BITSAT 2017 Question Paper with Answer Key

Birla Institute of Technology and Science Admission Test

BITSAT : SOLVED PAPER 2017

(memory based)

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This question paper contains total ۞� questions divided into four parts Part ゲ Physics Q No ۞ to Part ゲ ←hemistry Q No ۞ to Part ゲゲ 꾀序 쟼 nglish Proficien cy Q No ۞ to 黨 序 ogical Reasoning Q No 黨۞ to ۞ �

Part 5 V Mathematics Q No 🎡 to 🎡 🔶

- 꾀II questions are multiple choice questions with four options only one of them is
- · ਯach correct answer awarded □ marks and -☆ for each incorrect answer

5.

7.

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PART - I : PHYSICS

1. What is the minimum energy required to launch a satellite of mass m from the surface of a planet of mass M and radius R in a circular orbit at an altitude of 2R?

5GmM	$1 \qquad 2GmM$
(a) $\frac{360000}{6R}$	(b) $\frac{200001}{3R}$
GmM	GmM

(c)		(b)	Onn
	2R	(u)	2R

- A mercury drop of radius 1 cm is sprayed into 106 drops of equal size. The energy expressed in joule is (surface tension of Mercury is 460 × 10–3 N/m)
 - (a) 0.057 (b) 5.7

(

c)
$$5.7 \times 10-4$$
 (d) $5.7 \times 10-6$



with their curved surface towards each other and the space between them is filled with liquid of refractive index 4/3. Then the combination is convex lens of focal length 70 cm concave lens of focal length 66.6 cm convex lens of focal length 66.6 cm

- 4. A charged particle moves through a magnetic field perpendicular to its direction. Then
 - (a) kinetic energy changes but the momentum is constant

- (b the momentum changes but the kinetic
-) energy is constant
- (c) both momentum and kinetic energy of the
- (d particle are not constant
-) both momentum and kinetic energy of the particle are constant
- After two hours, one-sixteenth of the starting amount of a certain radioactive isotope remained undecayed. The half life (a)there isotope remained undecayed and there isotope remained undecayed and

(a) 0.1 s (b) 0.05 s (c) 0.3 s (d) 0.15 s Two concentric conducting thin spherical shells A, and B having radii_A and $r_{B}((r_{B} > r)_{A})$ re charged to Q and $-Q_{B}(|Q|_{B} > |Q|)$. The electric field along a line passing through the centre is



- 8. A capillary tube of radius R is immersed in water and water rises in it to a height H. Mass of water in the capillary tube is M. If the radius of the tube is doubled, mass of 14 water that will rise in the capillary tube will now be: (b) 2 M (c) M/2(d) 4 M
- A sonometer wire resonates with a given 9. tuning fork forming standing waves with five antinodes between the two bridges when a mass of 9 kg is suspended from the wire. When this mass is replaced by a mass M, the wire resonates with the same tuning fork forming three antinodes for the same positions of the bridges. The value of M is (a) (c)

When 25 kg_{25} kg stal surface (b) 11423 kg_{12} kg by light of

10. wavelengths 400 nm and 250 nm, the maximum

velocities of the photoelectrons ejected are v

2v respectively. The work function of the the tar $Ac \times 106 J$ (b) 1.5 hc $\times 106 J$ (B) - Pfanck@constant.(d)= Veldert & Delight in

11. Timo conducting shells of radius a and b are 16. connected by conducting wire as shown in figure. The capacity of system is :



(a) $4 pe_0 \frac{1}{b-a}$

(b) 4 pe0 (a + b)

(c) zero (d) infinite

- When U235 12. undergoes fission, 0.1% of its original mass is changed into energy. How much energy is released if 1 kg of ₉₂U235indergoes fi ssi on (b) 9 × 1011 J
 - (a) $9 \times 1010 \text{ J}$
 - (c) $9 \times 1012 \text{ J}$ (d) $9 \times 1013 \text{ J}$
- One mole of an ideal gas is taken from state 13. 18. A to state B by three different processes,



(i) ACB (ii) ADB (iii) AEB as shown in the P-V diagram. The heat absorbed by the gas is greater in process (ii) than in (i)

(b) (the dedst in pfocess | di X = 3 YZ2, X andZ have salingein-(isigned (if) capacitance and maghestscin (iii) uttainin (iii) spectively. The dimensions of Y in MKSA sys- tem are : (a) [M-3L-2T-2A-4] (c) [M-3L-2A4T8]

(b) [ML-2](d) [M-3L2A4T4]

15. Two very long, straight, parallel wires carry steady currents I and -I respectively. The distance between the wires is d. At a certain instant of time, a point charge q is at a point equidistant from the two wires, in the plane of the wires. Its instantaneous velocity v is perpendicular to this plane. The magnitude of the force due to the magnetic field acting on the charge at this instant is

$$\frac{m0 lqv}{2pd}$$
(b) $\frac{m0 lqv}{pd}$
(c) $\frac{2m0 lqv}{2m0 lqv}$
(d) 0

Two projectiles A and B thrown with speeds in

Characterized the same heights. If A is thrown at an angle of 45° with the horizontal, the angle of projection of B will be (a) 0° (b) 60° (c) 30° (d) 45°

A meter bridge is set up as shown, to determine an unknown resistance 'X' using a standard 10 17. ohm resistor. The galvanometer shows null point when tapping-key is at 52 cm mark. The end-corrections are 1 cm and 2 cm respectively for the ends A and B. The determined value of ' \check{X} ' is



(a

A dials of radius (a /1141 having a unifohmly distributed change 6 C is placed in the x - y plane with its centre at (-a / 2, 0, 0). A rod of length a carrying a uniformly distributed charge 8 C is placed on the x-axis from x = a/4 to x = 5a / 4. Two point charges -7C and 3 C are placed at (a / 4, -a / 4, 0)and (-3a / 4, 3a / 4, 0), respectively. Consider a cubical surface formed by six surfaces

$$x = \pm a / 2$$
, $y = \pm a / 2$, $z = \pm a / 2$. The electric flux

through this cubical surface is



- 19. A particle of mass m moving in the x direction with speed 2v is hit by another particle of mass 2m moving in the y direction with speed v. If the collision is perfectly inelastic, the percentage loss in the energy during the collision is close to (a) 56% (b) 62% (c) 44% (d) 50%
- 20. A coil is suspended in a uniform magnetic field, with the plane of the coil parallel to the magneti²⁵. lines of force. When a current is passed through the coil it starts oscillating; It is very difficult to stop. But if an aluminium plate is placed near to the coil, it stops. This is due to :
 - (a development of air current when the plate is placed
 - induction of electrical charge on the plate
 - (b shielding of magnetic lines of force as aluminium is a paramagnetic material.
 - (c) electromagnetic induction in the aluminium plate giving rise to electromagnetic
- damping.
 A steel wire of length 'L' at 40°C is suspended from the ceiling and then a mass 'm' is hung from its free end. The wire is cooled down from 40°C to 30°C to regain its original length 'L'. The coefficient of linear thermal expansion of the steel is 10–5 /° C, Young's modulus of steel is 1011 N/m2 and radius of the wire is 1 mm. Assume that L >>diameter of the wire. Then the value of 'm' in kg is nearly

22. On a hypotenuse of a right prism (30° - 60° - 90°) of refractive index 1.50, a drop of liquid 26. is placed as shown in figure. Light is allowed to fall normally on the short face of the prism. In order that the ray of light may get totally reflected, the maximum value of refractive index is : Liquid



- 23. A tuning fork of frequency 392 Hz, resonates with 50 cm length of a string under tension (T). If length of the string is decreased by 2%, keeping the tension constant, the number of beats heard when the string and the tuning fork made to vibrate simultaneously is :
- (a) 4 (b) 6 (c) 8 (d) 12
 24. Hydrogen (H), deuterium (D), singly ionized helium (He+) and doubly ionized lithium (Li++) all have one electron around the nucleus. Consider n = 2 to n = 1 transition. The wavelengths of emil2;d3radia#prespectively. Then approximately :

(a
$$| 1 = 12 = 413 = 914$$

)

)
$$411 = 212 = 213 = 14$$

(b
$$1\frac{1}{1} \equiv \frac{1}{12} \frac{1}{2} = \frac{1}{2} \frac{1}{12} \frac{1}{2} = \frac{2}{13} \frac{1}{2} \frac{2}{13} \frac{1}{2} = \frac{2}{13} \frac{1}{12} \frac{1}$$

The following figure depict a circular motion. The radius of the circle, the period of revolution, the initial position and the sense of revolution are fidicated on the figure.



The simple harmonic motion of the xprojection of the radius vector of the rotating particle P can be shown as :

(a)
$$x(t) = a \cos \frac{a c^2 \rho t}{4} + \frac{\rho \ddot{o}}{4}$$

(b) $x(t) = a \cos \frac{a c^2 \rho t}{4} + \frac{\rho \ddot{o}}{4}$
(c) $x(t) = a \sin \frac{a c^2 \rho t}{4} + \frac{\rho \ddot{o}}{4}$
 $x(t) = a \sin \frac{a c^2 \rho t}{4} + \frac{\rho \ddot{o}}{4}$
 $x(t) = a \cos \frac{a c \rho t}{3} + \frac{\rho}{4}$

There are two sources kept at distances 2l. A large screen is perpendicular to line joining the sources. Number of maximas on the screen in this case is (l = wavelength of light)





27. In the circuit shown in figure th'e current through A body moves in a circular orbit of radius R

- (a) the 3 W resistor is 0.50 A.
- (b) the 3 W resistor is 0.25 A.
- (c) the 4 W resistor is 0.50 A
- (d) the 4 W resistor is 0.25 A.
- 28. A telescope has an objective lens of 10 cm diameter and is situated at a distance of one kilometer from two objects. The minimum distance between these two objects, which can be resolved by the telescope, when the mean wavelength of light is 5000 Å, is of the order of 33.

(a) 5 cm (b) 0.5 m (c) 5 m(d) 5 mm

- 29. During vapourisation
 - change of state from liquid to vapour state I. occurs. II.
 - temperature remains constant.
 - IV. both liquid and vapour states coexist in equilibrium.

specific heat of substance increases.

Correct statements are

- (a) I, II and IV (b) II, III and IV
- (c) I, III and IV (d) I, II and III
- 30. A wire is connected to a battery between the point M and N as shown in the figure (1). The same wire is bent in the form of a square and then connected to the battery between the points M and N as shown in the figure (2). Which of the 34. following quantities increases?



