is k and mass of the scale pan is zero and the mass m does not bounce relative to the pan, then the amplitude of vibration is (a) mg/d



to Pb206 is 3. Calculate the age of the ore, assuming that all the lead present in the ore is the final stable product of U238. Take the halflife of U238 to be  $4.5 \times 109$  yr.

(a)	1.6 × 193 yr	(b)	1.5 × 104 yr

(c)	1.867 × 109 yr	(d)	2 × 105 yr
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- 26. A direct current of 5A is superposed on an alternating current  $I = 10 \sin wt$  flowing through the wire. The effective value of the resulting current will be
  - (b) 5<sub>3</sub>A (a) (15/2)A (d) 15 A
  - 55/A (c)

27.

A planoconvex lens fits exactly into a planoconcave lens. Their plane surface are parall(a) 50 m (b)25 m(c)

the lenses, then focal length of combination is

(a) 
$$\frac{R}{\mu 1 - \mu 2}$$
 (b)  $\frac{2R}{\mu - \mu 2}$   
(c)  $\frac{R}{2(\mu - \mu 2)}$  (d)  $\frac{R}{2 - (\mu 1 + \mu 2)}$ 

28. A thin rod of length 4l and mass 4m is bent at the points as shown in figure. What is the moment of inertia of the rod about the axis passes through point O and perpendicular to the plane of paper?



- 29. One of the lines in the emission spectrum of Li2+ has the same wavelength as that of the 2nd line of Balmer series in hydrogen spectrum. The electronic transition corresponding to this line is  $n = 12^{\circ} n = x$ . Find the value of x.
- (a) 8 (b) 6 (c) 7 (d) 5 Two particles X and Y having equal charges, 30. after being accelerated through the same potential difference, enter a region of uniform magnetic field and describe circular paths of radii A and R2, respectively. The ratio of masses of X 36. ....

$$(R/R)142$$
 (R2/R1)  
 $(R/R)2$  (R1/R2)

25. In an ore containing uranium, the ratio of U238 31. A glass capillary tube of internal radius r = 0.25 mm is immersed in water. The top end of the tube projected by 2 cm above the surface of the water. At what angle does the liquid meet the tube? Surface tension of water = 0.7 N/m. (a) (c) A particle of mats) 2 on is projected at an angle 90° 45° with the toprizo total with a velocity of  $= 45^{\circ}$  $= 35^{\circ}$ 32.

> 202m/s. After 1s, explosion takes place and the particle is broken into two equal pieces. As result of explosion, one part comes to rest. The maximum height from the ground attained by other part is

40 m (d)35 m to each other. If the lenses are made of different  $A^2$  m wide truck is moving with a uniform speed  $1 \& \mu^2$  and R is v = 8 m/s along a straight horizontal road. A pedestrain starts to cross the road with a uniform v = 8 m/s along a straight horizontal road. A pedestrain starts to cross the road with a uniform speed v when the truck is 4 m away from him. The minimum value of v so that he can cross the road safelv is



A new from moving with speed v makesa head on collisio/swith a hydrogen atom in ground state kept at rest. The minimum kinetic energy of the neutron for which inelastic collision takes place is

Vertidal displacement of a Planek with a body of massely on it is varying accoeving to law y = sin

wt +  $\Im$  coswt. The minimum value of w for which the mass just breaks off the Planck and the moment it occurs first after t = 0, are given by

$$\begin{array}{c} (a) \quad \sqrt{g/2}, \ \frac{\sqrt{2}}{6} \frac{p}{\sqrt{g}} \\ \sqrt{g/2}, \ \frac{p}{3} \sqrt{2/g} \end{array} \qquad (b) \quad \frac{g}{\sqrt{2}}, \frac{2}{3} \sqrt{p/g} \\ \sqrt{g/2}, \ \frac{p}{3} \sqrt{2/g} \qquad \sqrt{2g}, \ \sqrt{2g}, \ \sqrt{2g} \end{array}$$

A parallel plate capacitor of capacitance C is connected to a battery and is charged to a potential difference V. Another capacitor of

capacitance 2C is similarly charge to a potential difference 2V. The charging battery is now disconnected and the capacitors are connected in parallel to each other in such a way that the positive terminal of one is connected to the negative terminal of the other. The final energy of the configuration is (a) Zero 3 cuto

(B) <sup>3</sup>/<sub>2</sub>€₩2

(c) 
$$\frac{25}{6}$$
 CV2

37. In the circuit shown below, the ac source has voltage V = 20 cos(wt) volt with w = 2000 rad/s. The amplitude of the current will be nearest to 4

(a) 2A	
(b) 3.3A	6Ω
(c) 2/ 5/A	
	$5 \text{ mH}, 4 \Omega$ 50 $\mu \text{F}$
(d) √5A	

38. A constant voltage is applied between the two ends of a uniform metallic wire. Some heat is developed in it. The heat developed is doubled if (a)th the length and the radius of the wire are halved.

(b)th the length and the radius of the wire are doubled.

the radius of the wire is doubled.

the e length of the wire is doubled.

- 39. The frequency of a sonometer wire is 100 Hz. When the weights producing the tensions are completely immersed in water, the frequency becomes 80 Hz and on immersing the weights in a certain liquid, the frequency becomes 60 Hz. The specific gravity of the liquid is
  - (a) 1.42 (b)1.77 (c) 1.82 (d)1.21
- 40. A long straight wire along the Z-axis carries a current I in the negative Z-direction. The magnetic vector field B at a point having coordinates (x, y) in the Z = 0 plane is

(a) 
$$\frac{m_0 I(y_i^2 - y_i^2)}{2^p (x^2 + y^2 x_j^2)}$$
 (b)  $\frac{m_0 I(x_i^2 + y_i^2)}{2p (x^2 + y^2)}$   
(c)  $\frac{m_0 I(x_j^2 - y_i^2)}{2p (x^2 + y^2)}$  (d)  $\frac{m_0 I(x_i^2 - y_j^2)}{2p (x^2 + y^2)}$ 

#### PART - II: CHEMISTRY

- Which of the following pollutants is main 41. product of automobiles exhaust? (a) C O (b) CO (c) NO (d) Hydrocarbons The disease caused the high concentration of 42 hydrocarbon pollutants in atmosphere is/are (a) silicosis (b) TB (d) asthma (c) cancer 43. The element, with atomic number 118, will be (a) alkali (b) noble gas (c) lanthanide (d) transition element .44 Which law of the thermodynamics helps in calculating the absolute entropies of substances at different various temperatukes? (b) Second law (d) Zeroth law (c) Third law 45. The color of CoCl 3.5NH3.H2O is (a) red (b) orange (c) orange - yellow (d) pink The metal present in vitamin B12 is 46. (a) magnesium (b) cobalt (d) zinc (c) copper 47. Cobalt (60) isotope is used in the treatment of : (a) Heart diseases (b) Skin diseases (c) Diabetes (d) Cancer 48. Polymer used in bullet proof glass is (a) Lexan (b) PMMA (d) Kevlar (c) Nomex 49. What is the correct increasing order of Bronsted bases? ClO-<ClO-3<ClO-<Clo (a) Cl0->Cl0-3>Cl0->ClQ-(b) ClO-<ClO-<ClO-<ClO-2 (c)
  - (d) Cl0->Cl0-3>Çl0-<Cl0-
- 50. The boiling point of alkyl halide are higher than those of corresponding alkanes because of
  - (a) dipole-dipole interaction
  - (b) dipole-induced dipole interaction
  - (c) H-bonding
  - (d) None of the above
- 51. Some salts containing two different metallic elements give test for only one of them in solution, such salts are
  - (a) double salts (b) normal salts
  - (c) complex salts (d) None of these





- 63. Which of the following according to Le-Chatelier's principle is correct?
  - (a) Increase in temperature favours the
  - (b) endothermic reaction Increase in
  - (c) temperature favours the exothermic reaction Increase in pressure shifts the equilibrium in that side in which number of gaseous moles increases All of the above are true

64. The efficiency of fuel cell is given by the expression, h is

None of the above

- 65. The mass of the substance deposited when one Faraday of charge is passed through its solution is equal to
  - (a) relative equivalent weight
  - (b) gram equivalent weight
  - (c) specific equivalent weight
  - (d) None of the above
- 66. The unit of rate constant for reactions of second order is

- (c) L mol s-1 (d) s-1
- 67. In a first order reaction with time the concentration of the reactant decreases (a) linearly (b) exponentially
  - (c) no change (d) None of these
- 68. The P−P−P angle in # molecule and S−S−S angle in 8 molecule is(in degree) respectively
  (a) 60°, 107°
  (b) 107°, 60°
  (c) 40°, 60°
  (d) 60°, 40°
- 69. The number of elements present in the d-block of the periodic table is
  - (a) 40 (b) 41 (c) 45 (d) 46
- 70. Which of the following represents hexadentate ligand?
  - (a) EDTA (b) DMG
  - (c) Ethylenediamine(d) None of the above
- 71. Which one of given elements shows maximum number of different oxidation states in its compounds?
  (a) Am
  (b) Fm
  (c) La
  (d) Gd

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72.	K 4[Fe(CN)6] is used in detecting. (a) Fe3+ ion (b) Cu+ ion (c) Cu3+ ion (d) Fe2+ ion
73.	A spontaneous reaction is impossible if (a) (b) (c) DH and DS are negative both (d) DH and DS are positive DH is Which can be and by imprestives temporary hard here is more and DS is negative
74.	
75.	<ul> <li>(a) Slaked lime</li> <li>(b) Plaster of Paris</li> <li>(c) Epsom</li> <li>(d) Hydrolith</li> <li>Graphite is a</li> <li>(b)</li> </ul>
76.	<ul> <li>(a) molecular solid</li> <li>(d) covalent solid</li> <li>(c) ionic solid</li> <li>(c) metallic solid</li> <li>(c) which of the following ionic substances will be most effective in precipitating the sulphur sol?</li> </ul>
	(a) KCl (b) BaCl <sub>2</sub> (c) Fe2(SO4)3 (d) Na3PO4
77.	Which of the following fluorides of xenon is impossible?
78.	(a) XeF <sup>2</sup> (b) XeF3 (c) XeF4 (d) XeF6 Thomas slag is (a) Ca 3 (PO4) 2
	(b) CaSiO <sub>3</sub> (c) Mixture of (a) and (b) (d) FeSiO <sub>3</sub>
79.	A sequence of how many nucleotides in messenger RNA makes a codon for an amino acid?
80.	(a) Three (b) Four (c) One (d) Two Which of the following molecule/ion has all the three types of bonds, electrovalent, covalent and
	co-ordinate : (a) HCl (b) NH $+_4$ (c) Cl- (d) H 2O2
	PART - III (A): ENGLISH PROFICIENCY
best	ECTIONS (Qs. 81-83): Choose the word which expreses the meaning of the underlined word in sentence.
81.	Decay is an <u>immutable</u> factor of human life. (a) important (b) unique

- (c) unchangeable
  (d) awful
  82. It was an <u>ignominious</u> defect for the team.
  (a) shameful
  (d) admirable
  (c) unaccountable
  (d) worthy
- 83. The attitude of western countries towards the third world countries is rather <u>callous</u> to say the least.
  - (a) cursed (d) unkend
  - (c) unfeeling (d) passive

DIR	DIRECTIONS (Qs. 84-86): Fill in the blank.				
84.		are the rights of			
	every human. (a) inalienable (c) incalculable	(d) institutional			
85.	The team was well trai how their was	lined and strong, but some low			
	(a) morale	(d) moral (d) consciousness			
86.	His speech was disapp	pointing: it all the			
		(b) revealed (d) analysed			
DIRECTIONS (Qs. 87-89): Choose the word which					

is closest to the opposite in meaning of the underlined word in the sentence.