- Heat produced in the wire and resistance (a
 - offered by the wire.
- (b Resistance offered by the wire and current through the wire.
- (c) Heat produced in the wire, resistance offered
- by the wire and current through the wire. (d
- Heat produced in the wire and current through the wire.

under the action of a central force. Potential due to the central force is given by V(r) = kr(k is a positive constant). Period of revolution of the body is pro-portional to :

(a) R1/2 (b) R-1/2 (c) R-3/2 (d) R-5/2

Two equal heavy spheres, each of radius r, 32. are in equilibrium within a smooth cup of radius 3r. The ratio of reaction between the cup and one sphere and that between the two sphere is



2 (b) 3 (c) (d) 4 (a) 1 A long, hollow conducting cylinder is kept coaxially inside another long, hollow conducting cylinder of larger radius. Both the cylinders are initially electrically affeit difference appears between

- the two cylinders when a charge density is given to the inner cylinder. A
- (b) potential difference appears between two cylinders when a charge density is given to the outer cylinder. No potential difference appears between the two
- (c) cylinders when a uniform line charge is kept along the axis of the cylinders. No potential difference appears between the
- (d) two cylinders when same charge density is given to both the cylinders.

A thin but rigid semicircular wire frame of radius r is hinged at O and can rotate in its own vertical plane. A smooth peg P starts from Chealdy works constant speedby lifting the frame upward as shown in figure.



Find the angular velocity w of the frame when its diameter makes an angle of 60° with the vertical $\dot{v}0/r$ (b) v0/2 r(c) 2 v0/r(d) v0r

35. Given that A + B = R and A = B = R. What should be the angle between A and B?

(a) The basicp/magnerizalip/3 curliep for a

36. ferromagnetic material is shown in figure. Then, the value of relative permeability is highest for the point



- 37. Five gas molecules chosen at random are found to have speeds of 500, 600, 700, 800 and 900 m/s:
 - (a The root mean square speed and the
 - (b) average speed are the same.
 - (c) The root mean square speed is 14 m/s higher than the average speed.
 The root mean square speed is 14 m/s lowef¹¹. than the average speed.
 The root mean square speed is Ö14 m/s higher than the average speed.
- 38. What is equivalent capacitance of circuit between points A and B?



A cyclic process ABCD is shown in the figure P₄₄.
 V diagram. Which of the following curves represent the same process





40. In the circuit given below, V(t) is the sinusoidal voltage source, voltage drop XB(t) across the resistance R is



- (a) is half wave rectified
- (b) is full wave rectified
- (c) has the same peak value in the positive and negative half cycles
 (d) has different peak values during positive
- (d) has different peak values during positive and negative half cycle

PART - II : CHEMISTRY

Which of the following can be repeatedly soften on heating?

- (i) Polystyrene (ii) Melamine
- (iii) Polyesters (iv) Polyethylene
- (v) Neoprene
- (a) (\mathbf{q}) and (iii) (b (i) and (iv)
 - (iii), (iv) and (v) (ii) and (iv)
- 42. Which one of the following complexes is an outer orbital complex ?)
 - (a) $[Co(NH_3)6]^{3+}$ (b) $[Mn(CN)6]^{4-}$
 - (c) [Fe(CN)]4- (d) $[Ni(NH3)6]^{2+}$

For the reaction $\mathcal{H}(g) + Br2(g) \otimes 2HBr(g)$, the experimental data suggest, rate = $k\mathcal{H}Br2]^{1/2}$. The molecularity and order of the reaction are respectively

(a)
$$2,\frac{3}{2}$$
 (b) $\frac{3}{2},\frac{3}{2}$ (c) 1, 1 (d) $1,\frac{1}{2}$

Dead burn plaster is

(a)
$$CaSO_{4.22H2O}$$
 (b)MgSO4. 7H2O
(d) $CaSO_{4.22H2O}$ (d) $CaSO_{4.22H2O}$

(c) CaSO (d) CaSO4

- 45. Stronger is oxidising agent, more is (a standard reduction potential of that species
 - (b) the tendency to get it self oxidised the tendency to lose electrons by that
 -) species (G) standard oxidation potential of that species

46. Which of the following relation represents 52. correct relation between standard electrode potential and equilibrium constant?

I.
$$\log K = \frac{nFE^{\circ}}{2.303 \text{ RT}}$$

II. $K = e^{\frac{nFE^{\circ}}{RT}}$
III. $\log K = \frac{2.303 \text{ RT}}{2.303 \text{ RT}}$

 $\log K = 0.4342 \frac{\text{nFE}^{\circ}}{\text{...}}$

Choose the correct statement(s).

- (a) I, II and III are correct
- (b) II and III are correct
- (c) I, II and IV are correct
- (d) I and IV are correct
- 47. Which of the following shows nitrogen with its increasing order of oxidation number?

$$a NO < NO < NO < NO < NO - 3 NH + 4$$

$$(b \quad NH_4^+ < NO_2^- < NO_2^- < NO_3^- < NO_3^$$

$$\frac{\text{NH} + < NO < \text{NO} < \text{NO} < \text{NO} < \text{NO} }{\text{NH} + < \text{NO} < \text{NO} < \text{NO} < \text{NO} < \text{NO} }$$

(c)
$$NH + < NO < NO < NO_2 < NO_2 < NO_3$$

48. Raoult's law becomes a special case of Henry's law when

(a)
$$KH < p_1^{\circ}$$
 (b) $KH = p_1^{\circ}$

(c)
$$K^{11}, P_1$$

49. È⁶ for the cell, Zn | Zn2+ (aq) | | Cu2+ (aq) | Cu5ts
 1.10 V at 25°C. The equilibrium constant for the cell reaction

$$Zn+Cu2+(aq) \longrightarrow Cu+Zn2+(aq)$$

is of the order of

50. Which of the following represents Gay Lussac's law?

III.
$$\frac{P}{T} = \text{constant}$$
 II. $P_1T = \frac{P}{2}T_2$ 1

P1V1 = P2V2

- (a) I, II and III (b) II and III
- (c) I and III (d) I and II

51. For the reaction $CO(g) + \frac{1}{2}O2(g) \otimes CO2(g)$ Which one of the statement is correct at constant T and P?

- (a) DH = DE (b) DH < DE
- (c) DH > DE
- (d) DH is independent of physical state of the reactants

- The energy of an electron in second Bohr orbit of hydrogen atom is : is wrop $44 \times 10-19 \text{ kJ}$ $-5.44 \times 10-19$ J (a) NH (d 53. 3 < PH3 < AsHB - Acidic(b)Li < Be < B < C - IE(c) Al 2O3 < MgO < Na2O < K2O - Bacic(d)Li + < Na + < K + < Cs + - Ionic radius54. Which of the following is not involved in the formation of photochemical smog? (a) Hydrocarbon (b) NO (d) O3 (c) SO 2 55. Which of the following is not present in Portland cemen t? (8) 69321956 (c) Ca 56. Which of the following can form buffer solution? (a) aq.NH 3+NH4OH (b) KOH+HNO3 (d) KI+KOH (c) NaOH+HCl 57. Which of the following complex shows sp3d2 hybridization? (a) [Cr(NO ⅔ ℬ– (a) [Fr(EN)][1-(c) $[CoF_6]_{3-}$ 58. Which has glycosidic linkage? (a) amylopectin (b) amylase (c) cellulose (d) all of these Which of the following represents Schotten-Baumann reaction?
 - (a formation of amides from amines and acid) chlorides/NaOH
 - (b formation of amines from amides and) Li Al H
 - (c) formation of amines from amides and Br
 - In the ford wing structures, which two forms are
 - formataiggent avoid soft an on sinter and H?



- 61. Which of the following shows correct order of 72. bond length?
 - (a $O_2^{\pm} > O_2^{\pm} > O_2^{\pm} > O_2^{\pm} > O_2^{\pm}$
 -) $0^{1} < 0^{2} > 0^{2} < 0^{2}^{2-}$
 - $(b \quad O_2^{+} > O_2^{-} > O_2^{-}) > O_2^{-}$
 - $O_2 > O_2 < O_2 > O_2^{-2}$
- 62. The number of radial nodes of 3s and 2p orbital\$3.
 - (a) 2,0 (b) 0,2 (c) 1,2 (d) 2,2
- 63. If a 25.0 mL sample of sulfuric acid is titrated with 50.0 mL of 0.025 M sodium hydroxide to a phenolphthalein endpoint, what is the 74. molarity of the acid?

(a	0.020	(b)0.100 M
)	Μ	(d)0.050 M

- 64. (Find) Affield of the following compound can have mass fatios of C:H:O as 6:1:24 75.
 (a) HO-(C=O)-OH (b) HO-(C=O)-H
 (c) H-(C=O)-H (d) H 3CO-(C=O)-H
- 65. The number of atoms per unit cell of bcc structure is 76.
- (a) 1 (b) 2 (c) 4 (d) 6 66. Which of these doesn't exist?
 - (a) PH 3 (b) PH5 (c) LuH3 (d) PF5
- 67. Which of these compounds are directional?
 (a) NaCl (b) CO ²
 (c) BaO
 (d) CsCl2
- 68. For a given reaction, DH = 35.5 kJ mol-1 and DS = 83.6 JK-1 mol-1. The reaction is spontaneous at^{7,7}. (Assume that DH and DS do not vary with tempear at ur e) 78.
 - (a) T > 425 K (b) All temperatures
 - (c) T > 298 K (d) T < 425 K
- 69. Specific conductance of 0.1 M HA is 3.75 × 10–4 ohm–1 cm–1. If I¥ (HA) = 250 ohm–1 cm2 mol–1, the dissociation constant ₭ of HA is :
 - (a) $1.0 \times 10{-5}$ (b) $2.25 \times 10{-4}$
 - (c) $2.25 \times 10{-5}$ (d) $2.25 \times 10{-13}$
- 70. The rate of reaction between two reactants A and B decreases by a factor of 4 if the concentration of reactant B is doubled. The order of this reaction with respect to reactant79. B is:

(a) 2 (b) -2 (c) 1 (d) -1

- 71. A compound of molecular formula of C7H16 shows optical isomerism, compound will be 80.
 (a) 2, 3-Dimethylpentane
 - (b) 2,2-Dimethylbutane
 - (c) 3-Methylhexane
 - (d) None of the above

- Which of the following does not contain Plane of symmetry?
- (a trans-1,3 dichloro
-) cyclohexane trans-1,2
- (b dichloro cyclohexane cis-1,2
- dichloro cyclohexane trans-

Cadmilify some of the sector o

- (a) absorbing neutrons
- (b) cooling
- (c) release neutrons
- (d) increase energy

Which reagent converts nitrobenzene to N-phenyl hydroxyamine?

- (a) Zn/HCl (b) H 2O2
- (c) Zn/NH 4Cl (d) LiAlH4

Which of the following can act as both Bronsted acid and Bronsted base?

(a) Na 2CO3 (a)
$$\overline{NH3}$$

(c) HCO –

Identify the structure of water in the gaseous phase.

The correct statement about the compounds A, B, and C

$$\begin{array}{cccc} COOCH_{3} & COOH & COOH \\ H & OH H & OH H & OH \\ H & OH H & OH HO & H is \\ \hline COOH & COOCH_{3} & COOCH_{3} \\ (A) & (B) & (C) \end{array}$$

- (a A and B are identical A
-) and B are diastereomers
- (b A and C are enantiomers
-) A and B are enantiomers

Correct formula of the complex formed in the **b**rown ring test for nitrates is

(a) FeSO. NO
(b)
$$[Fe(H2O)5NO]^+$$

(c) $[Fe(HQ)NO]^+$
(d) $[Fe(HQ)NO]^+$
Which one of the following is an amine hormone?
(a) Thyroxine
(b) Oxypurin
(c) Insuring
(

(c) Insulin (d) Progesterone

(c) Content (d)	PROFICIEN plowing question, ou ne one which best en word. 86 Slow Unclear) writing clearly (b undergoing training) reading widely 86. Famous writers have achieved success by (a using their linguistic resources properly) disciplining their skill
DIRECTIONS (Qs. 82): Choose meaning to the given word.	the word opposite in) waiting for inspiration
(c) Careless (d)	Destructive se Flagrant aj	DIRECTIONS (Qs. 87-88) : In questions below, sentences are given with blanks to be filled in with an appropriate word (s). Four alternatives are suggested
birther birth passage and the passage with passage. Read the passage carefi best answer to each question alternatives.	5 questions in eachol ully and choose theg	 5 as each question. Choose the correct alternative out of the four. 87. China is a big country, in area it is bigger than any other country Russia. (a) accept (b) except
PASSAGE-I To write well you have to be able and logically, and you cannot do think clearly and logically. If you you should train yourself to do it problems and following them thr	this unless you can a cannot do this yet by taking particular	(c) toward (d) off
to a solution, without leaving any avoiding any difficulties that you At first you find clear, step-by-st difficult. You may find that you concentrate. Several unconnecte together. But practice will impr concentrate on a single idea and	ything out and without meet. F ep thought very se r mind is not able toge ed ideas may occur ove your ability to out	Image: Weight the sentences have errors and some are correct.Find out which part of a sentence has an error. If asentence is free from error, mark (d) in your Answer.89.My father gave me (a) / a pair of binocular (b) /90.91.92.93.94.94.95.96.97.98.98.99.99.90.90.91.92.93.94.94.95.96.97.98.98.99.99.90.90.91.92.93.94.94.95.95.96.97.98.98.99.99.99.90.90.91.92.93.94.94.95.95.96.97.
and logically. In order to increase	e your vocabulary should read widely p you find the exact	 (b) / for the trip. (c) / No error. (d) PART - III (B) : LOGICAL REASONIN 91. Which answer figure complete the form in question
Always remember that regular a practice is necessary if you want It is no good waiting until you I before you write. Even with the r inspiration is rare. Someone said nine percent hard work and one	and frequent to learn to write well. have an inspiration nost famous writers, that writing is ninety	figure ? 1. Question figure : ty- ?
 so the sooner you get into the h your-self to write, the better. 83. To write well, a person mus (a) (bleatingdy/ithitadlffituit to writet beavinge anything of 	abit of disciplining t train himself in pitiblein	
 84. (a a good dictionary is no) ideas occur without any 	gically p approach t used	
(b aids to correct writing a) exact usages of words a (c)	are not known	

- (c) (d)



DIRECTIONS (Qs. 95-96): Select a suitable figure from the four alternatives that would complete the figure matrix.

(b) Only II is implicit (c) Both I and II are implicit

(a) Only I is implicit

- (d) Both I and II are not implicit

102. Two statements are given followed by four conclusions, I, II, III and IV. You have to consider the statements to be true, even if they seem to be at variance from commonly known facts. You have to decide which of the given conclusions can definitely be drawn from the given statements. Indicate your answer. Statements :

(A)No cow is a chair

(B) All chairs are tables. Conclusions :

- I. Some tables are
- II. chairs. Some tables
- III. are cows Some chairs
- IV. are cows No table is
- (a) a cow
- (b) Either II or III
- (c) follow
- (d) Either II or IV follow Only I follows

DIRECTIONS (05:1403-104): In questions one/two statements are given, followed by two conclusions I and II. You have to consider the statements to be true, even if they seem to be at variance from commonly

known facts. You have to decide which of the given conclusions, if any follow from the given statement.

103. Statements :

- 1. Temple is a place of worship.
- 2. Church is also a place of worship.

Conclusions :

- I. Hindus and Christians use the same place for worship.
- All churches are temples.
 (a) Naither conclusion Lond
- a) Neither conclusion I and II follows
- (b) Both conclusions I and II follow
- (c) Only conclusion I follows
- (d) Only conclusion II follows

104.Statement :

The human organism grows and develops through stimulation and action.

- I Inert human organism cannot grow and (a) develop.
- (b) Human organisms do not react to
- (c) stimulation and action.
- (d) Neither conclusion I nor II follows Both conclusions I and II follow Only conclusion I follows Only conclusion II follows
- 105.Choose the set of figure which follows the given rule.

Rule: Closed figures gradually become open and open figures gradually become closed.



PART - IV : MATHEMATICS

106. Let f and g be functions from R to R defined as

$$f(x) = \begin{matrix} \frac{1}{7}x^2 + x - 8, x \notin 1 & \frac{1}{7} |x|, x < -3 \\ = i4x + 5, 1 < x \notin 7, g(x) = i0, -3 \notin x < 2 \\ \frac{1}{7} 8x + 3, x > 7 & \frac{1}{7}x^2 + 4, x^3 2 \end{matrix}$$

Then

(a) (fog)(-3) = 8 (b) (fog)(9) = 683

- (c) (gof)(0) = -8 (d) (gof)(6) = 427
- 107. How many different nine digit numbers can be formed from the number 223355888 by rearranging its digits so that the odd digits occupy even positions ?
 - (a) 16 (b) 36 (c) 60 (d) 180

108. If $\overset{a}{\underset{k=1}{\mathbb{R}}} k(k+1)(k-1) = pn4 + qn3 + tn2 + sn$,

where p, q, t and s are constants, then the value of s is equal to

a)
$$-\frac{1}{4}$$
 (b) $-\frac{1}{2}$ (c) $\frac{1}{2}$ (d) $\frac{1}{4}$

109. The length of the semi-latus rectum of an ellipse

is one thrid of its major axis, its eccentricity

would be (a)
$$\sqrt{\frac{2}{3}}$$
 (b) $\sqrt{\frac{2}{3}}$ (c) $\frac{1}{\sqrt{3}}$ (d) $\frac{1}{\sqrt{2}}$

110. If a and b are roots of the equation

$$x^2 + px + \frac{3p}{4} = 0$$
, such that $|a-b| = \sqrt{10}$, then

p belongs to the set :

- (a) $\{2, -5\}$ (b) $\{-3, 2\}$
- (c) $\{-2, 5\}$ (d) $\{3, -5\}$

- 3) + b(3x + 2y 5) = 0, the line of the system situated farthest from the point (4, -3) has the equation y - 15 = 0 (b 7x + y - 8 = 04x + 3y - 7 = 0) 3x - 4y + 1 = 0
- 112. One mapping is selected at random from all mappings of the set S) = $\{1, 2, 3, \dots, n\}$ into itself. The probability that it is one-one is $\frac{3}{2}$. Then

32

- 113. The integer just greater than $(3+\sqrt{5})2n$ is divisible by (n Î N) (a) 2n-1 (b) 2n+1 (d) Not divisible by 2 (c) 2n+2
- 114. The domain of the function 2öü
 - $f(x) = sin 1i log 2c \overset{a}{-} x \div y is$ $\hat{1} \overset{b}{-} \hat{2} \overset{a}{-} \emptyset p$ (a) (c) The marks bbt abred by 60 students in a certain test and biken below (-2, -1) E (d (1, 2)

)

2]

Marks	No. of students	Marks	No. of students
10-20	2	60-70	12
20-30	3	70-80	14
30-40	4	80-90	10
40-50	5	90-100	4
50-60	6		

Median of the above data is

(a)
$$68.33$$
 (b) 70
(c) 68.11 (d) None of these

eiA,eiB,eiC are in A.P. Then the triangle must

be

- (a) right angled (b) isosceles
- (c) equilateral (d) None of these
- 117. An observer on the top of a tree, finds the angle of depression of a car moving towards the tree to be 30°. After 3 minutes this angle becomes 60°. After how much more time, the car will reach the t r ee?
 - (a) $4 \min(b) 4.5 m$ (c) $1.5 \min(d) 2 \min(d)$

- 111. Given the system of straight lines a(2x + y 118). After striking the floor a certain ball rebounds
 - $\frac{4}{5}$ th of its height from which it has fallen. The total distance that the ball travels before coming to rest if it is gently released from a height of 120m is (a) 960 m (b) 1000 m (c) 1080 m (d) Infinite 119. An equilateral triangle is inscribed in the circle $x^2 + y^2 = a^2$ with one of the vertices at (a, 0). What is the equation of the side opposite to this vertex? (a) 2x - a = 0(b) x + a = 0(c) 2x + a = 0(d) 3x - 2a = 0120. The function $f(x) = x - |x - x^2|, -1 \pm x \pm 1$ is continuous on the interval (a) [-1, 1](b) (-1, 1) (d) $(-1, 1) - \{0\}$ (c) $\{-1, 1] - \{0\}$ $121. \frac{\hat{I}_{n}}{(a)} \frac{4n}{n+1} < \frac{(2n)!}{(n!)2}$, then P(n) is true for $n^{3}1(b)$ n > 0 (c) n < 0 (d) $n^{3} 2$ 122. If a system of equation -ax + y + z = 0x - by + z = 0x + y - cz = 0 (a, b, c¹-1) has a non-zero solution then 1 1 (a) If f(x) = xx, then f(x) is increasing in interval: 0 (b) 1 (c) 2 (d) 3 123. $\begin{pmatrix} b \\ d \end{pmatrix} \begin{bmatrix} 0, \frac{1}{e} \end{bmatrix}$ None of these $\{a\} = [0, e]$ 124. If x is real number, then $\frac{x}{x^2 - 5x + 9}$ must lie (a) $\frac{1}{-1}$ and 1 (b) -1 and $\frac{1}{-1}$

(c)
$$-11$$
 and 1 (d) $-\frac{1}{11}$

and 1

125. The value of

$$\lim_{x \otimes i} \frac{a_{1}^{a_{1}/x} + \frac{b_{2}}{2}x + \dots + a_{n}^{1/x} \ddot{o}^{nx}}{\dot{s}}$$

$$a_{1} > 0, i = 1, 2, \dots, n, is$$

$$a_{1} + a_{2} + \dots + a_{n}$$

$$b) ea 1 + a 2 + \frac{1}{4}an$$

$$(c) \frac{a_{1} + a_{2} + \dots + a_{n}}{n}$$

126. The value of $\cot -17 + \cot -18 + \cot -118$ is

(a) p (b) $\cot -1.3$,cot-1 5 exdxis equal to : sinx+1

$$\begin{array}{c} \underbrace{e^{x} \cos x}_{1+\sin x} + C & (b) \\ C - \underbrace{e^{x}}_{1+\sin x} & \underbrace{e^{x} + \$iftx}_{1+\sin x} \\ \end{array}$$

128. A random variable X has the probability distribution

X 4 3 5 6 8 p(X) 0.15 0.23 0.12 0.10 0.20 0.08 0.07 0.05 For the events $E = \{X \text{ is a prime number}\}$ and $F = {X < 4}$ then $P(E \to F)$ is