- 87. Hydra is biologically believed to be immortal.
  (a) undying
  (b) perishable
  (c) ancient
  (d) eternal
- The Gupta rulers <u>patronised</u> all cultural activities and thus Gupta period was called the golden era in Indian History.
  - (a) criticised (b) rejected
  - (c) opposed (d) spurned
- 89. The General Manager is quete tactful and
  - handles the workers union very effectively. (a) incautious (b) discreet
    - (c) strict (d) disciplined

DIRECTIONs (Qs. 90-92): In each ot the following questions, out of the four alternatives, choose the one which can be substituted for the given words/ nt sentence.

- 90. A person who does not believe in any religion
  (a) Philatelist
  (b) Rationalist
  (c) Atheist
  (d) Pagan
- 91. A person who believes that pleasure is the chief good
  - (a) Stoic (d) Hedonist
  - (c) Epicure (d) Sensual
- 92. A person who is incharge of museum. (a) caretaker (b) warden (c) supervisor (d) curator

DIRECTIONS (Qs. 93-95): Choose the order of the sentences marked A, B, C, D and E to form a logical paragraph.

- 93. A. Tasty and healthy food can help you bring
  - B. out their best.
    - One minute they are toddlers and next you
       see them in their next adventure. Your young ones seem to be growing so fast.

- D. Being their loving custodians, you always
- E. want to see them doing well.
- Their eye sparkle with curiosity and endless questions on their tongues.

Codes (a)

DBCEA	(c)	(b)	CADEB
CBEDA		(d)	ECABD

- 94. A. It is hoping that overseas friends will bring in big money and lift the morale of the peop l e. But a lot needs to be done to kick
  - B. start industrial revival. People had big
  - C. hopes from the new gover n men t. So far
  - D. government has only given an incremental push to existing policies and programmes. Government is to go for big time reforms, which it promised.

E.

Codes	(a)			
BCDAE	(c)	(b)	EADCB	
DABCE		(d)	CDEAB	

95. A :Forecasting the weather has always been a defficult business.

B : During a period of drought, steams and rivers dried up, the cattle died from thirst and were ruined.

C :Many different things affect the weather and we have to study them carefully to make accurate forecast.

- D :Ancient egyptians had no need of weather in the Nille valley hardly ever changes. In
- E: early times, when there were no instruments, such as their mometer or the barometer, a man looked for tell tale signs in the sky.

(a) ABDCE (c)	(b)	EDCBA	
ACBDE	(d)	BDCAE	

#### PART - III (B): LOGICAL REASONING

96. Choose the correct answer figure which will make a complete square on joining with the problem figure Problem figure





97. In the following question, five figures are given. Out of them, find the three figures that can be joined to form square.



Choose the answer figure which completes the problem figure matrix.
 Problem Figures

Answer Figures



99. What is the opposite of 3, if four different positions of dice are as shown below :



100. In the following questions, one or more dots are placed in the figure marked as (A). The figure is followed by four alternatives marked as (a), (b), (c) and (d). One out of these four options

Answer Figures

contains region(s) common to the circle, square, triangle, similar to that marked by the dot in figure (A).





- 101. Complete the series by replaing '? mark G4T, J9R, M20P, P43N, S90L
  - (a) S90L (b)V185J(c) M20P (d)P43N
- 102. Neeraj starts walking towards South. After walking 15 m, he turns towards North. After walking 20 m, he turns towards East and walks 10 m. He then turns towards South and walks 5 m. How far is he from his original position and in which direction?

(a) 10 m, East	(b) 10 m, South-East
(c)10 m, West	(d)10 m, North-East

103. The average age of 8 men is increased by 2 yr when one of them whose age is 20 yr is replaced by a new man. What is the age of the new man

- 104. Shikha is mother-in-law of Ekta who is sister-in-law of Ankit. Pankaj is father of Sanjay, the only brother of Ankit. How is Shikha related to Ankit?
  (a) Mother-in-law
  (b) Aunt
  - (c) Wife (d) Mother
- 105. In a queue of children, Arun is fifth from the left and Suresh is sixth from the right. When they interchange their places among themselves, Arun becomes thirteenth from the left. Then, what will be Suresh's position from the right?

(a) 8	3th	(b) 14th	(c)	15th	(d) 16th
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#### PART - IV: MATHEMATICS

106. 
$$\lim_{x^{\oplus} ¥} \frac{\dot{Q}^{2x} x e^{x^2} dx}{e^{4x^2}}$$
 equals

(a) 0 (b) ¥ (c) 2 (d) 
$$\frac{1}{2}$$

107. If w is the complex cube root of unity, then the

(a) 
$$-1$$
 (b)1 (c)  $-i$  (d)i

108. The root of the equation

2(1+i)x2-4(2-i)x-5-3i=0 which has

greater modulus is

(a) 
$$\frac{3-5i}{2}$$
 (b)  $\frac{5-3i}{2}$   
(c)  $\frac{3-i}{2}$  (d) none

109. The value of  $\frac{3}{4} + \frac{1}{5} + \frac{6}{3} + ...$  upto n terms is

(a) 
$$n - \frac{4n}{3} - \frac{1}{3} \begin{pmatrix} 1 & 6 \\ 6 & 4 \end{pmatrix}$$
 (b)  $n + \frac{4 - n}{3} - \frac{1}{3}$   
(c)  $n + \frac{4^n}{3} - \frac{1}{3}$  (d)  $n - \frac{4 - n}{3} + \frac{1}{3}$ 

110. The period of tan 3q is

(a) p

f

(b) 3p/4 (d) None of these

(c) p/2 (d) None of t 111. If a function f(x) is given by

$$(x) = \frac{x}{1+x} + \frac{x}{(x+1)(2x+1)} + \frac{x}{(2x+1)^{X}(2x+1)} + \frac{x}{($$

- (a) has no limit
- (b) is not continuous
- (c) is continuous but not differentiable
- (d) is differentiable
- 112. If g is the inverse of function f and  $f c(x) = \sin x$ , then gc(x) is equal to
  - (a)  $cosec \{g(x)\}$  (b)  $sin \{g(x)\}$

(c) 
$$\frac{1}{\sin\{g(x)\}}$$
 (d) None of these

- 113. A bag contains (2n + 1) coins. It is known that n 119 Let a, b and c be three vectors satisfying a × b = of these coins have a head on both sides, whereas the remaining (n + 1) coins are fair. A coin is picked up at random from the bag and tossed. If the probability that the toss results in a head is 31/42, then n is equal to
- (a) 10 (b) 11 (c) 12 (d) 13 114. If f (x) is a differential function, then the solution of the differential equation  $dy + \{y f c(x) - f(x) f c(x) \}$ (x)dx = 0, is

(a) 
$$y={f(x)}-}+ce^{-f(x)}$$
  
(b)  $yf(x)={f(x)}2c$   
(c)  $fye(x)=f(e)f(x)+c$   
 $y-f(x)=f()^{x}f(x)$ 

- 115. The area of the region  $R = \{(x, y): |x| \notin |y| \text{ and } x^2\}$ + y2 £ 1} is
  - (a)  $\frac{3p}{8}$  sq units (b)  $\frac{5p}{8}$  sq units
- (c)  $\frac{p}{2}$  sq units (d)  $\frac{p}{8}$  sq unit 116. Universal set,
- $U = \{x \mid x5 6x4 + 11x3 6x2 = 0\}$  $A = \{x \mid x^2 - 5x + 6 = 0\}$  $B = \{x \mid x^2 - 3x + 2 = 0\}$ What is (A Ç B)' equal to ? (a) {1, 3} (b) {1, 2, 3}
  - (c) {0, 1, 3} (d) {0, 1, 2, 3}
- 117. If  $\cos -1x \cos \sin \frac{y}{2} = a$ ,
  - then  $42x 4xy \cos a +$ 2y is equal to (a) 2 sin 2a (b) 4 (c) 4 sin2a (d) - 4 sin2a
- 118. If  $\frac{ex + e5x}{e^{3x}} = a_0 + a1x + ax_2^2 + a3x^3 + \dots$  then
  - the value of 2a 1+23a3+25a5+.... is
  - (a)  $e^2 + e^{-2}$ (b) e4 – e–4 (c) e4 + e-4(d) 0

 $(a \times c)$ , |a| = |c| = 1, |b| = 4 and  $|b \times c| = 15$ . If b = 162c = la, then l equals

- 120. The total number of 4-digit numbers in which the digits are in descending order, is
  - (a) 10C × 4! 100 (þ) 10! None of these 4!
- 121. The line which is parallel to X-axis and crosses the curve y=  $\sqrt{x}$  at an angle of 45°, is

(a) 
$$x = \frac{1}{4}$$
 (b)  $y = \frac{1}{4}$   
(c)  $y = \frac{1}{2}$  (d)  $y = 1$ 

- 122. In a DABC, the lengths of the two larger sides are 10 and 9 units, respectively. If the angles are in AP, then the length of the third side can be
  - (a)  $5 \pm \sqrt{6}$ (b) 3.3 (d) Mone5of these

(a)

123. The arithmetic mean of the data 0, 1, 2, ....., n with frequencies 1, nÇ, nC,...., nC is

n (b) 
$$\frac{2n}{n}$$
 (c)  $n+1$  (d)  $\frac{n}{2}$ 

124. The mean square deviation of a set of n observation x, x, .... x about a point c is defined  $as \frac{1}{n} å(xiQ)$ 

> The mean square deviations about - 2 and 2 are 18 and 10 respectively, the standard deviation of this set of observations is

- (2a) 3 (b) (d) Not one lof these
- 125. Let S be the focus of the parabola  $y^2 = 8x$  and PQ 4y = 0 and the given parabola. The area of DPQS is
  - (a) 4 sq units (b) 3 sq units (c) 2 sq units (d) 8 sq units
- 126. The number of real roots of the equation ex-1 + x-2 = 0 is
  - (a) 1 (b) 2 (c) 3 (d) 4

127. Minimise 
$$Z = \prod_{j=1}^{n_0} \prod_{j=1}^{n_0} Z_{j} = b_j, j = 1, 2, ..., n$$
  
and  $Z_{j} = 1, 2, ..., m$  is a LPP with number of the set of different colours is.  
(a)  $m - n$  (b)  $m$  (c)  $m + n$  (d)  $\frac{m}{n}$   
(a)  $m - n$  (b)  $m$  (c)  $m + n$  (d)  $\frac{m}{n}$   
(a)  $m - n$  (b)  $m$  (c)  $m + n$  (d)  $\frac{m}{n}$   
(b)  $2/5$   
(c)  $3/5$  (d) None of these  
129. Let M be a 3 × 3 non-singular matrix with det (M)  
 $= a. If [M-1 adj (adj (M)] = KI, then the value of K is
(a) 1 (b) a (c) a2 (d) a3
130. Tangents are drawn from the origin to the curve
 $y = \cos x$ . Their points of contact lie on  
 $(a) 2 - 2 + \sqrt{2} - (b)$   
(b)  $2/5 + (c) 3/5 - (c) 3/5 - (c) 2p (d) 3p/2$   
131. The stog2e of the tangent to the curve  $y = e \cos x$   
 $x is minimum at  $x = a, 0 \in a \in 2p$ , then the value of  $x = a, \frac{y}{3-a} = \frac{z}{-2}$   
132. Two lines  $1 : x = 5, \frac{y}{3-a} = \frac{z}{-2}$   
133. The eccentricity of an ellipse, with its centre at the origin, is 1/2. If one of the directrices is  $x = 4$ , then the equation of the ellipse is:  
(a)  $4x^2 + 3y^2 = 1$  (b)  $3x^2 + 4y^2 = 12$   
(c)  $4x^2 + 3y^2 = 1$  (b)  $3x^2 + 4y^2 = 12$   
134. The function fixex  
(a)  $x = 2$  (b)  $x = -2(c) = (d) x = 0$  (d)  $x = 1$  (c)  $[1, 2]$$$ 