- (a) 0.50 (b) 0.77 (c) 0.35 (d) 0.87 (a) 0.50° (b) 0.77° (c) 0.77° (c) 0.77° (c) 0.77° (c) 137.5 m models for a second seco (a) 4 (b) 5 (d) 8
- (c) 6 130 The area under the curve $y = |\cos x - \sin x|$,

Of
$$x \notin \frac{p}{2}$$
, and above x-axis is:
(a) $2\sqrt{7}$ (b) $2\sqrt{7}$ -2
(c) $2\sqrt{7}$ +2 (d) 0

 $i x \log \cos x$ x = 0

131. If
$$f(x) = \frac{1}{10} \frac{\log(1+x^2)}{\log(1+x^2)}$$
 then $f(x)$ is
 $\frac{1}{10} = 0$, $x = 0$

- (a) continuous as well as differentiable at x = 0
- (b) continuous but not differentiable at x = 0
- (c) differentiable but not continuous at x = 0
- (d) neither continuous nor differentiable at $\mathbf{x} = \mathbf{0}$
- 132. The maximum value of z = 3x + 2y subject to $x + 2y^{3}2$, $x + 2y \pounds 8$, x, $y^{3}0$ is : (a) 32 (b) 24
 - (c) 40 (d) None of these
- 133. A cylindircal gas container is closed at the top and open at the bottom. if the iron plate of the top is $\frac{3}{4}$ time as thick as the plate forming the 140. cylindrical sides. The ratio of the radius to the height of the cylinder using minimum material for

the same capacity is (b) $\frac{1}{2}$ (c) $\frac{1}{5}$ (d) $\overline{3}$ (a) $\frac{1}{3}$

134. Let A, B, C be finite sets. Suppose that n (A) = 10, n (B) = 15, n (C) = 20, n (A C B) = 8and n (B \subset C) = 9. Then the possible value of n (A E B E C) is (b) 27(c) 28 (d) Any of the three values 26, 27, 28 is possible

135. If
$$f(z) = \frac{7 - z}{1 - z^2}$$
, where $z = 1 + 2i$, then $|f(z)|$ is equal to :

Z (a) (b) |z| $\overline{2}$ (d) None of these (c) 2 | z |

136. If
$$f(x) = \cos \frac{\hat{e}^{1} \cdot (\log x) \hat{2}}{\hat{e}\hat{e}^{1} + (\log x) \hat{2}\hat{u}\hat{u}}$$
 then the value of $f \notin (e)$

is equal to

(b) (c)(d) 2 (a) 1 $\overline{2e}$

is to be formed using the digits 0, 1, 2, 3, 4 and 5 with repetition. The total number formed are 216. Statement 2 : If sum of digits of any number is divisible by 3 then the number must be divisible by 3.

- (a) Statement-1 is true, Statement-2 is true, Statement-2 is a correct explanation for Statement -1
- Statement -1 is true, Statement-2 is true ; (b)Statement-2 is NOT a correct explanation for Statement-1
- Statement-1 is true, Statement-2 is false (c)
- (d) Statement-1 is false, Statement-2 is true
- 138. The equation of one of the common tangents to the parabola $y_2 = 8x$ and $x_2+y_2-12x+4=0$ is

(a)
$$y = -x + 2$$

(b) $y = x - 2$
(c) $y = x + 2$
(d) None of these

é cost sintù

- 139. If R (t) = \hat{e}_{sint} costúû then R(s) R(t) equals
 - (a) R(s+t)(b) **R** (s-t) $\hat{\mathbf{r}}$ \mathbf{R} $\hat{\mathbf{s}}$ + $\hat{\mathbf{R}}$ $\hat{\mathbf{r}}$ (d) None of these

$$If = - 1\ddot{a}$$

$$\overset{\text{In}}{\underset{\text{e}}{\text{of }}} \overset{\text{log}}{\underset{\text{f}}{\text{fr}}} \overset{\text{f}}{\underset{\text{f}}{\text{fr}}} \overset{\text{f}}{\underset{\text{f}}{\text{fr}}} dx = f(x) \log(x+1) + g(x)x^2 + Lx$$

$$+ C, \text{ then}$$

(a)
$$f(x) = \frac{1}{2}x^2$$

(b) $g(x) = \log x$
(c) $L = 1$
(b) $R(x) = \log x$
(c) None of these

146. The ratio in which the join of (2, 1, 5) and (3, 4, 3)141. Let a,b&c be non-coplanar unit vectors is divided by the plane $(x + y - z)\frac{1}{2}$ is: equally inclined to one another at an acute angle q. Then [[abc]] in terms of q is equal to (a) 3:5 (b) 5:7 (c) 1:3 (d) 4:5(a) $(1+\cos q) \sqrt{\cos 2q}$ 147. Value of $\underset{0}{\overset{p/2}{\diamond}} \frac{\sqrt{\sin x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx$ is (b) $(1+\cos q) \frac{1}{2\cos q}$ (c) $(1-\cos q) \frac{1}{2\cos q}$ (a) <u>P</u> (b) $\frac{-p}{2}$ (d) None of these р (c) <u>4</u> 142. 21/4. 22/8. 23/16. 24/32.....¥ is equal to-(d) None of these (b) 2 (a) 1 (d) 5/2 (c) 3/2148. The dot product of a vector with the vectors $i+j^{-3}k^{\circ}$, $i+3j^{-2}k^{\circ}$ and $2i^{+}j^{+4}k^{\circ}$ are 0, 5 and 143. If $a_{r=0}^{n}$ $r = \frac{1}{r+3} + \frac{3}{r+3} + \frac{3}{r+3}$, then a - n is equal to 8 respectively. The vector is (a) $i^{+}2j^{+}k^{-}$ (b) $-i^{+}3j^{-}2k^{-}$ (a) 0 (b) 1 (c) $i^{+}2j^{+}3k^{-}$ (d) $i^{-}3i^{-}3k^{-}$ (c) 2 (d) None of these 149. The angle between the lines whose intercepts 144. If $\begin{vmatrix} p & q - y & r - z \\ p_{-} x & q & r \\ p_{-} x & q_{-} y & r \end{vmatrix}$ then the value of on the axes are a, -b and b, -a respectively, is (a) $\tan -1 \frac{a^2 - b^2}{ab}$ (b) $\tan 1 \frac{b^2 - a^2}{2}$ (c) $\tan^{-1} \frac{b^2 - a^2}{2ab}$ None of these $\frac{p}{x} + \frac{q}{v} + \frac{r}{z}$ is (a) 0 (b) 1 (c) 2 (d) 4pqr 150. If the line through the points A (k, 1, -1) and B 145. An urn contains five balls. Two balls are drawn (2k, 0, 2) is perpendicular to the line through the and found to be white. The probability that all the points B and C (2 + 2k, k, 1), then what is the balls are white is value of k?

- (a) $\frac{1}{10}$ (b) $\frac{3}{10}$ (c) $\frac{3}{5}$ (d) $\frac{1}{2}$
- (a) -1 (b) 1 (c) -3 (d) 3

SOLUTIONS

5.

6.

PART - I : PHYSICS

1.

(a) As we know,
Gravitational potential energy
$$\frac{-GMm}{r}$$

and orbital velocity, $y = \sqrt{GM/(R+h)}$
 $= \sqrt{\frac{GM}{(R+2R)}} = \sqrt{\frac{GM}{3R}}$
Ef $= \frac{1}{2}mv2Q$ $\frac{GMm}{3R} = \frac{1}{2}m\frac{GM}{3R} - \frac{GMm}{3R}$
 $= \frac{GMme}{3R} \frac{-\ddot{Q}}{c^2} - \ddot{Q} = \frac{-GMm}{6R}$
Ei = $\frac{-GMm}{R} + K$
Therefore minimum required energy,

K =
$$\frac{5GMm}{6R}$$

2. (a) W = TDA = 4pR2T(n1/3 - 1)
= 4 × 3.14 × (10-2)2 × 460 × 10-3 [(106)1/3 -1]
= 0.057
3. (c) $\frac{1}{f_1} = \frac{\& 3 \cdot \ddot{o} \& 1}{\& 2} \cdot \frac{1}{25\sigma} & \frac{1}{50}$, 7.
 $\frac{1}{f_2} = \frac{\& 4 \cdot \ddot{o} \& 1}{\& 3} \cdot \frac{1}{20\sigma} = \frac{3}{100}$
and $\frac{1}{f_3} = \frac{\& 3 \cdot \ddot{o} \& 1}{\& 2} \cdot \frac{1}{20\sigma} = \frac{3}{100}$
and $\frac{1}{f_3} = \frac{\& 3 \cdot \ddot{o} \& 1}{\& 2} \cdot \frac{1}{20\sigma} = \frac{1}{20} = \frac{1}{40}$
Now $\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2} + \frac{1}{f_3}$
 $= -\frac{1}{50} + \frac{3}{100} - \frac{1}{40}$
A (1) Where a charged on the product of the term

(b) When a charged particle enters a magnetic 4. field at a direction perpendicular to the direction of motion, the path of the motion is circular. In circular motion the direction of velocity changes at every point (the magnitude remains constant). Therefore, the tangential momentum will change at every point. But kinetic energy

will remain constant as it is given $\frac{1}{2}ynv^2$ and v2 is the square of the magnitude of velocity which does not change. $\frac{2}{3}$

(b)
$$N=N0 \quad \frac{\partial e^{i}}{\partial \xi^{2}} \dot{\vec{e}}^{i}$$
or
or
or
Half life
$$\frac{N_{0}}{16} = N0 \frac{\partial e^{i}}{\partial \xi^{2}} \dot{\vec{e}}^{i}$$

$$n = 4$$

$$t_{1/2} = -n = \frac{1}{4} = \frac{1}{2}h$$
(a) The charging of inductance given

(a) The charging of inductance given by,

 $= -\frac{1 \overset{\text{ac}}{\xrightarrow{}} QB - Q_A \ddot{o}}{\frac{4}{0} \rho \dot{l} \dot{e} r_B^2 \overset{\text{c}}{\xrightarrow{}} \sigma}$

These values are correctly represent in option (a).