 $\frac{d^2y}{dx^2}$  ), then (1 + x2)  $\frac{d^2y}{dx^2} + x \frac{dy}{dx}$  is b) – n2y(c) - y(d)2*x*2*y* 

æ\_<u>1</u> ö ç—÷= ₿, e 1 ö — A and limxsin <sub>X:</sub>@\_ x<sup>®</sup> 0 e of the following is correct? **B**  $\neq$  0=1 and B(b) 1 If a and b are sBo≢x02 + ax + b(∉)0 then of  $x^2 + ax + b$  is

(a) 
$$\frac{2}{3}$$
 (b)  $-\frac{9}{4}$  (c)  $\frac{9}{4}$  (d) 1

then

< sin x

- < tan x
- n x < x
- he above
- the differential equation satisfying

$$\sqrt{1-x^2+}$$
  $\sqrt{1+y^2} = a(x-y)$  is  
(a) 1 (b) 2 (c) 3 (d) 4

olynomial of degree three satisfying f(1) = 0. Also, 0 is a stationary point loes not have an extremum at x = 0,

(a) 
$$\frac{x^2}{2} + C$$
 (b)  $x + C$ 

(d) None of these

the function

$$x = \frac{\sin^{-1}(x-3)}{\sqrt{9-x 2}}$$
 is

(b) [2,

- (d) 3)
  - [2,
  - 3]

142. If the intervention the point and 1, then the point and 1, and 1, q (p2, q2) and (p3, q3) (a) are collinear (b) form an equilateral triangle (c) form a scalene triangle (d) form a right angled triangle 143. Area of the circle in which a chord of length  $\sqrt{2}$ makes an angle p/2 at the centre, is (b) 2p sq units (a) p/2 sq units (d) p/4 sq units (c) p sq units 144. If  $\frac{\cos A}{\cos a} = n$ ,  $\frac{\sin A}{\cos a} = m$ , then the value of (m2 - n2)cosB sinB sin2B is (a) 1 + n2 (b)1 - n2(c) n2 (d)-n2 145. If complex number z 1, z2 and 0 are vertices of equilateral triangle, then z2+z22-z1z2 is equal to (a) 0 (b) z1 – z2(c) z1 + z2 (d)1 146. If  $r = \{(x, y) | x^2 + y^2 = 1; x, y \hat{I} R\}$ . Then, r is

(a) reflexive (b) symmetric

(c) transitive (d) anti-symmetric 147. A line makes the same angle with each of the X and Z-axes. If the angle, which it makes with Y-axis, is such that  $\sin 2b = 3\sin 2q$ , then cos2 q equals (a) 12/13 a bing miabdistribution n = 4, P(X = 0) = then P(X = 4) equals 16 cos2 q equals (d) 2/3 81,

(a) 
$$\frac{1}{16}$$
 (b)  $\frac{1}{-}$  (c)  $\frac{1}{27}$  (d)  $\frac{1}{8}$ 

149. Let f: R ® R be a function such that

$$f(x + y) = f(x) + f(y)$$
, "x, y Î R  
If f(x) is differentiable at x = 0, then which one of  
the following is incorrect?

- (a) f(x) is continuous, "xÎR
- (b) f¢(x) is constant, "xÎR
- (c) f(x) is differentiable, "xÎR
- (d) f(x) is differentiable only in a finite interval containing zero.
- 150. If binomial coefficients of three consecutive terms of (1 + x)n are in HP, then the maximum value of n is

(a) 1 (b) 1	2
-------------	---

(c) 0 (d) None of these

## SOLUTIONS

#### PART - I: PHYSICS

1. (b) The escape velocity from earth is given by

ve = 2gRe... (i) The orbital velocity of a satellite revolving around earth is given by

$$v0 = \frac{\sqrt{GMe}}{(Re+h)}$$

where, Me = mass of earth, Re = radius of earth, h = height of satellite from surface of earth.

By the relation  $GM_e = gR2_e$ 

So, 
$$v0 = \frac{\sqrt{gR_e^2}}{(Re+h)}$$
 ... (ii)  
Dividing equation (i) by (ii), we get  
 $\frac{v_e}{v_0} = \frac{\sqrt{2(Re+h)}}{(R_e)}$   
Given,  $v0 = \frac{ve}{2}$   
 $\frac{2v_e}{v_e} = \frac{\sqrt{2(R_e+h)}}{R_e}$   
Squaring on both side, we get  
 $4 = \frac{2(Re+h)}{Re}$   
or  $Re+h = 2Re$  i.e.,  $h = Re$   
Consider FBD of structure.

Applying equilibrium equations,  $Av + Bv = 200 \text{ N} \dots \text{ (i)}$   $AH = BH \dots \text{ (ii)}$ From FBD of block *B*,  $B_V$ 



 $B + BF \cos 60^\circ - NB \sin 60^\circ = 0$  $B_{\rm I}\cos 60^{\circ} - BV - 300 + FB\sin 60^{\circ} = 0$ **₿** = 0.25 NB **月** − 0.74 NB= 0 ... (iii) -B + 0.71 NB = 300 $-B + 0.71 , ... FBD of block A A_V$ ... (iv)  $A_H$ A  $F_A$ 400N NA FA - AH = 0NA - AV = 400... (v)  $FA = \mu A NA$  $\mu ANA - AH = 0$ ... (vi) On solving above equations, we get NA = 650 N, FA = 260N, FA = μANA  $\mu A = \frac{260}{250} = 0.4$ 

 (a) Let v = speed of sound and vS = speed of tuning forks. Apparent frequency of fork moving towards the observer is

n 
$$1 \stackrel{\text{@}}{\underset{\text{ev}}{=} \frac{v}{v} \stackrel{\text{"o}}{\underset{s}{=} \frac{v}{v}}$$

Apparent frequency of the fork moving away from the observer is

$$n_{2} = \frac{\underset{c}{\overset{}{\overset{}}{\overset{}}} v}{\underset{e}{\overset{}{\overset{}}{\overset{}}} v + v^{s}} \overset{\ddot{o}}{\overset{}{\overset{}}{\overset{}}}$$
  
If f is the number of beats heard per second.  
then f = n1 - n2

$$p f = \frac{a}{v_{c}^{2} - v^{s}} + \frac{a}{v_{e}^{2} + v^{s}} + \frac{a}{v_{e$$

2.

(a)

putting v = 340 m/s, f = 3, n = 340 Hz we get,  $v_s = \frac{340'3}{3'340} = 1.5 \text{ m/s}$ 

(a) The displacement of the particle is given by: 4.

$$x = A\sin(-2wt+) \quad B\sin^2 wt$$
  
=  $-A\sin^2 wt + \frac{B}{2}(1 - \cos^2 wt)$   
=  $-(A\sin^2 wt + \frac{B}{2}\cos^2 wt) + \frac{B}{2}$   
This motion represents SHM with an  
amplitude:  $\sqrt{A2 + \frac{B}{4}^2}$ , and mean position  
 $\frac{B}{2}$ .

7.

8.

(d) From similar triangles, 5.



$$PQ = PC - QC = R \frac{-R}{\sqrt{3}} = R \frac{2}{\varepsilon^{1}} \frac{1}{\sqrt{3}} \frac{\ddot{o}}{\dot{\sigma}}$$

(c) Using Gauss's law, we have 6.

$$\widetilde{\mathsf{N}}\overset{\mathsf{K}}{\mathsf{O}} \overset{\mathsf{E}}{\mathsf{C}} \overset{\mathsf{I}}{\mathsf{A}} \overset{\mathsf{I}}{\mathsf{I}} \overset{\mathsf{O}}{\mathsf{O}} (\mathsf{r} dv) \overset{\mathsf{I}}{\overset{\mathsf{O}}{\mathsf{O}}} \overset{\mathsf{R}}{\mathsf{O}} \overset{\mathsf{r} a \, ' \, 4 \, \mathsf{p}^{r2dr}}{\overset{\mathsf{O}}{\mathsf{O}}}_{0}^{\mathsf{C}}$$
or  $E' 4 \mathsf{p} R^{2} = \overset{\mathfrak{C}}{\overset{\mathsf{C}}{\mathsf{e}}} \overset{\mathsf{I}}{\overset{\mathsf{O}}{\mathsf{O}}} \overset{\mathfrak{O}}{\overset{\mathsf{O}}{(a+3)}}$ 

$$\land E1 = \frac{k R^{(a+1)}}{10 (a+3)}$$

$$\mathsf{For } r = \frac{R}{2} \cdot E2 = \frac{\overset{\mathfrak{C}}{\overset{\mathsf{C}}{\mathsf{E}}} \overset{\mathfrak{O}}{\overset{\mathsf{O}}{\mathsf{O}}} \overset{\mathfrak{O}}{\overset{\mathsf{O}}{\mathsf{O}}}^{\mathsf{I}}}{0 (a+3)}$$

$$\mathsf{G} \text{ iven } , E2 = \frac{E_{1}}{8}$$

or 
$$\frac{k}{1}\frac{geR}{G}\frac{gaR}{d} = \frac{1}{8}\frac{kR(a^{+1})}{10(a+3)}$$

$$\int_{0}^{1}\frac{1}{a+1} = \frac{1}{8}$$

$$\int_{0}^{0}\frac{1}{a+1} = \frac{1}{8}$$

0.8 cm. Image distance v = 80 cm Object distance = u Using mirror formula, 1 1 1 1 1 1

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f} \stackrel{P}{\Rightarrow} \frac{1}{60} + \frac{1}{u} = \frac{1}{16}$$

$$\stackrel{P}{\Rightarrow} u = 20 \text{ cm}$$
Magnification,  $m = \frac{v}{u} = \frac{8}{0} = 4$ 
Magnification = i d stancesbetween images of slits
$$= \frac{0.8}{d} = \frac{1}{d} = 4 \stackrel{P}{\Rightarrow} d = 0.2 \text{ cm}$$
Fringe width  $b = \frac{Dl}{d}$ 

Therefore, the work done against elastic for ce

 $W_{\text{external}} = -W = \frac{ky}{2}(2x+y)$ 1. (c) Let the body is projected vertically upwards from A with a speed u0. Using equation, s= ut  $\frac{+1}{2}$  at2 For case (1) – h = utr  $\frac{1}{2}gt^2$  ...(1) For case (2) – h = u0t2  $-\frac{2}{-gt_1^2}$  ...(2) Subtracting eq (2) from (1), we get  $0 = u 0(t2 + ) = \frac{1}{2}g(t22 - t)$  $P_{\text{U}} = \frac{1}{2}g(1 - t^2) \dots (3)$ Putting the value of u0 in eq (2), we get  $P h=(\frac{1}{2}).t.(4)$ For case 3, u0 = 0, t = ? -h=0′ æ1ö e2÷gt<sup>2</sup> æ1ö § ∋gt2 Comparing eq. (4) and (5), we get  $\frac{1}{2}$  gt2=1gt1t2 \ t=  $\sqrt{t1t_2}$ DQ = DW = work done per unit time = L2. (c)  $\frac{D_{\tau}}{Dt} \frac{D_{\tau}}{Dt}$ k aq L  $\frac{dW}{dt} = P \frac{dV}{dt} = k \frac{aq}{L}, P = \frac{nRT}{V}$  $\Rightarrow \quad \frac{0.5R(300)}{V}A.\frac{dl}{dt} = \frac{kaq}{L}$  $P \qquad \frac{0.5 R(300)}{A.\frac{L}{2}} A.v = \frac{kaq}{L}$  $v = \frac{k\alpha}{R} \frac{\approx 27}{\xi} \frac{\ddot{o}}{300} \frac{\dot{o}}{\dot{\phi}} = \frac{k}{100R}$ Þ 13. (a) At any time t, the side of the square  $a = (a_0)$ -a t), where a0 = side at t = 0.