8. (b)
$$M = (p2rh)_r = pr \frac{2\pi}{e} \frac{2\pi}{rrg} \frac{cosq}{\sigma} rrg}{rrg} rrg} r$$

and $Mc = (2) r \frac{2\pi}{c} \frac{2T \cos q}{c rrg} rrg} rrg}{rrg} rrg} rrg} rrg$
 $= 2M.$
9. (a) $f = \frac{5}{2i} \sqrt{\frac{F}{rrg}} = \frac{5}{2i} \sqrt{\frac{9\pi}{rrg}}$ (i)
 $\frac{1}{\sqrt{1-rg}} rrg} rrg} rrg rrg} rrg$
and $f = \frac{3}{2l} \sqrt{\frac{Mg}{rrg}}$ (ii)
From above equations, we get $M = 25$ kg.
10. (a) We have, $E = W0 + K$
or $\frac{hc}{40010^{-9}} = W0 + \frac{1}{2}mv^2$... (i)
and $\frac{hc}{250'10.9} = W0 + \frac{1}{2}m(2v)2$... (ii)
On simplifying above equations, we get
 $W0 = 2hc'106J.$
11. (d $V = 0$, and so $C = V \otimes V$.
12.) Mass of uranium changed into energy
(d) $= \frac{0.1}{700} r 1$
 $= 10-3 kg.$
The energy released $= mC2$
 $= 10-3 \times (3 \times 108)2$
 $= 9 \times 1013 J.$
13. (d) The change in internal energy DU is same
in all process.
 $QACBFDU + W_{ACB}$
 $Q = r,$
 $QAEBBDU + AEW$
Here W_{CB} is positive and W_{EB} is negative.
Hence $Q_{ACB} > Q_{ADB} > Q_{AEB}$
14. (c) Dimensions of $Y = dimensions of X$
 $= \frac{M^{-1}L^{-2}T^{4} R^{2}}{(MT^{-2}Z^{-1})^{2}}$
 $= [M-3 L^{2}T8 A4]$

15. (d) Net magnetic field due to the wires will be downward as shownbelow uirn the figure. Since angle between v and B is 180°,



$$\sqrt{\frac{X}{53}} = \frac{10}{50}$$
 $\sqrt{X} = \frac{53}{5} = 10.6W$

18. (a) Total flux through the cubical surface,

$$f = \frac{q_{in}}{\hat{l}_0}$$

$$= \underbrace{e^{\frac{4}{9}3 + 2(+7)}}_{\frac{6}{9}} \underbrace{e^{\frac{3}{10}} \underbrace{e^{\frac{2}{10}}}_{\frac{10}{10}} \underbrace{e^{\frac{2}$$

$$= (\underline{\mathbf{m}' 2\mathbf{v}})^2 + (2\underline{\mathbf{m}' \mathbf{v}})^2 \quad (\text{magnitude})$$
$$= 22\overline{\mathbf{m}}\mathbf{v}$$

Final momentum of the system = 3mVBy the law of conservation of momentum

$$2\sqrt{2}mv=3mV$$

 $\Rightarrow \frac{2\sqrt{2}v}{3} = V_{\text{com bi ned}}$
Loss in energy

$$DE = \frac{1}{2}m1V^{2}H \frac{1}{2}m2V^{2}-\frac{1}{2}m1 + m2)V_{combined}^{2} 25.$$

$$DE = 3mv^{2}-\frac{4}{3}mv^{2}=\frac{5}{3}mv^{2}=55.55\%$$

20. (d) Because of the Lenz's law of conservation of energy.

21. (c)We know that

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$$Y = \frac{\text{mg/A}}{\text{DI/I}} = \frac{\text{mg1}}{\text{ADI}} \qquad \dots (1)$$

Also $D_{|} = | a DT$ From (1) and (2)

$$Y = \frac{mgl}{A \mid a \mid DT} = \frac{mg}{A_a \mid DT}$$
$$m = \frac{YA_a \mid DT}{g} = \frac{10 \quad (p(10 \ 3)2 \ (10 \ -5 \ (10))}{10} = p \approx 3$$

24.

١

$$\delta r$$
 rmd = $\frac{1}{\sin 60^{\circ}}$

$$\frac{mg}{m_{\mu}} = \frac{2}{\sqrt{3}}$$
$$= \frac{\sqrt{3}}{2}mg = \frac{\sqrt{3}}{2}$$
'1.5
$$= 1.3$$

 $C_{max} = 60^{\circ}$

1

23. (c) The frequency of tuning fork, f = 392 Hz.

Also
$$392 = \frac{1}{2'50} \sqrt{F/m}$$
(i)
After decreasing the length by 2%, we have
 $fc = \frac{1}{2(49)} \sqrt{F/m}$ (ii)

From above equations,

f¢=400 Hz.
\Beats frequency=8 Hz.
(a)
$$Z_1 = 1, Z_2 = 1, Z_3 = 2$$
 and $Z_1 = 3$.

$$\begin{cases}
1 & RZ_{22} = 1 \\
z = constant
\end{cases}$$
or $3RZ_2$
or $1Z_2 = constant$
So
 $1(1)_2 = 12(1)_2 = 13(2)_2 = 1$ a(3)³
or $11 = 12 = 413 = 914$.
(a) $t = t = 0$
 $t = t = 0$

$$x = a\cos \frac{\mathbf{p}}{\mathbf{e}} + \frac{\mathbf{p}}{\mathbf{e}} + 4\mathbf{0}$$

or
$$x = a\cos\frac{a^2pt}{4} + \frac{p\ddot{o}}{4}$$

26. (b) $Dx_{max} = 0$ and $Dx_{max} = 21$ Theortical maximas are $= 2n + 1 = 2 \times 2 + 1 = 5$ But on the screen there will be three maximas.

27. (d) The net resistance of the circuit is 9W as shown in the following figures.



The flow of current in the circuit is as follows. 32.



The current divides into two equal parts if passes through two equal resistances in parallel. Thus current through 4W resistor is 0.25 A.

- 28. (d) Here $\frac{x}{1000} = \frac{1.221}{D}$ 34. or $x = \frac{1.22 \cdot 5 \cdot 103 \cdot 10^{-10} \cdot 10^3}{10^{\cdot}10^{-2}}$ or $x = 1.22 \times 5 \times 10{-3}$ m = 6.1 m x is of the order of 5 mm.
- 29. (d) The change of state from liquid to vapour (for gas) is called vapourisation. It is observed that when liquid is heated, the temperature remains constant untill the ³⁵. entire amount of the liquid is converted into vapour.

The temperature at which the liquid and the vapour states of the substance coexists is called its boiling point.

30. (d)When the wire is bent in the form of a squar86. and connected between M and N as shown in fig. (2), the effective resistance between M and N decreases to one fourth of the value in fig. (1). The current increases four times the initial value according to the relation V = IR. Since H = I2 Rt, the decrease in the value of resistance is more than compensated by the increases in the value of current. Hence heat produced increases. Percentage loss in energy during the collision ; 56% U = mV =

kmr. Force, $F = -\frac{dU}{dr} = -km$ $Nqw_{\pm} \frac{mv^2}{r} = km P v \mu r^{-1/2}$ $\frac{2pr}{v} = \frac{2pr}{cr1/2} PT\mu r^{1/2}$ (b) $\sin q = \frac{1}{2}$ $N_1 \sin q = N_2$ $\frac{N1}{N2} = \frac{1}{\sin q} = 2.$

 (a) When charge is given to inner cylinder, an electric field will be in between the cylinders. So there is potential difference between the cylinders.

(a)
$$\frac{x}{\sin 2q} = \frac{r}{\sin(90\text{-}q)}$$

$$p \qquad x = 2r \sin q$$

$$\sqrt{\frac{dx}{dt}} = 2 r \cos q \cdot \frac{dq}{dt}$$

$$\frac{dq}{dt} = \frac{dx/dt}{2r \cos q} = \frac{v_0}{2r \cos 60^\circ} = \frac{v_0}{r}$$

(c)
$$\frac{R^2}{R^2} = [A^2 + B + 2 AB \cos q]$$

$$= R^2 + R^2 + 2R^2 \cos q$$

$$R^2 = 2R^2 \cos q \text{ or } \cos q = -1/2$$

or $q = 2p/3$

(b) B=m0mrH \triangleright mr μ $\frac{B}{H}$ = slope of B-H curve

According to the given graph, slope of the graph is highest at point Q.

37. (b)
$$v_{av} = \frac{6500 + 600 + 700 + 800 + 900}{6} \dot{u}_{=} 700 \text{m/s}$$

and
$$= \sqrt{\frac{5002 + 6002 + 7002 + 8002 + 9002}{2}} = 714 \text{m/s}$$

$$= \frac{1}{14 \text{ m/s}} - \frac{1}{14 \text{ m/s}}$$

is greater than average speed by 14 m/s.
38. (b) The effective circuit is shown in figure.



$$C = \frac{2}{3}\mu C$$

Now $C_{AB} = 2C = \frac{4}{3} \text{ mF}$

- 48. 48.
 39. (a) Process AB is isobasic and BC is isothermal, CD isochoric and DA isothermic com pr essi on .
 40. (d) During the operation either of D and D ⁴⁹.
- 40. (d) During the operation, either of D and D ^{49.} be in forward bias. Also R and R are different, so output across R will have different peaks. 50.

PART - II : CHEMISTRY

41. (b) Polystyrene and polyethylene belong to the category of thermoplastic polymers which are capable of repeatedly softening on heating and harden on
 42 (d) cooling. Hybridisation :

42. (d)

$$[Fe(CN)_{d}]^{4-}, [Mn(CN)_{d}]^{4-}, d^{2}sp^{3}$$

$$(fe(CN)_{d}]^{4-}, [Mn(CN)_{d}]^{4-}, d^{2}sp^{3}$$

$$(feco(NH_{3})_{6}\dot{\mu}]^{3+} feco(NH_{3})_{6}\dot{\mu}]^{2+}$$

$$(feco(NH_{3})_{6}\dot{\mu}]^{3+} feco(NH_{3})_{6}\dot{\mu}]^{2+}$$

$$(feco(NH_{3})_{6}\dot{\mu}]^{3+} feco(NH_{3})_{6}\dot{\mu}]^{2+}$$

$$(feco(NH_{3})_{6}\dot{\mu}]^{3+} feco(NH_{3})_{6}\dot{\mu}]^{2+}$$

$$(feco(NH_{3})_{6}\dot{\mu}]^{2+} feco(NH_{3})_{6}\dot{\mu}]^{2+} feco(NH_{3})_$$

44. (d) ₄

- 45. (a) More is E[°]_{RP}, more is the tendency to get itself reduced or more is oxidising power.
- $DG = -2.303 \text{ RT} \log K$ 46. (c) $-nFE^\circ = -2.303 \text{ RT} \log K$ $\log K = \frac{nFE}{2.303 \text{ RT}}$ 0.4342_RT_ (i) $\ln K = {^{nFE}}$ RT nFE (ii) K = e RTO.S. of N 47. (c) Compound N2O NO + 1 +2NO2 +4+ 5NO-3 NH+4 - 3 Therefore increasing order of oxidation state of N is:

$$NH_4^+ < N_2O < NO < NO < NO3$$

(a) Raoult's law becomes special case of Henry's law when Hybecome equal to p°.1

.

(b)
$$E_{cell}^{o} = \frac{0.059}{2} \log K cor \quad 0.059^{2} = \log K_{c}$$

 $\langle K_{c} = 1.9' 10^{37}$

(d)
$$\frac{P}{T}$$
 = constant (Gay Lussac's law)

$$\stackrel{P}{1} = \frac{P}{2} \stackrel{P}{\Rightarrow} P1T2= P2T1$$

$$\stackrel{PV}{=} \stackrel{P}{constant}$$

$$\stackrel{PV}{=} \stackrel{P}{2} \stackrel{V2}{=} [Boyle's law]$$

$$\stackrel{P}{=} \stackrel{P}{2} \stackrel{P}{=} \stackrel{P}{2} \stackrel{P}{=} \stackrel{$$

51. (b) Dn=-
$$\frac{1}{2}$$
; DH=DE- $\frac{2}{R}$ T; \Rightarrow DE>DH

52. (d) For H atom,
$$E_{\mathbf{H}} - \frac{13.6Z^2}{n^2} eV$$

For second orbit, $n = 2$
 $Z = At. no. = 1$ (for hydrogen)
 $\langle E_2 = -\frac{13.6 \cdot (1)^2}{(2)^2} = \frac{-13.6}{4} eV$
 $= \frac{-13.6 \cdot 1.6 \cdot 10^{-19}}{4} J$

$$= -5.44 \ 10^{-19} \text{J}$$

- 53. (b The right sequence of LE of Li < B < Be < Colored 3. (c) M1V1 = M2V2
- 54.) Photochemical smog does not involve SQ.
- 55. (c There are four chief minerals present in a) Portland cement tricalcium silicats (Ca) (c dicalcium silicate (Chand calcium atumino-
 -) aluminate (Ca ferrite (CaAlnFe2-nO7).
- 56. (a) Ammonia is a weak base and a salt containing its conjugate acid, the **Authors in the solution** when they are present together in a solution. Among these ligands, 'F' is a weak field
- 57. (c) ligand, makes only high spin complexes which has sp3d2 hybridization. Glycosidic linkage is a type of covalent bond
- 58. (d) that joins either two carbohydrate (sugar) molecule or one carbohydrate to another group. All molecules show such type of linkages.
 - Schotten-Baumann Conditions

$$R \longrightarrow \begin{array}{c} O \\ R \longrightarrow \\ Cl \end{array} + H^{2N} - R \not \in \begin{array}{c} NaOH \\ R \longrightarrow \\ R \longrightarrow \\ R \longrightarrow \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} O \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array} \xrightarrow{O} \\ N - R \not \in \begin{array}{c} N \\ H \end{array}$$

The use of added base to drive the equilibrium in the formation of amides from amines and acid

- 60. (c) chlorides. Note that in structures 1 and 2, every two adjacent hydrogen atoms are at maximum possible distance from each other (staggered
- 61. (b) conformation). Bond length decreases with an increase in bond order. Therefore, the order of bond bygth ind bracer spaces 25 0 = 2, 2 + 5. $O^{2}_{-}=1)$
- 62. (a) For a given orbital with principal quantum number (n) and azimuthal quantum number (1) number of radial nodes = (n - 1 - 1) for 3s orbital: n = 3and 1 = 0 therefore, number of radial nodes = 3 - 0 - 1 = 2 for 2p orbital: n = 2 and 1 = 1 therefore, number of radial nodes = 2 - 1 - 1 = 0

- (0.025 M) (0.050 L) = (2M(0.025 L))M2 = 0.05 Mbut, there are 2 H's per **25**O4 so [H2SO4] = 0.025 M
- 64. (a) Given, mass ratio is C:H:O (6:1:24) so, molar ratio will be 6/12:1/1:24/16 = 1:2:3therefore, HO-(C=O)-OH has molar ratio 1:2:3
- 65. (b) In bcc structure, no. of atoms at corner = $1/8 \times 8 = 1$ no. of atom at body centre = 1therefore, total no of atom per unit cell = 2.
- 66. (b) **PH**oes not exist because d-orbital of 'P' interacts with s-orbital of H. Bond formed is not stable and not energetically favorable. It depends on size and orientation of interaction.
- Ionic bonding is non directional, whereas 67. (b)
 - covalent bonding is directional. So, CDis d ir ect ion al.
- 68. (a) Given DH 35.5 kJ mol-1 DS = 83.6 JK - 1 mol - 1Q DG = DH - TDSFor a reaction to be spontaneous, DG = -vei.e., DH < TDS

$$T > \frac{DH}{DS} = \frac{35.5'103 \text{Jmol-1}}{83.6 \text{JK}^{-1}}$$

So, the given reaction will be spontaneous at T > 425 K

69. (c)
$$|_{m} = \frac{1000k}{0.1} = \frac{1000 \cdot 3.75 \cdot 10^{-4}}{0.1} = 3.75;$$

 $a = \frac{|_{m}}{|_{m}^{\frac{1}{m}}} = \frac{3.75}{250} = 1.5 \cdot 10^{-2};$
Ka = G2 = 0.1 × (1.5 × 1 $\frac{69}{10}$ = 2.25 × 10⁻⁵
70. (b) Rate = k [A]x[B]y ... (1)

$$\frac{\text{Rat}q}{4} = k [A]x [2B]y \qquad \dots (2)$$

or Rate = 4k[A]x[2B]y

$$\frac{k[A]^{x}[B]^{y}}{4} = k[A]x[2B]y$$

$$\frac{[B]^{y}}{4} = [2B]y$$

or
$$\frac{1}{4} = \underset{B}{\overset{\text{e}}{\oplus}} \underset{\emptyset}{\overset{B}{\oplus}} \underset{\emptyset}{\overset{O}{\oplus}} \underset{\emptyset}{\overset{V}{\oplus}} \underset{\emptyset}{\overset{V}{\oplus}} \frac{1}{4} = 2y \text{ or } (2) - 2 = 2y$$

71. (a) A compound is said to exhibit optical isomerism if it atleast contains one chiral carbon atom, which is an atom bonded to 4 different atoms or groups.

- 72. (c) Meso compounds are characterized by an internal plane of symmetry that renders them achiral. Control rods
- 73. (a) slowdown the motion of neutrons and help in controlling the rate of fission. Cadmium is efficient for this purpose.
- 74. (c) Reducing reagent is needed, as shown 80. in given reaction.



- 75. (c) H2CO3 $\xrightarrow{H^+ + HCO}$ $\xrightarrow{H^+ + HCO}$ $\xrightarrow{H^+ + HCO}$ $\xrightarrow{H^+ + HCO}$ $\xrightarrow{H^+ + HCO}$ candonate and accept H.
- 76. (c)





- 77. (c) Because Na is very reactive and cannot be extracted by means of the reduction by C, CO etc. So it is extracted by
 78. (d) electrolysis Potation of B through 180°
- 78. (d) electrolysis. Rotation of B through 180° within the plane

of the paper gives D which is an enantiomer of A, hence A and B are enantiomers



79. (b

.) Thyroxine is an amine hormone.

PART - III (A) : ENGLISH PROFICIENC

- 81. (a) indeansordLoquacious (Adjective)
 - talking a lot; talkative. Option (a) is the right synonym while others have different meanings.
- 82. (c) The word Meticulous (Adjective) means : paying careful attention to every detail; fastidious; thorough. Careless in option (c) is the correct

antonomy.

- 83. (c 84. (b) 85. (d) 86. (b)
- 87.) China is a big country. In area it is bigger
 - (b than any other country except Russia.
) [except means other than, accept means consent, expect means to anticipate and access means entrance].
- 88. (d) The treasure was hidden off the shore. When something is hidden "off the shore," it just means that it's hidden somewhere near it.
- 89. (b Delete 'pair of' before binocular because the word 'binocular' itself suggests a pair.
- 90.) Delete 'all' before 'left'. Here the usage of 'all' is superfluous as 'the teacher as well as
 - (b his students' itself signifies everyone.

PART - III (B) : LOGICAL REASONIN

91. (b

)

92.) Option (d) will complete the question figure.



94. (c) All the components of question figure are present in Answer Figure (c)



- 95. (b) In each row, the second figure is obtained from the first figure by adding two mutually perpendicular line segments at the centre and the third figure is obtained from the first figure by adding four circles outside the main
- 96. (d) figure ach row, the second figure is 103. (a) Tentifie and V: Church are places of obtained by rotating the first figure through 90° CW or 90° ACW and adding a circle to it. Also, the third figure is obtained by adding two circles to the first figure (without rotating the
- O is the husband of P. M is the son of P. 97. (a Therefore, M is the son of O.
- Wife of Vinod's father means the mother of 98.) Vinod.
 - Only brother of Vinod's mother means 105. (c) (a maternal uncle of Vinod.
- Therefore, Vinod is cousin of Vishal. 99. (a) The pattern is as follows:
 - A³/4+³/42[®] +²C³/3/4[®]E²/3/4[®]G³/3/4[®]I³/4[°]/4[°]/8^K

 - $S^{3/4+3/4} = B^{3/4} + 3^{3/4} + 2^{3/4} + 3^{3/4} + 2^{3/4} +$
 - Y³/4+³/42/R³/₄³/₄²/₈⁴/₈
- 100. (b) The pattern is as follows :

 $P^{3/4}$ +3 +3 +3 +3 E 348S34348Y34348Y34348B +3 3444 R 3434 R 3434 R 3434 R 3448 +3 0 34+343+3+3+3T®W3434®Z3434®C34348F

34+343+3+3+318L34348O34348R34348U

Therefore, the first term should be

 $GA^{3/4+3/4} \mathbb{R}^{3/4+3/4} \mathbb{R}^{3/4+3/4} \mathbb{R}^{3/4+3/4} \mathbb{R}^{3/4} \mathbb{R}^{$ М

The statement implies that politicians win elections by the votes of people. Therefore, neither of the assumptions is implicit in the statement.



wErship. It does not imply that Hindus and Christians use the same place for worship. Church is different temple. Therefore, neither Conclusion I nor II follows. Growth and development of 104. (a) human organism is a continuous process. Some changes take place in human body now and then. Therefore, neither Conclusion I nor II follows.