At this instant, flux through the square :  $f = BA \cos 0^{\circ} = B (a \oplus at)^{2}$  df emf induced E = - dt E = -B.2 (a0 - a t) (0 - a) = +2aaB14. (b) As we know, threshold wavelength  $(l_{0}) = hc.$  f  $(l_{0}) = hc.$  f  $(1 \oplus a) = hc.$   $(1 \oplus b) = hc.$  f  $(1 \oplus b) = hc.$   $(1 \oplus b) = hc.$  f  $(1 \oplus b) = hc.$   $(1 \oplus b) = hc.$  (1

emit electron from the metal surface. For each wavelength energy incident on the surface per unit time = intensity of each × area of the surface

$$=\frac{3.6'10-3}{3}$$
 (1cm)=1.2'10-7joule

Therefore, energy incident on the surface for each wavelength in 2s

 $E = (1.2 \times 10-7) \times 2 = 2.4 \times 10-7 J$ 

wavelength

Number of photons n1 due to wavelength 4144  ${\rm \AA}$ 

$$n1 = \frac{(2.4 \, 10^{-7}) (144 \, 10^{-10})}{(6.63 \, 10 \, 34) (10^{8})} = 0.5 \, 10^{12}$$

Number of photons n  $_{\rm 2}\,$  due to the wavelength 4972 Å

$$n_{2} = \frac{(2.4 \ 10^{-7})(972 \ 10^{-10})}{(6.63 \ 10^{-34})(10^{8})} = 0.572' \ 10^{12}$$

Therefore total number of photoelectrons liberated in 2s,

$$N = n_1 + n_2$$
  
= 0.5 10 <sup>12</sup> 0.575 '10<sup>12</sup>  
= 1.075 10 <sup>12</sup>

15. (c) The net force acting on the gate element of width dy at a depth y from the surface of the fluid, is

$$= \frac{2}{2} \frac{m^{2}}{2} - \frac{1}{2} \frac{(1.6 ')^{2}}{m}$$

$$= \frac{1}{2} \frac{(1.6 ')^{2}}{(9.1 \cdot 10^{-31})}$$

$$= 2.97 \times 10^{15} \text{ J}$$

$$= \frac{2.97 \cdot 10^{-15}}{1.6 \cdot 10^{-19}} = 18.36 \text{ keV}$$

Energy of the incident photon  $\frac{=hc}{I}$ 

$$=\frac{12.}{4}=24.8$$
keV

16. (b)

Th**erg**fore, Binding energy = 24.8 – 18.6 = 6.2, keV

17. (c) Given : Voltage across the collector V0 = 2  $W_{VC}$  Busetor resistance,  $R = 2 \times 103$ resistance  $R_{\overline{B}}$  1 × 10 W; Input signal voltage, Vi = ?



V0 = ICRC = 2  

$$P_{L_{c}} = \frac{2}{2'103} = 10-3A$$
  
Current gain a =  $\frac{IC}{IB} = 100$   
 $P_{B} = \frac{I_{c}}{100} = \frac{10-3}{100} = 10^{-5}A$   
 $P_{V \models RI^{BB}} = V_{i} = 1 \times 10^{3} \times 10^{-5}$   
 $V \models 10-2V = V_{i} = 10 \text{ mV}$   
Initial potential energy of the system  
 $1 = \frac{6q^{2}}{2} = \frac{q^{2}}{2} = \frac{q^{2}}{2} = \frac{10}{2}$ 

18. (a)

$$= \frac{1}{4_{pe^{0}}} \frac{e^{q^{2}}}{e^{a}} + \frac{q^{2}}{a} + \frac{q^{2}\dot{u}}{a} \frac{1}{\dot{u}\dot{u}} = \frac{1}{4_{pe^{0}}} \frac{e^{3}q^{2}\ddot{o}}{\dot{c}} \frac{\dot{c}}{a} \frac{\dot{c}}{\phi} \frac{\dot{c}}{\dot{c}} \frac{\dot{c}}{a} \frac{\dot{c}}{\dot{c}} \frac{\dot{c}$$

Let charge at A is moved to mid-point O, Then final potential energy of thhe system

$$Uf = \frac{1}{4^{pe0}} \overset{\acute{e}}{\underset{e}{\partial}} \overset{2q^2}{(a / 2^2)} + \frac{q^2 \dot{u}}{2^3 a \dot{u}}$$
$$= 5' \frac{1}{4^{pe_0}} \overset{2q^2}{\underset{e}{\partial}} \overset{2q^2}{\underset{e}{\partial}} + \frac{q^2 \dot{u}}{2^3 a \dot{u}}$$

Work done = U & Ui = 18 × 10<sup>7</sup>J Also, energy supplied per sec = 1000 J (given)

Time required to move one of the mid-point of the line joining the other two

$$t = \frac{18'107}{1000} = 18'10s^{4} = 50h$$

19. (d) Let there are n1 moles of hydrogen and n2 moles of helium in the given mixture. As Pv = nRT

Then the pressure of the mixture

$$P = \frac{n1RT}{V} + \frac{n2RT}{V} = (n_1 + n_2) \frac{RT}{V}$$
  
P  
2'101.3'103= (n\_1 + n\_2)' (8.3 300)  
or,  
(0.1 + 0.2)' (10 - 3)

$$(n_1 + n_2) = \frac{2^{101.3} 10^{2} 20^{10-3}}{(8.3(300))}$$

or, n1 + n2 = 1.62 ... (1) The mass of the mixture is (in grams)

n1 × 2 + n2 × 4 = 5  
(n1 
$$\neq$$
 2n2) = 2.5 ....(2)  
Solving the eqns. (1) and (2), we get  
n1 = 0.74 and n2 = 0.88  
Hence,  $\frac{\text{mH}}{\text{mHe}} = \frac{0.74 \cdot 2}{0.88 \cdot 4} = \frac{1.48 = 2}{3.52}$   
(c) Resistance of wire () = rl  
*R i*  
If wire is bent in the middle then  
 $l \notin \frac{l}{2}, A \notin = 2A$   
 $\land$  New resistance,  $R \notin = r \frac{l \notin}{A \notin} = \frac{r \frac{l}{2}}{2A} = \frac{rl}{4A} = \frac{R}{4}$ .  
(b) The path difference when transparent sheet  
is introduced  $Dx = (m-1)t$ 

20.

21.

Þ

is introduced Dx = (m– 1)t If the central maxima occupies position of nth fringe, then (m– 1)t = n l = d sin q

sin q = 
$$\frac{(m-1)t}{d} = \frac{(1.17-1)^{7}1.510^{-7}}{3^{1}10^{7}} = 0.085$$
  
Therefore, angular position of central maxima  
q = sin<sup>-1</sup> (0.085) =4.88° » 4.9

For small angles, sin q » q » tan q

$$b \quad \tan q = \frac{y}{D}$$

$$\frac{y}{D} = \frac{(m-1)t}{d} \quad b \quad y = \frac{D(m-1)t}{d}$$
From exception

22. (c) From question, Horizontal velocity (initial),  $u_x = \frac{40}{2} = 20 \text{ m/s}$ Vertical velocity (initial),  $50 = uyt + \frac{1}{2}gt2$   $puy \times 2 + \frac{1}{2}(-10) \times 4$ or, 50 = 2uy - 20or,  $uy = \frac{70}{2} = 35 \text{ m/s}$ herefore a gradient of the second second

Angle q = 
$$\tan_0^2 \frac{7}{4}$$

23. (a) Newton's law of viscosity,  $F = hA \frac{dv}{dy}$ 

Stress = 
$$\frac{F}{A} = h \underbrace{\overset{\partial}{\partial}}_{\partial y \overset{\partial}{\partial} = hk}^{\partial Q} \frac{49}{a^2} - \frac{3y^2 \ddot{O}}{a^3 \overset{\partial}{\phi}}$$
  
At  $y = , astress = hk \underbrace{\overset{\partial}{\partial}}_{\partial a}^{\partial Q} - \frac{3\ddot{O}}{a^3} \overset{\partial}{\phi}$ 

24. (b) According to energy conservation pr in cipl e,

If, x1 is maximum elongation in the spring when the particle is in its lowest extreme position. Then,

27.

28.

mgh = 
$$\frac{1}{2}$$
kx<sub>1</sub><sup>2</sup> - mgx1  
 $\frac{1}{2}$   
 $\frac{1}{2}$  - kx21-mgx1-mgh=0

1

or, 
$$1 - \frac{2mg}{k} \times 1 - \frac{2mg}{k} \cdot h = 0$$
  
 $\sum_{k=\pm}^{k} \frac{1}{\sqrt{e}} \frac{\sqrt{e}}{k} \frac{2mg}{\dot{e}} + 4 \cdot \frac{2mg}{k} \dot{h} \dot{h}$ 

Amplitude A =  $X_{f}^{4}$  – X0 (elongation in spring for equilibrium position)

$$A = \frac{mg}{k} \sqrt[\text{@}]{e} \frac{\ddot{o}}{c1+2hk}$$

25. (c) Let the initial mass of uranium be MO Final mass of uranium after time t,  $M = \frac{3}{4}M_0$ 

> According to the law of radioactive disintegration.

$$\frac{M}{M0} = \frac{1}{2} \frac{1}{2} \frac{c}{2} \frac{c}{2} \frac{t}{M} \Rightarrow \frac{M0}{M} = (2)t/T$$

$$\frac{W}{M0} = \frac{1}{2} \frac{W}{M} = (2)t/T$$

$$\frac{W}{M0} = \frac{W}{M} = \frac{$$

$$=\frac{\text{Tlog1(0 1.333)}}{\log_{10}(2)} = 4.5 \cdot 10\% \frac{0.1249\ddot{0}}{0.3010\dot{a}}$$

$$= 1.867 \times 109 \text{ yr.}$$

P I eff = 
$$\stackrel{e}{e} \stackrel{v}{Q} \stackrel{T}{Q} \stackrel{T}{Idt} \stackrel{v}{2} \stackrel{u}{u} \stackrel{u}{u}$$
  
=  $e \stackrel{1}{e} \stackrel{T}{Q} \stackrel{v}{Q} \stackrel{T}{dt} \stackrel{u}{u}$   
=  $e \stackrel{1}{e} \stackrel{T}{Q} \stackrel{v}{Q} \stackrel{t}{dt} \stackrel{u}{u}$   
=  $e \stackrel{1}{e} \stackrel{T}{Q} \stackrel{v}{Q} \stackrel{t}{dt} \stackrel{t}{dt} \stackrel{u}{dt} \stackrel{t}{dt} \stackrel{t$ 

Moment of inertia, I = 
$$10c$$
  
 $c$   
 $c$   
 $\dot{c}$   
 $\dot{e}$   
 $\dot{a}$   
 $\dot{3}$   
 $\dot{+}$ ø

29. (b) For 2nd line of Balmer series in hydrogen spectrum

$$\frac{1}{t} = R(1) \quad \frac{\cancel{2}}{\cancel{2}} = \frac{1}{\cancel{2}} = \frac{3}{\cancel{4}} = \frac{3}{\cancel{4}} R$$

For Li2+  $\dot{\underbrace{e}_{l}^{i}}_{e}$  = R'9  $\begin{array}{c} \underbrace{\approx 1}_{e}_{X}^{2} \\ \underbrace{e}_{X}^{i} \end{array}$   $\begin{array}{c} 1 \\ \underbrace{2}_{e} \\ 12^{2} \\ \underbrace{i}_{e} \\ 16 \\ \underbrace{i}_{u}^{i} \end{array}$ which is satisfied by n = 12  $\overset{\circ}{}$  n = 6.

30. (c) When a charge particle is allowed to move in a uniform magnetic field, then it describes spiral or circular path

Centripetal force, 
$$\frac{mv^2}{R} = qvB$$
 \  
 $v = \underbrace{eeqB}_{em} R \frac{\ddot{o}}{\dot{a}}$   
Hence,  $\sqrt{\frac{2qV}{m}} = \underbrace{eeqB}_{em} \overset{\ddot{o}}{\dot{b}} R \stackrel{\acute{e}}{\underline{e}} V = \sqrt{\frac{2qV}{m}} \overset{\dot{v}}{\dot{u}}$   
 $P R = \underbrace{eeqmV}_{q} \overset{\ddot{o}^{1/2}}{\dot{a}} \cdot \frac{1}{B}$   
or, m  $\mu$  R2  
[Q V, q and B are constant]

or, 
$$\frac{m1}{m2} \approx \frac{R\ddot{o}^2}{R\dot{z}\dot{\phi}}$$

 31. (b) Water wets glass and so the angle of contact is zero.
 For full rise, neglecting the small mass in the meniscus

$$_{rrg}^{2prT = p}$$
r2hrgÞh= $\frac{2}{rrg}$ [Qwater wets glass, q=0°]  
= 2'0.07

As the tube is only 2 cm above the water and so, water will rise by 2 cm and meet the tube at an angle such that,

$$P = 2T \cos q = h c rg$$

Þ cos

$$q = \frac{h r g}{2T}$$
$$= 2^{10^{-2}} 0.25 10^{-3} 1000^{-2}$$

2 ´ 0.07

The liquid will meet the tube at an angle, q @ 70°

9.8

32. (d) Given : Initial velocity 
$$u = 20\sqrt{2}$$
 m/s;  
angle of projection q = 45°

Therefore horizontal and vertical components of initial velocity are

 $ux = 20\sqrt{2}\cos 45^\circ = 20 \text{ m/s}$ 

and uy=202sih45°=20m/s After 1s, horizontal component remains unchanged while the vertical component becomes

vy = uy – gt

Due to explosion, one part comes to rest. Hence, from the conservation of linear momentum, vertical component of second part will become v cy=20m/s.

Therefore, maximum height attained by the second part will be

=  
Using, h ut 
$$\frac{+1}{2}at2$$
  
P  $h_1 = (201') - \frac{1}{2} 10'(1)^2 15 m$   
 $a = g = 10 m/s2$   
 $h_2 = \frac{\sqrt{q^2}}{2g} = \frac{(20)2}{2'10} = 20m$   
H = 20 + 15 = 35 m

33. (c) Let the man starts crossing the road at an angle q as shown in figure. For safe crossing the condition is that the man must cross the road by the time the truck describes the distance 4 + AC or 4 + 2cotq.

From equation (i),

$$v\min = \frac{8}{2\frac{2}{c}\frac{2}{c}\frac{2}{\sqrt{5}}\frac{2}{0}\frac{2}{\sqrt{5}}\frac{2}{0}\frac{1}{\sqrt{5}}} = \frac{8}{\sqrt{5}} = 3.57 \text{ m/s}$$

34. (b) Let speed of neutron before collision = V  
Speed of neutron after collision = V1  
Speed of proton or hydrogen atom after  
collision = V2  
Energy of excitation = DE  
From the law of conservation of linear  
momentum,  

$$mv = mv1 + mv2 \dots (1)$$
  
And for law of conservation of energy,  
 $\frac{1}{2} \frac{m^2 + 1}{2} \frac{m^2 + 1}{2} \frac{mv22}{2} \dots (2)$   
From squaring eq. (i), we get  
 $v2 = v21 + v22 \frac{2DE}{m} \dots (4)$   
From eqn (3) & (4)  
 $\langle 2v1v2 = \frac{2DE}{m}$   
 $\langle (v1-v 2)^p = (v_1^+ v2)^p - 4vy_2 = v2 - \frac{4DE}{m}$   
As,  $v1 - v2$  must be real,  $v^2 - \frac{4DE^{30}}{m}$   
 $p = \frac{1}{2} mv2^{-3} 2DE$ 

The minimum energy that can be absorbed by the hydrogen atom in the ground state to go into the excited state is 10.2 eV. Therefore, the maximum kinetic energy needed is

$$\frac{1}{2}$$
 mv<sup>2</sup><sub>min</sub> = 2 10.2 = 20.4 eV

35. (a) From, figure,

$$A_{R} = \sqrt{\left(\sqrt{3}\right)^{2} + \binom{21}{2}} = 2 \sqrt{3}$$

$$q = \tan \frac{1 \approx \sqrt{3} \ddot{0}}{\overset{\circ}{\xi} 1 \overset{\circ}{\theta} p} = \frac{1}{3}$$

$$y = 2\sin \frac{2}{\xi w t} + \frac{p \ddot{0}}{4} = \frac{1}{3}$$

$$\frac{d^{2}y}{dt^{2}} = a = -\frac{w^{2}}{sn} \frac{g}{\xi} \frac{g}{w} t + \frac{g}{\theta} \frac{g}{\theta}$$

$$a_{max} = -\frac{w^{2}}{s} = g$$
For which mass just breaks off the plank
$$w = \sqrt{g/2}$$
This will be happen for the first time when
$$wt + \frac{g}{y} = \frac{g}{2}$$

$$t = \frac{g}{6w} = \frac{g}{6}\sqrt{\frac{2}{g}}$$
36. (b) From the figure.
The net charge shared between the two capacitors
$$Q t = Q^{2} - Q^{2} = 4CV - CV = 3CV$$

$$\frac{g}{y} + \frac{g}{y} = \frac{g}{2}$$

$$\frac{g}{y} + \frac{g}{y} = \frac{g}{2}$$

The two capacitors will have some potential, say V¢.

The net capacitance of the parallel combination of the two capacitors

C¢=C1+C2=C+2C+3C

The potential of the capacitors

$$V \notin = \frac{Q \notin}{C \notin} = \frac{3CV}{3C} = V$$

The electrostatic energy of the capacitors

$$E = \frac{1}{2} C V = \frac{1}{2} (3C) V = \frac{3}{2} C V$$

$$Z = \sqrt{\frac{R^2}{8}} \frac{+2}{8} \frac{+2}{W} L - \frac{1}{W} \frac{\ddot{o}^2}{\dot{c}}$$
$$= \sqrt{\frac{102 + 22000510}{\dot{e}} - \frac{3}{2000'50'10^{-6}}} \frac{1}{2000'50'10^{-6}} \frac{\ddot{o}^2}{\dot{c}}$$
$$= 10^{W}$$
$$i = \frac{V_0}{Z} = \frac{20}{10} = 2A.$$

38. (b) The heat produced is given by

$$H = \frac{V^2}{R}$$
 and  $R = \frac{r_{l}}{pr_{l}^2}$ 

$$H = V^{2} \overleftarrow{\underbrace{e}_{ert}}^{epr} \overrightarrow{o}$$
  
or 
$$H = \overleftarrow{\underbrace{p}_{ert}}^{evr} \overleftarrow{i}_{ert}^{2}$$
  
$$\overleftarrow{b}_{ert}^{2} \overrightarrow{o}_{ert}^{2}$$

Thus heat (H) is doubled if both length (l)

√g

39. (b)

and radius (r) are doubled.

 $f\mu \sqrt{mg}$  or  $f\mu$ In water, fw=0.8fair

As we know, frequency

$$\frac{g^{\ddagger}}{g}(0.8) = 0.64$$

$$\Rightarrow 1 - \frac{r}{rm} = 0.64$$

$$\Rightarrow \frac{rW}{rm} = 0.36 \dots(1)$$
In liquid,  

$$r \frac{g^{\ddagger}}{g} = (0.6)2 = 0.36$$

$$1 - \frac{1}{rm} = 0.36\frac{r}{rm} = 0.64 \dots(2)$$
From eq. (1) and (2)  

$$\frac{rl}{rn} = \frac{0.64}{0.36} \setminus rl = 1.77$$

40. (a) The wire carries a current I in the negative z-direction. We have to consider the

> magnetic vector field Bat (x, y) in the z = 0pl an e.



Maugrnetic field is perpendicular to OP.  $B=B\sin i$ q - B cosqi

sin q = 
$$\frac{y}{r}$$
, cos q =  $\frac{x}{r}$  B =  $\frac{m_0 I}{2pr}$   
 $\downarrow u r = \frac{m_0 I}{2pr^2} (\hat{y} \hat{f} x \hat{j})$   
or  $m_0 y (-x \hat{j})$   
 $\frac{2p I}{r} (x + y)$ .

41. (c) NO pollutant is the main product of automobiles exhaust. The high concentration of hydrocarbon 42. (c) pollutants in atmosphere causes cancer. 43. (b) Electronic configuration of element with atomic number 118 will be [Rn]5f146d10 7s27p6. Since its elctronic configuration in the outer most orbit (ns2np6) resemble with that of inert or noble gases, therefore it will 44. (c) be noble gas element. The third law helps to calculate the absolute entropies of pure substances at different temperature. The entropy of the substance at different temperature. T may be calculated by the measurement of heat capacity change

PART - II: CHEMISTRY

$$S_{T} - S_{0} = DS = 0$$

Where ST = Entropy at T K S0= Entropy at OK

Λ

= Cp.logeT

45

46

48.

49.

= 2.303Cp.logT

- (d CoCl3.5NH3.H2O is pink in colour
- ) Cobalt is present in vitamin B12.
- Cobalt (60) isotope is used in the treatment (b of cancer.
- PMMA is used in bullet proof glass (þ)
  - ClO-4<ClO-3<ClO-2<ClO- is the correct (a) increasing order of Bronsted base. With increase in the number of oxygen atoms in the conjugate bases, the delocalisation of the p bond becomes more and more extended. This results in decrease in the electron density. Consequently basicity also decreases.
- Due to dipole-dipole interaction the boiling 50. (a) point of alkyl halide is higher as compared to corresponding alkanes.
- Complex compounds contains two different 51. (c) metallic elements but give test only for one of them. Because complex ions such as [Fe

(CN)]4-6of K4 [Fe (CN)6], do not dissociate into Fe2+ and CN- ions.

 52. (b) Primary amines (aromatic or aliphatic) on 62. warming with chloroform and alcoholic KOH, gives carbylamine having offensive smell. This reaction is called carbylamine reaction.

$$\underbrace{\bigcirc}^{\text{NH}_2} + \text{CHCl } 3 + 3\text{KOH} \xrightarrow{D} \underbrace{\bigcirc}^{\text{N} = \text{C}} + 3\text{KCl} + 3\text{H} 20$$

- sublimation, a solid is converted directly into gaseous state on heating without passing through liquid phase.
- 55. (b) Zeise's salt is common name of K[Pt CB(h=C2H4)]
- 56. (c) CaCl2 is produced as a by product in solvay ammonia process.
  - (i) NaCl + CO2 + NH3 + H2O

<sup>3</sup>/<sub>4</sub><sup>3</sup>/<sub>4</sub><sup>®</sup>NaHCO3 + NH4Cl

(ii) CaCO3 <sup>3</sup>/<sub>4</sub><sup>3</sup>/<sub>4</sub><sup>®</sup>CO2 + CaO

(iii)2NH2Cl + CaO <sup>3</sup>/<sub>4</sub><sup>3</sup>/<sub>4</sub><sup>®</sup>2NH3 + CaCl <sub>2</sub> + H2O Byproduct

- 57. (b) Semiconductor materials like Si and Ge are usually purified by zone refining. Zone refining is based on the principle of fractional crystallisation i.e. difference in solubilities of impurities in solid and molten states of metal, so that the zones of impurities are formed and finally removed.
- 58. (c) Order of basic character is NH3 > PH3 > AsH3 > SbH3. Basic-character decreases down the group from N to Bi due to increase
- 59. (c) in atomic size. Normal glass is calcium alkali silicate glass made by fusing the alkali metal carbonate,

(c) Exa = 1018(b) More the oxidation state of the central

60

- . (b) More the oxidation state of the central 70
  - atom (metal) more is its acidity. Hence SeO2 (0. S. of Se = +4) is acidic. Further for a given O.S., the basic character of the oxides increases with the increasing size of the central atom. Thus Al2O3 and Sb2O3 are amphoteric and Bi2O3 is basic.