PART - IV : MATHEMATICS

- 106. (b) We have g(-3) = 0f(g(-3)) = f(0) = 7(0)2 + 0 - 8 = -8Þ١ fog(-3) = -8g(9) = 92 + 4 = 85 P f (g(9)) = f (85) = 8(85)+3 = 683
 - fog(9) = 683١ f(0) = 7.02 + 0 - 8 = -8 Pg(f(0)) = g(-8)= |-8| = 8

$$\begin{cases} gof (0) = 8 \\ f (6) = 4(6) + 5 = 29 \ P \ g (f (6)) = g (29) = (29)2 \\ + 4 = 845 \\ gof (6) = 845 \end{cases}$$

101.(d)

107. (c) X - X - X - X. The four digits 3, 3, 5,5 can be arranged at (-) places in $\frac{4!}{2!2!} = 6$ ways. The five digits 2, 2, 8, 8, 8 can be arranged 111. (d) The given system of lines passes through at (X) places in $\frac{5!}{1213}$ ways = 10 ways Total no. of arrangements = 6'10=60ways 108. (b) $\overset{n}{\overset{n}{a}}_{k=1}^{n}(k)(k+1)(k-1) = \overset{n}{\overset{n}{a}}_{k=1}^{n}k(k^{2}-1) = \overset{n}{\overset{n}{a}}_{k=1}^{n}(k^{3}-k)$ $= a e^{a(n+1)} \ddot{o}^{2}_{2} - n(n+1)$ $=\frac{n(n+1)}{2}\underset{\xi}{\overset{\alpha}{\overset{\alpha}}}_{\xi}\frac{n(n+1)}{2}-\overset{\ddot{o}1}{\overset{+}{\wp}}_{\xi}$ $=\frac{n^{2}+n^{2}+n^{2}+n^{2}-2}{2}\overset{o}{g}=\frac{n^{4}+n^{3}-2n^{2}+n^{3}+n^{2}-2n}{4}$ 113 $=\frac{n^4}{4}+\frac{n^3}{2}-\frac{n^2}{4}-\frac{n}{2}$ $\Rightarrow =8-\frac{1}{2}$ 109. (c) Let eq. of ellipse $b\frac{x^2}{2} + \frac{y^2}{b^2} = 1$, length of semi-latus rectum 114 $=\frac{b^{r}}{a}=\frac{a^{r}(1-e^{r})}{a}=a(1-e^{r})$ Given $a(1 - \frac{e^2}{2}) = \frac{1}{r}(ra)$ $p = 1 \cdot e^2 = \frac{2}{3} p \cdot e^2 = 1 \cdot \frac{2}{3} = \frac{1}{3} \cdot e^2 = \frac{1}{\sqrt{3}}$ 110. (c) Given quadratic eqn. is $x^2 + px + \frac{3p}{4} = 0$ So, $a + b = -p \cdot ab = \frac{3p}{2}$

Now, given
$$| \mathbf{a} - \mathbf{b} | = \sqrt{10} \mathbf{pa} - \mathbf{b}$$

= $\pm \sqrt{10}$
 $\mathbf{p} (\mathbf{a} \cdot \mathbf{b})^2 = 10 \mathbf{pa} 2 + \mathbf{b} - 2\mathbf{ab} = 10$
 $\mathbf{p} (\mathbf{a} \cdot \mathbf{b})^2 - 4\mathbf{ab} = 10$

 $p2-4 \times \frac{3p}{4} = 10 \Rightarrow p2-3p-10 = 0$ $p = -2, 5^{4}$ $p\hat{} = -2, 5\}$

Þ

the point of intersection of the straight lines 2x + y - 3 = 0 and 3x + 2y - 5 = 0[L1 + 1L2 = 0 form], which is (1, 1). The required line will also pass through this point. Further, the line will be farthest from point (4, -3) if it is in direction perpendicular to line joining (1, 1) and (4, -3). The equation of the required line is y-1 = $\frac{1}{-3-1}(x-1)b$ 3x - 4y + 1 = 0 112. (b) $\frac{n!}{n^n} = \frac{3}{32} \triangleright \frac{n!}{n^n} = \frac{8 \cdot 3}{8 \cdot 3} = \frac{4!}{24^4}$ n = 4

113. (b) R
$$=(3+\sqrt{5})^{2n}$$
, G $=(3-\sqrt{5})^{2n}$
Let [R] + 1 = I (Q[.] greatest integer
function)
P R + G = I (Q 0 < G < 1)
P $(3+\sqrt{5})^{2n} + (3-\sqrt{5})^{2n} = I$
seeing the option put n = 1
I = 28 is divisible by 4 i.e. 2n+1
114. (c) For f (x) to be defined, we must have
 $-1 \notin \log 2 \stackrel{\text{@}}{\underset{e2}{\text{@}}} \stackrel{1 \times 2\ddot{0}}{\underset{e2}{\text{@}}} \pounds 1$
p $2-1 \notin 2 \times 2 \notin 21$ [Q the base = 2 > 1]
P $1 \notin x^2 \notin 4$ (1)
P Now, $1 \notin x^2$
P $x^2 - 1^3$ 0 i.e. $(x - 1) (x + 1)^3$ 0
P $x \notin -1$ or x^3 1(2)
P Also, $x^2 \notin 4$
 $x^2 - 4 \notin 0$ i.e. $(x - 2) (x + 2) \notin 0$
 $-2 \notin \pounds 2$ (3)
Form (2) and (3), we get the domain of
f = {(- $\frac{1}{3}$, -1] $\stackrel{\text{`E}}{\text{[}}$ [1, $\frac{1}{3}$]} $\stackrel{\text{`C}}{\text{[}}$ [-2, 2]
= [-2, -1] $\stackrel{\text{`E}}{\text{[}}$ [1, 2]
115. (a) We construct the following table taking
assumed mean a = 55 (step deviation
method).

Class	X.	f_i	c.f.	$u_i = \frac{xi-a}{10}$	$f_i^{}u_i^{}$
10-20	15	2	2	-4	-8
20-30	25	3	5	-3	-9
30–40	35	4	9	-2	-8
40–50	45	5	14	-1	-5
50-60	55	6	20	0	0
60–70	65	12	32	1	12
70–80	75	14	46	2	28
80–90	85	10	56	3	30
90–100	95	4	60	4	16
Total		60			56

\ The mean =
$$\frac{a^{a}\hat{f}\hat{i}\hat{i}\hat{i}}{a\hat{f}\hat{i}}$$
 ' h
= 55 + $\frac{56}{60}$ ' 10 = 55 + $\frac{56}{6}$ = 64.333

Here $n = 60 P \frac{n}{2} = 30$, therefore, 60–70 is the median class Using the formula :

M =
$$|+\frac{-\bar{f}C}{12}$$
, $c = 60 + \frac{30-20}{12}$ 10

$$= \frac{60 + \frac{100}{12}}{_{iB}} = 60 + 8.333 = 68.333$$

116. (c) $2e = e + e^{iC}$

$$\Rightarrow 2\cos B = \cos A + \cos C \qquad \dots (i)$$

- & 2 sin B = sin A + sin C ...(ii) Squaring and adding we get cos(A-C)=1ÞA-C=0
- A = C, From (i) and (ii) cos B = cos Aand sin B = sin A $So, A = B. <math>\blacktriangleright A = B = C$

117. (c)
$$d = h \cot 30^\circ - h \cot 60^\circ$$
 and time = 3 min.



It will travel distance h cot 60° in



119. (c) Since the equilateral triangle is inscribed in the circle with centre at the origin, centroid lies on the origin.

So,
$$\frac{AO}{OD} = \frac{2}{1} \Rightarrow OD = \frac{1}{2}AO = \frac{3}{2}$$

So, other vertices of triangle have coor din a t es,



\ Equation of line BC is :

$$x=-\frac{a}{2}$$
 $b^{2}x + a = 0$

120. (a) we have, f(x)=x-|x-x2|=x-|x(1-x)|=x-|x||1-x|, Continuity is to be checked at x = 0 and x =١ 1. At x = 0 $LHL = \underset{h \circledast 0}{\text{lim}} f(0-h) = \underset{h \circledast 0}{\text{lim}} h-l-h \|1+h\|$ $=\lim_{h\to h}(1+h)=0$ h®0 $RHL = \lim_{h \Subset 0} f(0+h) = \lim_{h \circledast 0} -|h||1$ h| h®0 =limh-h(1-h)=0 h®0 and f(0) = 0Since LHL = RHL = f(0), $\int f(x)$ is continuous at x = 0. At x = 1LHL = $\lim_{h \otimes 0} f(1 - h) = \lim_{h \otimes 0} (1 h) |1 h||1 (1 - h)|$ $= \lim(1 h) h(1 h) 4 =$ h® 0 $\frac{\text{Similarly RHL}}{1 + h} =$ and f(1)=1-|1|.|1-1|=1 f(x) is continuous at x = 1١ Hence f(x) is continuous for all [x, 1, 1]121. (d) Let $P(n) : \frac{4^n}{n+1} < \frac{2n}{n!} + \frac{4^n}{2}$ For n = 2. $P(2): \frac{4^2}{2+1} < \frac{4!}{(2)2} \Rightarrow \frac{16}{3} < \frac{24}{4}$ which is true. Let for $n = m^{3} 2$, P(m) is true. i.e. $\frac{4m}{m+1} < \frac{(2m)!}{(m!)2}$ Now, $\frac{4^{m+1}}{m+2} = \frac{4^m}{m+1} \cdot \frac{4(m+1)}{m+2}$ $<\frac{(2m)!}{(m!)!}\cdot\frac{4(m+1)}{(m+2)}$

$$= \frac{(2m)!(2m + 1)(2m + 2)4(m + 1)(m + 1)^2}{(2m + 1)(2m + 2)(m + 2)(m + 1)2(m + 2)}$$

 $=\frac{[2(m+1)]!}{[(m+1)!]2} \cdot \frac{2(m+1)^2}{(2m+1)!(m+2)}$ $< \frac{[2(m+1)]!}{[(m+1)!]2}$ Hence, for $n^2 2$, P(n) is true. 122. (b) $D = \begin{vmatrix} -a & 1 & 1 \\ 1 & -b & 1 \\ 1 & 1 & -c \end{vmatrix} = 0$ for non-zero solution Pabc - a - b - c - 2 = 0P abc = a + b + c + 2Now, $\frac{1}{1+2} + \frac{1}{1+b} + \frac{1}{1+c}$ $=\frac{3+2(a \ b+c)+(ab+bc+ac)}{1+(a+b+c)+(ab+bc+ac)+abc}$ $=\frac{3+2(a+b+c)+(ab+bc+ac)}{1+2(a+b+c)+2+ab+bc+ac}=1$ 123. (b) A function f(x) is said to be increasing function in [a, b] if f'(x) > 0 in [a, b]. (i) Given f(x) = xxDifferentiate equation (i) $f'(x) = xx (1 + \log x)$ Put f'(x) = 0 $0 = xx \left(1 + \log x\right)$ \flat x =0, logx = -1 \flat x = ^{e-1} $\flat x = \frac{1}{2}, 0$ Now, $\inf_{\ddot{e}} \hat{e}_{0,1}^{\dot{1}\dot{u}}, fx() > 0$ f (x) is increasing in intervation, e_{ij}^{1} 124. (d) Let $y = \frac{x}{x^2 - 5x + 9}$ $x^2y - (5y + 1)x + 9y = 0$ for real x, Discriminant = $b2 \overline{a}c^{4_3} 0$ (5y + 1)2 - 36y2 > 0(5y + 1 - 6y)(5y + 1 + 6y) > 0

125. (d) Putting
$$x = \frac{1}{y}$$
, we get

$$L = \lim_{y \ge 0} \xi \frac{a_1^y + a_2^y + \dots + a_n^y}{n} \dot{c}^{n/y} \dot{c}^{n/y$$

$$\log L = \lim_{y \otimes 0} \frac{n}{y} \frac{1}{\log a_1} \left(a_1^y + a_2^y + \dots + a_n \frac{a_n}{e_0} \right)$$
$$= n \lim_{y \otimes 0} \frac{\frac{a_1^y \log a_1 + a_2^y \log a_2 + \dots + a_n^y \log a_n}{\frac{a_1^y + a_2^y + \dots + a_n^y}{1}} \frac{a_1^y + a_2^y + \dots + a_n^y}{1} \right)$$
$$[using Let Honizal rule]$$