 (b) BF3 does not follow octate rule because central atom, boron lacks an electron pair. Thus, it also acts as Lewis acid.



- 63. (a) According to Le-Chatelier's principle increase in temperature favours the endothermic reaction while decrease in temperature favour the exothermic reaction. Increase in pressure shifts the equilibrium
- 64. (a) in that side in which number of gaseous Efficiency of fuel cell is:  $h = \frac{hFE}{DH} (100)$
- 65. (b) The mass of the substance deposited when one Faraday of charge is passed through its solution is equal to gram equivalent weight. Unit of rate constant for
- 66. (a) second order reaction is L mol-1 sec-1.
- 67. (b) For first order reaction [A] = [A]<sub>t</sub>-kt \ The concentration of reactants will exponentially decreases with time.
  - (a) In P4 molecule, the four sp3-hybridised phosphorous atoms lie at the corners of a regular tetrahedron with DPPP = 60°.

In S8 molecule S-S-S angle is 107° rings.



- (a) 40 elements are present in d-block.
- (a) EDTA is hexadentate ligand

69



- 71. (a) Am shows maximum number of oxidation states, + 3, + 4, + 5, + 6
- 72. (a) Fe3+ ion can be detected by K4[Fe(CN)6]  $4Fe3^+ + 3K_4 \not\in Fe(CN) \not\models$

- 73. (d) DG = D TS; D is positive for a reaction to be non-spontaneous when DH is positive and DS is negative.
- 74. (a) This method is known as Clark's process. In this method temporary hardness is 80. removed by adding lime water or milk of lime.

Ca (OH) 2 + Ca(HCO)<sub>3 2</sub> 
$$\frac{3}{434^{\circ}}$$
 2CaCO3 - +2H2O

· (b

)

1:5

1:20

Structures of Xenon fluorides

Xe F 2 :Hybindazhos p 3 d Xe

Linear

Square planar

XeF6 : Hybribisation spd<sup>8</sup> <sup>3</sup> F

Pentagonal pyramidal or distorted octahedral Calcium silicophosphate (a mixture of

78. (c) mixture of Ca3(PO4)2 & Ca2SiO4) is called Thomas
79. (a) alog

slag. The sequence of bases in mRNA are read in a serial order in groups of three at a

#### time.

Each<sub>ific</sub>triplet of nucleotides (having a sequence of bases) in known as codon. Each codon specifies one amino acid.

hece, cle arly NH+4ion contains all three types of bonds.

#### PART - III (A): ENGLISH PROFICIENCY

alternative.

- 81 (c) 'Immutable' means 'unchangeable'. So, option (c) is correct choice. 'ignominious'
  . (a) means 'shameful'. So, option (a) is correct choice. 'callous' means 'showing
  82 (c) or having an insensitive and cruel disregard for others'. So, option (c) is
  - correct choice. Option (d) institutional as the word means relating to principles (a) esp. of law, so legally also every human has rights of freedom and equality. 86. (c) Immortal means living forever, never dying or decaying. So, perishable is the (a) correct opposite to it. Opposed is the (b correct answer of this. To patronise means favour or pat on the back. Tactful means having or showing skill and (c) senstivity in dealing with others or with defficult essues. So, in cautious is the (a) correct opposite of factful. Atheist is the best alternative. 'Epicure' is the best



84. 83

85

87

88

(c) (c)



\ Age of new man = 20 + 16 = 36 yr So, the new man is 16yr older to the man by whom the new man is replaced.

104. (d) The relation is as following:



It is clearly shown that Shikha is the mother of Ankit. Since Arun and Suresh

interchange places, so Arun's new position 105. (b) (13th from left) is the same as Suresh's earlier position (6th from right). So, number of children in the queue = (12 + 1)+ 5) = 18.Now, Suresh's new position is the same as

> Arun's earlier position fifth from left. Therefore Suresh's position from the right =(18-4)=14th.



Difference of ages = 8(x + 2) - 8x



$$= \frac{1}{2} \frac{\acute{e}}{\acute{e}} + \frac{3}{22} + \frac{32}{24} + \frac{33}{26} + ..., \overset{\acute{u}}{\acute{u}}$$
  
Since  $\frac{\acute{e}}{\acute{e}} + \frac{3}{22} + \frac{32}{24} + ... - ... - \frac{\acute{e}}{3}$  is a G.P.  
therfore bysum of infinite G.P, we have  
$$= \frac{1}{2} \frac{\acute{e}}{\acute{e}} - \frac{1}{3} \frac{\acute{u}}{\acute{u}} = \frac{1}{2} \frac{\acute{e}}{\acute{e}} - \frac{1}{3} \frac{\acute{e}}{\acute{u}} = \frac{1}{3} \frac{\acute{e}}{\acute{u}} - \frac{3}{4} \frac{\acute{u}}{\acute{u}} = 2$$
  
(Given expression  
 $= -1$   
 $\acute{e}$   $\frac{\acute{e}}{\acute{e}} - \frac{1}{2} \frac{\acute{u}}{\acute{u}} = \frac{1}{3} \frac{\acute{e}}{\acute{e}} - \frac{3}{4} \frac{\acute{u}}{\acute{u}} = 2$   
(H +  $\frac{1}{4} + \frac{1}{4} + \frac{1}{26} + \frac{1}{22} + \frac{1}{24} + \frac{1}{26} + \frac{1}{22} + \frac{1}{22} + \frac{1}{24} + \frac{1}{26} + \frac{1}{26} + \frac{1}{26} + \frac{1}{26} + \frac{1}{26} + \frac{1}{26} + \frac{1}{22} + \frac{1}{26} +$ 

p/3. 111. (b) Let

$$f(x) = \frac{x}{1+x} + \frac{x}{(x+1)(2x+1)} + \frac{x}{(2x+1)(3x+1)} + \dots + \frac{x}{(2x+1)(3x+1)(3x+1)} + \dots + \frac{x}{(2x+1)(3x+1)(3x+1)(3x+1)} + \dots + \frac{x}{(2x+1)(3x+1)(3x+1)(3x+1)(3x+1)} + \dots + \frac{x}{(2x+1)(3x+1)(3x+1)(3x+1)(3x+1)} + \dots + \frac{x}{(2x+1)(3x+1)(3x+1)(3x+1)(3x+1)(3x+1)}$$

 $= \lim_{\substack{n^{\circ} \neq \\ \lim_{x^{\circ} \neq} \\ r=1}} a_{r=1}^{n} \frac{x}{\underline{e}(r-1)x+1\underline{u}(rx+1)}$  $= \lim_{n \stackrel{\otimes}{\mathbb{Y}}} 1 \stackrel{e}{\stackrel{\circ}{\mathbb{E}}} - \frac{1}{nx} \stackrel{\dot{u}}{\mathbb{P}} = 1$ For x = 0, we have f(x) = 0 Thus, we have  $f(\mathbf{x})_{i0, x=0}^{1, x=0}$ Clearly,  $\lim_{x \in \Omega_{-}} f(x) = \lim_{x \in \Omega_{+}} f(x)^{1} f(0)$ So, f(x) is not continuous at x = 0. 112. (c) Since, g is the inverse of function Therefore, g(x) = f - 1(x) $\models f[g(x)] = x$ Þ fog (x=x,forallx Differentiate both side,w.r.tx  $\models \frac{d}{dx} \{ fog(x) \models \frac{d}{dx}(x), forall x \}$  $\Rightarrow \phi f[g(x)] g(x) = 1$ , for all x  $P \sin gx$  g'x = 1, for all x (By defn of f(x)) 1 Þ

$$p g'(x) = \frac{1}{\sin\{g(x)\}}$$

sides from the bag.

E2= Getting a fair coin from the bag

A = Toss results in a head

Given: P(A) = 
$$\frac{31}{42}$$
, P(1) =  $\frac{n}{2n+1}$   
and P(E) =  $\frac{n+1}{2n+1}$   
Then,

$$P(A) = P(E) P(A E1) (E) P(A E)$$

f.

$$p = \frac{3}{1} = \frac{n}{2n+1} \cdot 1 + \frac{n+1}{2+1} \cdot \frac{1}{2}$$

$$q = \frac{3n}{2n+1} + \frac{n+1}{2(2n+1)} + \frac{n}{2(2n+1)}$$

$$p = \frac{3}{1} = \frac{3n+1}{2(2n+1)} + \frac{3}{2(2n+1)} + \frac{3}{2(2n+1$$

Required area = 4 (Area of the shaded region in first quadrant)

 $=4\dot{Q}^{1\sqrt{2}}(y_{1}-y_{2})dx=4\dot{O}^{1\sqrt{2}}\dot{\xi}^{2}\sqrt{1-x^{2}}-x\dot{\ddot{g}}dx$ 

$$= 4\frac{6}{2}\sqrt{1-x^{2}} + \frac{1}{2}\sin^{-1}x - \frac{2\dot{u}1}{2\dot{u}_{0}^{2}}$$

$$= 4\frac{6}{2}\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}} + \frac{1}{2} - \frac{1}{2}\frac{1}{4}\frac{1}{4}$$

$$= \frac{6}{8}\frac{1}{2}\sqrt{2} - \frac{1}{\sqrt{2}} + \frac{1}{2} - \frac{1}{4}\frac{1}{4}\frac{1}{4}$$

$$= \frac{6}{8}\frac{1}{4}\frac{1}{4} + \frac{1}{8} - \frac{1}{2}\frac{1}{8}\frac{1}{4}\frac{1}{4}\frac{1}{8} = \frac{1}{2}Sq \text{ units}$$
116. (c)  $U = \{x : x5 - 6x4 + 11x3 - 6x2 = 0\}$ 
Solving for values of x, we get
$$U = \{0, 1, 2, 3\}$$

$$A = \{x : x2 - 5x + 6 = 0\}$$
Solving for values of x, we get
$$A = \{2, 3\}$$
and  $B = \{x : x2 - 3x + 2 = 0\}$ 
Solving for values of x, we get
$$B = \{2, 1\}$$

$$A \subseteq B = \{2\}$$

$$\langle (A \subseteq B)^{2} = U - (A \subseteq B)$$

$$= \{0, 1, 2, 3\} - \{2\} = \{0, 1, 3\}$$
117. (c)  $\cos^{-1}x - \cos^{-1}\frac{y}{2} = a$ 

$$P \cos^{-1}\frac{e^{x}y}{\sqrt{2}} + \sqrt{(1-x^{2})}\frac{e^{x}}{\sqrt{2}} + \frac{y^{2}}{4}\frac{1}{\frac{x}{2}}} = a$$

$$P \cos^{-1}\frac{e^{x}y}{\sqrt{2}} + \sqrt{(1-x^{2})}\frac{e^{x}}{\sqrt{2}} + \frac{y^{2}}{4}\frac{1}{\frac{x}{2}}} = a$$

$$P \cos^{-1}\frac{e^{x}y}{\sqrt{2}} + \sqrt{(1-x^{2})}\frac{e^{x}}{\sqrt{2}} + \frac{y^{2}}{4}\frac{1}{\frac{x}{2}}} = a$$

$$P \cos^{-1}\frac{e^{x}y}{\sqrt{2}} + \sqrt{(1-x^{2})}\frac{e^{x}}{\sqrt{2}} + \frac{y^{2}}{4}\frac{1}{\sqrt{2}} + \frac{x^{2}}{\sqrt{2}}\frac{1}{\sqrt{2}}\frac$$

 $= a_{0} + a_{1}x + a_{2}x^{2} + a_{3}a^{3} + \dots$   $= a_{1} = a_{3} = a_{5} = \dots = 0$ Hence,  $2a_{1} + 2^{3}a_{3} + 2^{5}a_{5} + \dots = 0$ 119. (d) Let qbe the angle between b and c. Given, b' c =  $\sqrt{15}$  b |b|¢ \$in q =  $\sqrt{15}$  b  $\frac{1}{5}$  sin q =  $\frac{15}{\sqrt{16}}$  c  $\cos q = \sqrt{1 - \frac{15}{16}} = \frac{1}{\sqrt{16}} = \frac{1}{4}$ Now given, b- 2c =  $|a|b - 2c^{2}| = |a|^{2}|$  b  $|b|^{2} + 4|c| - 4$  (b) $e^{|2|}a|^{2}$  b 16 + 4 - |4|b|ccosq = 12 b 20 - 16cos q = 12 b 20 - 16cos q = 12 c  $a_{1}^{2}$  b 16 + 4 - |4|b|cosq = 12 c 20 - 16cos q = 12 c 20 - 16cos q = 12 c  $4 = 1^{2} p |2^{2} - 16 e^{c} cosq = \frac{1}{4} e^{c}$ 

$$=\frac{{}^{10}C4'4!}{4!}=10C4$$

121. (c) Given equation of a line parallel to X-axis is y = k.

Given equation of the curve is  $y = \sqrt{x}$ ,

On solving equation of line with the equation of curve, we get x = k2Thus the intersecting point is (k2, k) It is given that the line y = k intersect the

ɛuatværyænglæ of p/4. This means that the slope of the tangent to

y= 
$$\sqrt{x}$$
 at (k2, k) is tan  $\stackrel{\text{get}}{\stackrel{\bullet}{=}} \frac{p \ddot{o}}{4 \not{o}} = \pm 1$ 

$$\begin{array}{rcl} & \stackrel{\text{\tiny \ensuremath{\text{\tiny \ensuremath{\text{\tiny \elsymbol{math{\text{\tiny elsymbol{math{\text{\tiny math{\text{\tiny math{\text{math{\text{\tiny math}\text{\tiny math{\text{\tiny math{\text{math}\text{\tiny math{\text{\tiny math}\text{\tiny math{\text{\tiny math{\text{math}\text{\tiny math{\text{math}\text{\tiny math{\text{math{\text{math}\text{math{\text{math}\text{\tiny math{\text{math}\text{math{\text{math}\text{math{\text{math}\text{math{\text{math}\text{math{\text{math}\text{\tiny math{\text{math}\text{math{\text{math}\text{math{\text{math}\text{math{\text{math}\text{math{\text{math}\text{math{\text{math}\text{math{\text{math}\text{math{\text{math}\text{math}\text{math{\text{math}\text{math{\text{math}\text{math}\text{math{\text{math}\text{math}\text{math{\text{math}\text{math{\text{math}\text{math{\text{math}\text{math}\text{math{\text{math}\text{math{\text{math}\text{math}\text{math}\text{math{\text{math}\text{math}\text{math}\text{math{\text{math}\text{math}\text{math}\text{math}\text{math{\text{math}}\text{math}\text{math}}\text{math}}\text{math}}\math}}}}}}}}}}}}}}}}}}}}}}}}}}}}} \\ \shn \subber \subber \subber subber subb}\text{math}}\text{math}}\math}}\math}\math}\math}}\math}}\math}\math}\math}}\math}\math}}\math}\\math}}\math}}}}}}}}}}}}}}}}}}}}}}}}}} \\shn \subber \subber subber subber subber subbr}}\math}}\math{}}\math}}\math}}\math}\math}}\math}}\math}}}}}}}}}}}}}}}}}}}}} }} } } \\subber subber subbr} subbr subbr} subbr} subbr} subbr} subbr$$

(a) Let A, B and C be the three angles of DAB and Let a = 10 and b = 9 It is given that the angles are in AP.  $\ 2B = A + C$  on adding B both the sides, we get 3B = A + B + C $\Rightarrow 3B = 180^{\circ} \Rightarrow B = 60^{\circ}$ Now, we know  $\cos B = \frac{a^{2} + c^{2} - b^{2}}{2ac}$  $\Rightarrow \frac{\cos 60^{\circ} = 10^{2} + c^{2} - 9^{2}}{2(10) c}$ 

123. (d) Since, Mean= 
$$\frac{afix_i}{a}$$
 where x are  $afi$ 

observations with frequencies fi, i = 1, 2, .....n The required mean is given by

$$\overline{X} = \frac{0.1 + 1.nC_{1} + 2.nC_{2} + ..... + n.nC_{r}}{1 + nC_{1} + nC_{2} + .... + nC_{n}}$$

$$= \frac{r = 0, r = 0,$$

124. (a) We have 
$$\prod_{n=1}^{r=0} a_{n=1}^{n} (x^{i} + 2)^{2} = 18$$
 and  
 $\frac{1}{n} a_{i=1}^{n} (x^{i} - 2)^{2} = 10$   
 $a_{i=1}^{n} (x_{i} + 2)^{2} = 18n$  and

å

$$\overset{n}{a} (xi - 2)^{2} = 10n$$

$$\overset{i=1}{a} (xi + 2) 2 \overset{n}{\underset{i=1}{a}} (xi - 2) = 28n$$

$$and_{i=1}^{n} (xi + 2) 2 \overset{n}{\underset{i=1}{a}} (xi - 2) = 28n$$

$$\overset{n}{and_{i=1}^{n}} (xi + 2) 2 \overset{n}{\underset{i=1}{a}} (xi - 2) = 8n$$

$$\overset{p}{b} 2 \overset{n}{\underset{i=1}{a}} + 4) 2 \overset{n}{28n} and \overset{n}{\underset{i=1}{2}} \overset{n}{a} 4 \times Bn$$

$$\overset{p}{b} \overset{n}{\underset{i=1}{a}} x^{2i} + 4n = 14n and \overset{n}{\underset{i=1}{a}} \overset{n}{a} xi = n$$

$$\overset{p}{b} \overset{n}{\underset{i=1}{a}} x^{2i} = 10 n and \overset{n}{\underset{i=1}{a}} xi = n$$

$$\overset{s}{b} \overset{n}{\underset{i=1}{a}} x^{2i} = 10 n and \overset{n}{\underset{i=1}{a}} xi = n$$

$$\overset{s}{b} \overset{n}{\underset{i=1}{a}} x^{2i} \overset{n}{\underset{i=1}{a}} (\overset{n}{\underset{i=1}{a}} x^{2i} \overset{n}{\underset{i=1}{a}} (\overset{n}{\underset{i=1}{a}} ) \overset{n}{\underset{i=1}{a}} = 3$$

125. The parametric equations of the parabola  $y^2 = 8x \text{ are } x = 2t \text{ and } y = 4t.$ and the given equation of circle is  $x^2 + y^2 - 2x - 4y = 0$ On putting  $x = 2t^2$  and y = 4t in circle we get  $4t^{4}$ + 16t<sup>2</sup> - 4t<sup>2</sup> - 16t = 0  $\Rightarrow 4t^2 + 12t^2 - 16t = 0$   $\Rightarrow 4t^2 + 12t^2 - 16t = 0$   $\Rightarrow 4t(t^3 + 3t - 4) = 0$   $\Rightarrow t(t - 1)(t^2 + t + 4) = 0$   $\Rightarrow t = 0, t = 1$  $e^{Qt^2} + t + 4^{1} = 0$ 

Thus the coordinates of points of intersection of the circle and the parabola are Q (0, 0) and P(2, 4). Clearly these are diametrically opposite points on the circle.

The coordinates of the focus S of the parabola are (2, 0) which lies on the circle.

\ Area of DPQS = 
$$\frac{1}{2} \times QS \times SP = \frac{1}{2} \times 2 \times 4$$
  
= 4 sq. units.

126. (a) Let f(x) = ex-1 + x - 2check for x = 1 Then, f (1) = e0 + 1 - 2 = 0 So, x = 1 is a real root of the equation f(x) = 0 Let x = a be the other root such that a > 1 or a < 1. Consider the interval 1,a] ora,1].

Clearly f(1) = f(a) = 0By Rolle's theorem fc(x) = 0 has a root in (1, a) or in (a, 1). But fc(x) = ex-1 + 1 > 0, for all x. Thus, which is a contradiction of f(a, 1), Hence, f(x) = 0 has no real root other than 1.

- 127. (c) Constraints will be
  - x11 + x21 + .... + xm1 = b1 x12 + x22 + ..... xm2 = b2 x1n + x2n + .... + xmn = bn x11 + x12 + ... + x1n = b1 x21 + x22 + ... + x2n = b2 xm1 + xm2 + ... + xmn = bn So, total number of constraints = m + n
- 128. (c) Let A ° event that drawn ball is red B ° event that drawn ball is white Then AB and BA are two disjoint cases of the given event.
  \ P (AB + BA) = P(AB) + P (BA)

$$= P(A) P \frac{\partial B}{\partial A} \frac{\ddot{o}}{\dot{c}} + P(B) P \frac{\partial A}{\partial A} \frac{\ddot{o}}{\dot{c}}$$
$$= \frac{3}{6} \cdot \frac{3}{5} + - \cdot \frac{3}{5} = \frac{3}{5}$$

129. (b) We know that, M (adj M) = |M| I Replacing M by adj M, we get adj M [adj (adj M) = det (adj M) I = det (M) M-1 [adj (adj M) = a<sup>2</sup>l

130. (c) Let (x1, y1) be one of the points of contact. Given curve is  $y = \cos x$ 

Now the equation of the tangent at (x1,y1) is

$$y - y_{c} \frac{\frac{\partial edy}{\partial t} \ddot{o}}{\frac{\partial edy}{\partial t}} \dot{\tilde{c}} (x-x_{1})}{\dot{e}}$$

$$y - y_{1} = -\sin x_{1}(0 - x_{1})$$

Since, it is given that equation of tangent passes through origin.

$$0-y1 = -\sin x10-x1$$

 $P = y1 = -x1 \sin x1 \dots (i)$ 

Also, point (x1, y1) lies on  $y = \cos x$ .

 $y1 = \cos x1$ ١ From Eqs. (i), (ii) , we get

$$\sin 2x_1 + \cos 2x_1 = \frac{y_1^2}{x_1^2} + y_{1}^2 = 1$$

Hence, the locus of (x1, y1) is  $x^2 = y^2 + y^2 x^2 \models x^2 y^2 = x^2 - y^2$ 

131. (b) Let m be the slope of the tangent to the cu r ve

 $y = ex \cos x$ .

Then, m 
$$\frac{=dy}{dx} = ex(osx-sinx)$$

Diff. w.r.t 'x'

.

$$\frac{dm}{dx} = ex(COSX \sin x) + ex (inx - \cos x)$$
$$= -2ex \sin x$$

and 
$$\frac{d^2m}{dx^2} = -2ex(sin x + cos x)$$
  
Put  $\frac{dm}{dx} = 0 \Rightarrow sin x = 0 \Rightarrow x = 0, p, 2p$ 

Clearly,  $\frac{d^2m}{dx^2}$  >0 for x = p

Thus, y is minimum at x = pHence the value of a = .p

The equations of given lines can be written 132. (a) as

L1:x-5=
$$\frac{y}{3-a} = \frac{z}{-2}$$
  
L2:x<sup>-a=y=</sup> $\frac{z}{-1}$  $\frac{z}{2-a}$ 

Since, these lines are coplanar.

Therefore, 
$$\begin{vmatrix} 5 - a & 0 - 0 & 0 - 0 \\ 0 & 3 & -a & -2 \\ 0 & -1 & 2 -a \end{vmatrix} = 0$$
  

$$\Rightarrow (5 - a) (3 - a) (2 - a) - 2 = 0$$
  

$$\Rightarrow (5 - a) (6 - 3a - 2a + a2 - 2] = 0$$
  

$$\Rightarrow (5 - a) (a2 - 5a + 4] = 0$$
  

$$\Rightarrow (5 - a) (a - 1)(a - 4) = 0$$
  

$$\Rightarrow a = 1, 4, 5$$

133. (b) 
$$e^{=}\frac{1}{2}$$
. Directrix,  $x = \frac{a}{e} = 4$   
\\a = 4'  $\frac{1}{2} = 2$  \\b =  $2\sqrt{1-\frac{1}{4}} = \sqrt{3}$   
Equation of ellispe is

$$\frac{x^2}{4} + \frac{y^2}{3} = 1 \Rightarrow 3x^2 + 4y^2 = 12$$

134. (d)  $\frac{x}{2} + \frac{2}{x}$  is of the form x  $+ \frac{1}{x}^{3}$  2 and equality holds for x = 1

or 
$$\sqrt{1+x^2} \frac{dy}{d} = ny$$
 or  $\sqrt{1+x^2} y_1 = ny$   
(y1  
 $= \frac{dy}{dx}$ ) X  
Squaring,  $(1+x^2)y^2 = n^2y^2$   
Differentiating,  
 $(1+2x)2y_1y_2 + y^2.2x = n^2.2yy1$   
or  $(1+x^2)y_2 + xy = n^2 y$   
As given,  
 $\approx 1 \ddot{o}$ 

136. (a)

 $A = \lim_{x^{\oplus} ¥} x \sin \frac{a \mathfrak{A}}{e^{*}} \ddot{o} \lim_{x^{\oplus} + x^{\oplus} ¥} \frac{\sin c \overline{c} \overline{x}}{a \mathfrak{A}} \frac{\dot{e}}{c}$ Let  $t = \frac{1}{x}$  when  $x^{\circ}a$ ,  $t^{\circ}$  0  $P A = \lim_{\substack{t \in V \\ t \neq 0 \\ \hat{g} Q}} \frac{sint}{t} = 1$  $\frac{e}{t} \frac{t}{t} \frac{sinx}{t} = 1$ and  $B = \lim_{x \ge 0} x \sin \frac{a \cdot a}{c}$  $P B = \lim_{x \ge 0} x \cdot \lim_{x \ge 0} \sin \frac{\partial \dot{e} I o}{c x \dot{e}}$ PB=0A = 1 and B = 0 is correct \ 137. (b) As given a and b are the roots of the equation  $x^{2} + ax + b = 0$ Þ sum of roots, a + b = -aÞ b = -2a...(1)and product of roots, ab = b ab - b = 0Þ Þ b(a-1) = 0if b = 0 then a = 0if  $b^1 0$  then a = 1 and b = -2so, the expression will be,  $f(x) = x^2 + x - 2$  $= x^{2} + 2.\frac{1}{2}x + \frac{2}{2}\frac{\ddot{o}^{2}}{\dot{a}} - \frac{2}{2}\frac{\ddot{o}^{2}}{\dot{a}} - 2$ 

 $f(x) = \frac{2}{6}x + \frac{1}{2}\frac{1}{6}x - \frac{9}{4}$ So, f (x) will be minimum, if  $\frac{e}{c}x + \frac{1}{2}\frac{o^2}{\dot{e}} = 0$ i.e. when x =  $-\frac{1}{2}$ minimum value of function =  $-\frac{9}{4}$ Þ 138. (d) Let us assume the functions f(x) and g(x)given by f(x) = tanx - x and g(x) = x - sinx, for  $0 < x < \frac{p}{2}$ Now,  $f(x) = \sec 2x - 1$  and  $g(\mathbf{\hat{x}}) = 1 - \cos x$  $\models f(\mathbf{x}) > 0 \text{ and } g(\mathbf{x}) > 0, \quad \begin{array}{c} \mathbf{x} \hat{\mathbf{x}} \\ \mathbf{x} \\ \mathbf{x} \hat{\mathbf{x}} \\ \mathbf{x} \\ \mathbf{x} \hat{\mathbf{x}} \\ \mathbf{x} \\ \mathbf$  $\begin{array}{l} \stackrel{\text{b}}{\qquad} f(x) > f(0) \text{ and } g(x) > g(0) \text{ " } x \stackrel{\hat{I} \approx}{\underset{c}{\text{v}}} 0, \frac{p\ddot{o}}{\underset{c}{\div} 2 \emptyset} \\ \stackrel{\text{b}}{\qquad} tan \ x - x > 0 \text{ and } x - sin \ x^{\hat{e}} > 0, \\ \stackrel{\text{"}\hat{I} \approx c}{\underset{x}{\xrightarrow{e}}} 0, \frac{p\ddot{o}}{\underset{c}{2} \vartheta} \end{array}$  $\tan x > x$  and  $x > \sin x$ ,  $\overset{"}{=} \overset{\text{po}}{\stackrel{\text{e}}{2}}$ Þ  $\sin x < x < \tan x$ , " $\hat{I} \approx c_0, \frac{p\ddot{o}}{\div 2g}$ Þ 139. (a) Put x = sin q and y = sin fcos q + cos f = a (sin q - sin f)₿ cos  $\frac{q+f}{2}\cos\frac{q-f}{2} = 2a\cos\frac{q+f}{2}\sin\frac{q-f}{2}$  $\oint \cot \frac{q-f}{2} = a \not p q - f = 2 \cot -1 a$ interpretation intDifferentiate  $\frac{1}{\sqrt{1 - x^2}} - \frac{1}{\sqrt{1 - y^2}} \frac{dy}{dx} = 0$ so the degree is one 140. (b) Let f(x) = ax3 + bx2 + cx + dPut x = 0 and x = 1

Then, we get f(0) = -1 and f(1) = 0Þ d = -1 and a + b + c + d = 0a + b + c = 1 Þ ...(i) T It is given that x = 0 is a stationary point of ٢ f(x), but it is not a point of extremum. Therefore,  $f\phi(0) = 0 = f\phi\phi(0) a \mu d f\phi\phi\phi(0)$ Now, f(x) = ax3 + bx2 + cx + dfcc(x) = 6ax + 2b and fccc(x) $fc = 0, fcc(0)=0 \text{ and } fccc(0)=0^{1}0$  $P c = 0, b = 0 and a^{1} 0$ From Eqs. (i) and (ii), we get \ a = 1, b = c = 0 and d = -1Put these values in f(x)we get f(x) = x3 - 1Hence,  $\dot{O}_{x^{3}}^{\frac{f}{3}} = \dot{O}_{x^{3}}^{\frac{3}{2}} = \dot{O}_{x^{3}}^{\frac{3}{2}} = \dot{O}_{x^{3}}^{\frac{3}{2}} = \dot{O}_{x^{3}}^{\frac{1}{2}} = \dot{O}_{x^{3}}$ 146. (b) 141. (b)  $f(x = \frac{\sin^{-1}(x-3)}{\sqrt{9-x^2}}$  is defined if (i)-1£x-3£1Þ2£x£4 and (ii) 9-x2>0Þ-3<x<3 Taking common solution of (i) and (ii), we get 2£x<3 Domain = [2, 3]142. (a) The equations of the lines are p1x + q1y - 1 = 0...(i) p2x + q2y - 1 = 0...(ii) and p3x + q3y - 1 = 0...(iii) As they are concurrent,  $\begin{vmatrix} p_1 & q_1 & -1 \\ p_2 & q_2 & -1 \\ p_3 & q_3 & -1 \end{vmatrix} = 0 \quad P \begin{vmatrix} p_1 & q_1 & 1 \\ p_2 & q_2 & 1 \\ p_3 & q_3 & 1 \end{vmatrix} = 0$ Given n = 4 and P(X = 0) =  $\frac{16}{81}$ This is also the condition for the points 148. (b) (p1, q1), (p2, q2) and (p3, q3) to be collinear. 143. (c) Let AB be the chord of length  $\sqrt{2}$  2. Let O be the centre of the circle and let OC be the perpendicular from O on AB.

Then, AC = BC = 
$$\frac{\sqrt{2}}{2} = \frac{1}{\sqrt{2}}$$
  
in DOBC, we have  
DB = BC cosec 45°  
 $= \frac{1}{\sqrt{2}}, \sqrt{2} = 1$   
Area of the circle = p(OB)2 = p sq units

 $\Lambda$  Area of the circle = p(OB)2 = p sq units 144. (b)  $\cos A = n \cos B$  and  $\sin A = m \sin B$ Squaring and adding, we get  $1 = n2 \cos 2B + m2 \sin 2B$  $P1 = n2 (1 - \sin 2B) + m2\sin 2B$  $(m2 - n2) \sin 2B = 1 - n2$ 145.(a) z1, z2, 0 are vertices of an equilateral triangle, so we have  $z_1^2 + z_2^2 + 0^2 = z_1 z_2 + z_2 0 + 0. z_1$  $P z_1^2 + z_2^2 = z z_2 P z_1^2 + z_2^2 - z_1 z_2^2 = 0$ Obviously, the relation is not reflexive and transitive, but it is symmetric, because  $x^{2} + x^{2} = 2x^{2} 1$ and  $x^2 + y^2 = 1$ ,  $y^2 + z^2 = 1$ Px2 + z2 = 1But  $x^2 + y^2 = 1^{1/2} y^2 + x^2 = 1$ 147. (c) Let *l*, m and n be the direction cosines. Then,  $l = \cos , am = \cos b, n = \cos q$ we have  $l^{2} + m^{2} + n^{2} = 1$  $P \cos 2q + \cos 2b + \cos 2q = 1$  $P 2\cos 2q + 1 - \sin 2b = 1$  $\Rightarrow 2\cos 2q - \sin 2b = 0$  $\Rightarrow$  2cos2q - 3sin2b = 0  $\stackrel{e}{Q}$  sin<sup>2</sup> b = 3sin<sup>2</sup> q(given)  $P \tan 2q = 2/3$  $\int \cos^2 q = \frac{1}{1+\tan 2} = \frac{1}{1+2/3} = \frac{3}{5}$ 

> Let p be the probability of success and q that of failure in a trial.

Then, P(X = 0) = 4C0pQ = 0

$$P = q^{4} = \bigoplus_{e \to 3}^{e \to 3} \frac{\ddot{b}^{0}}{\dot{b}^{0}}$$

$$(Q)_{0} = 1$$

$$P = q = \frac{2}{3} P = \frac{1}{3}$$

$$P(X = 4) = 4C_{Q}4q_{0} = p_{4} = \bigoplus_{e \to 3}^{e \to 1} \frac{\ddot{b}^{0}}{\dot{b}^{0}} = \frac{1}{81}$$

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$$P(X = 4) = 4C_{Q}4q_{0} = \frac{1}{$$

$$f \phi f \phi f h = f \phi(0)$$

$$f f(x) = x f \phi(0) + C$$

$$But f(0) = 0$$

$$C = 0$$

$$Hence, f(x) = x f \phi(0), "x \hat{I}R$$

$$Clearly, f(x) is everywhere continuous and differentiable and f \phi(x) is constant.$$

$$"x \hat{I} R$$

150. (d) Let the coefficients of rth, (r + 1)th, and (r + 2)th terms be in HP.

Then, 
$$\frac{2}{n_{C_r}} \overline{c}_r \frac{1}{n_{C^{-1}}} + \frac{1}{n_{Cr^{+1}}}$$
  
 $r_1 = \frac{r_1}{n_{Cr^{-1}}} - \frac{n_{Cr^{+1}}}{n_{Cr^{+1}}}$   
 $p = 2 = \frac{n - r + 1}{n_{C_r}} + \frac{r + 1}{n_{Cr^{+1}}}$   
 $p = 2 = \frac{n - r + 1}{r} + \frac{r + 1}{n_{Cr^{+1}}}$   
 $p = n_2 - 4nr + 4r_2 + n = 0$   
 $p = (n - 2r)^2 + n = 0$ 

which is not possible for any value for n.