[using L¢Hopital rule]

$$= n. \frac{\log(a1a2...a_n)}{n}$$

\ \log L =\log(a_1.a2...an) \P L = a1.a2.a3....a_n

126. (d) We have
$$\cot^{-1}7 + \cot^{-1}8 + \cot^{-1}18$$

$$Q xy = \frac{1}{7} \cdot \frac{1}{8} < 1$$

$$\sqrt{\frac{\tan^{-1} \frac{1}{7} + \frac{\tan^{-1} \frac{1}{8} + \tan^{-1} \frac{1}{18}}{\frac{1}{7} + \frac{1}{8} + \frac{\ddot{0}}{\dot{5}} + \frac{\dot{1}}{8}}}{\frac{\tan^{-1} \frac{1}{18} + \tan^{-1} \frac{1}{18} + \tan^{-1} \frac{1}{18} + \tan^{-1} \frac{1}{18}}{\frac{\sin^{-1} \frac{1}{7} + \frac{1}{8}}{\frac{5}{6}} + \tan^{-1} \frac{1}{18}}$$

$$also; \frac{also}{-1} \times \frac{1}{8} < 1$$

$$\xi$$

$$\tan^{-1} \frac{3}{11} + \tan^{-1} \frac{1}{18} = \tan^{-1} \frac{a}{5} + \frac{1}{11} + \frac{\ddot{0}}{5} + \frac{\ddot{0}}{11} + \frac{\ddot{0}}{11} + \frac{\ddot{0}}{8} + \frac{\dot{0}}{5} + \frac{1}{11} + \frac{\ddot{0}}{8} + \frac{\dot{0}}{5} + \frac{1}{11} + \frac{\ddot{0}}{8} + \frac{\dot{0}}{5} + \frac{1}{11} + \frac{\ddot{0}}{11} + \frac{\ddot{0}}{1}$$

127. (a) Let, I =
$$\partial_{sinx+1}^{cosx-1}$$
 ex dx
= $\partial_{e}^{e} \frac{cosx}{e^{sinx+1}} - \frac{1}{sinx+1} \dot{u}^{e^{x}} dx$
= $\partial_{1}^{e^{x}} + sinx - \partial_{sinx+1}^{u^{1}} ex dx$
= $e^{x.cosx} - \partial_{1}^{c(1+sinx)sinx-cos2x} exdx$
 $- \partial_{sinx+1}^{e^{x}} dx$
= $\frac{e^{x}cosx}{1+sinx} - \partial_{1}^{c(1+sinx)sinx-cos2x} exdx$
 $- \partial_{sinx+1}^{e^{x}} dx$
= $\frac{e^{x}cosx}{1+sinx} + \partial_{1}^{e^{x}} dx + s \partial_{1}^{e^{x}} dx$
= $\frac{e^{x}cosx}{1+sinx} + C$
 $e^{Using} \partial_{1}^{e^{x}} + C$
 $e^{Using} \partial_{1}^{e^{u^{x}}} + C$
 $e^{Using} \partial_{1}^{e^{Using}} + C$
 $e^{Using} \partial_{1}^{e$

 $x=2n p \pm \frac{2p}{3}, n\hat{H}$ Þ Hence the required general solution are 2n

132.

134.

x= (2m 4)
$$\frac{p}{4}$$
 and x=2n p $\pm \frac{2p}{4}$
130. (b) y = |cos x - sin x|
Y
f(x) = cos x g(x) = sin x
p/4 p/2
Required area = $\frac{2}{0}(cos x - sin x)dx$
= 2[sink + cos x] $\frac{p}{4}$
= 2 $\frac{e}{2}\frac{2}{\sqrt{2}}$ $\hat{h}_{u} = (2\sqrt{2} - 2)sq.units$
131. (a) We have,

$$Lf \notin (0) = \lim_{h \otimes 0} \frac{f(0 - h) - f(0)}{-h} = \lim_{h \otimes 0} \frac{-h \log \cosh}{-h \log (1 + h2)}$$
$$= \lim_{h \otimes 0} \frac{\log \cosh}{\log (1 + 2h)} \qquad \stackrel{\text{and}}{\stackrel{\text{ch}}}}\stackrel{\text{ch}}{\stackrel{\text{ch}}{\stackrel{\text{ch}}{\stackrel{\text{ch}}{\stackrel{\text{ch}}{\stackrel{\text{ch}}{\stackrel{\text{ch}}{\stackrel{\text{ch}}{\stackrel{\text{ch}}{\stackrel{\text{ch}}{\stackrel{\text{ch}}}}}}}}}{\frac{a}{a}} \int form \frac{\ddot{o}}{o}$$

$$= \lim_{h \ge 0} \frac{-\tan h}{2h/(1+2h)} = -1/2$$

$$\operatorname{Rf} \phi(0) = \lim_{\substack{h \otimes 0 \\ \lim \end{array}} \frac{f(0+h) \cdot f(0)}{h}}{\lim_{\substack{h \otimes 0 \\ \lim \end{array}} \frac{h \otimes 0}{\log(1+h)^{2}}} = \lim_{\substack{h \otimes 0 \\ \underset{\substack{h \otimes 0 \\ h \otimes 0 \\ \underset{\substack{h \otimes 0 \\ h \otimes 0 \\ \frac{h \otimes 0}{2h/(\frac{1}{2}+h)}}} = \frac{\underset{\substack{e \in 0 \\ \underset{\substack{h \otimes 0 \\ e \\ 0 \\ \frac{e}{2h/(\frac{1}{2}+h)}}}{\lim_{\substack{h \otimes 0 \\ \frac{e}{2h/(\frac{1}{2}+h)}}} = \frac{-1}{2}$$

Since Lf(0) = Rf(0), therefore f(x) is differentiable at x = 0



top will be
$$(5/4)k$$
. S = $(2prh)k + (pr2)$
(5/4)k ('S' is vol. of material used)

orS =
$$2\beta k. \frac{V}{p^{r2}} + \frac{5}{4}p^{r2k} = k\frac{\partial^2 V}{\partial t} + \frac{5}{4}p^{r2} \frac{\ddot{Q}}{\dot{Q}}$$

 $\setminus \frac{dS}{dr} = k\frac{\partial^2 V}{\xi^2} + \frac{5}{2}p^2 \frac{\ddot{Q}}{\dot{Q}} \setminus r^3 = 4V/\mathfrak{P}$
 $\frac{d2S}{dr2} = k\frac{\partial^4 V}{\xi r^3} + \frac{5}{2}p\frac{\ddot{Q}}{\dot{Q}}, = \frac{15}{2}kp = \text{positive}$
When $r^3 = 4V/\mathfrak{F}$ or $5pr^3 = 4pr2h.$
 $\frac{r}{h} = \frac{4}{5}.$
(d) We have
 $n (A \not{E} B \not{E} C) = n (A) + n (B) + n (C)$

ン) B) - n(BCC) - n(CCA)– n (A Ç $+ n (A \zeta B \zeta C)$

= 10 + 15 + 20 - 8 - 9 - n (Ç A) + n (AÇ Q C) = $28 - \{n(C C A) - n (A C B C C)\}$...(i) Since n (C C A)³ n (A Q C C) We have n (C C A) - n (A C C C)³ From (i) and (ii) ...(ii)

n (AÈ B C) 28 ...(iii) Now, n(AÈ B) = n (A) +n (B) -n (A B) = 10 + 15 - 8 = 17 and n (BÈ C) = n (B) + n (C) - n (B C) = 15 + 20 - 9 = 26 Since, n (AÈ BÈ C) n (A È C) and n (AÈ BC) n (B È C), we have n (AÈ BC) n (B È C), we have n (AÈ BC) n (A È C) and n (AÈ BC) 26 Hence n (AÈ BC) 26 ...(iv) From (iii) and (iv) we obtain 26 f (A È BC) 22 Also n (AÈ BÈ C) is a positive integer n (AÈ BC) = 26 or 27 or 28

135. (a)
$$z = 1 + 2i |z| = \sqrt{1 + 4} = \sqrt{5}$$

$$\int f(z) = \frac{7 \cdot z}{1 \cdot z^2} = \frac{7 \cdot 1 \cdot 2i}{1 \cdot (1 + 2i)^2}$$
$$= \frac{6 \cdot 2i}{1 \cdot (1 - 4 + 4i)} = \frac{6 \cdot 2i}{4 \cdot 4i} = \frac{3 \cdot i}{i} = \frac{3 \cdot i}{2 \cdot 2i}$$
$$P|f(z)| = \left|\frac{3 \cdot i}{2 \cdot 2}\right| = \frac{|3 \cdot 2i|}{i|2 \cdot 2}$$
$$= \frac{\sqrt{9 + 1}}{\sqrt{4 + 4}} = \frac{\sqrt{5}}{2} = \frac{|z|}{2}$$

136. (b) Let
$$f(x) = \cos{-\frac{\acute{e}l - (\log x)^2 \acute{u}}{\acute{e}4}} (\log x)^2 \acute{u}$$

$$Put \log x = t \text{ in } f(x)$$

$$f(x) = \cos^1 \frac{e^{1} - t^2 \dot{u}}{e^{1} + t \dot{u}}$$

Now, put t = tanq, we get

$$f(x) = \cos - e^{i \left[\begin{array}{c} -i \left[2 + i \right] n q \right] \hat{u}} \\ \hat{e}^{i} + i \left[1 + i \left[2 + i \right] \hat{u} \right] \\ \hat{e}^{i} = \cos - 1 \left[\cos 2 \right] = 2 q = 2 \tan^{-1} t = 2$$

tan–1 (log x) Diff. both side w.r.t 'x', we get

$$f'(x) = 2\frac{1}{1 + (\log x)2} \frac{1}{x}$$

Now,

$$f'(e) = 2 \cdot \frac{1}{1 + (\log e)^2} \cdot \frac{1}{e} = \frac{1}{e}$$

$$(Q\log e = 1)$$

137. (d) Number form by using 1, 2, 3, 4, 5 = 5! = 120 Number formed by using 0, 1, 2, 4, 5

Total number formed, divisible by 3 (taking numbers without repetition) = 216Statement 1 is false and statement 2 is true.

138. (c) Any tangent to parabola $y_2 = 8x$ is

$$y = mx + \frac{2}{m} \dots (i)$$

It touches the circle 2+2xy-12x+4=0, if the length of perpendicular from the centre $\sqrt{}$ (6, 0) is equal to radius 32. $\frac{6m + \frac{2}{m}}{\sqrt{m^2 + 1}} = \pm \sqrt{32} \overset{\text{pag}}{\stackrel{\text{e}}{\text{e}}} 3m + \frac{1}{m} \overset{\text{o}}{\overset{\text{o}}{\text{o}}}^2 = 8(m2 + 1)$ (3m2 + 1)2 = 8(m4 + m2)

 $\begin{array}{l} \flat & (3m2 + 1)2 = 8(m4 + m2) \\ \flat & m4 - 2m2 + 1 = 0 \ \flat \ m = \pm 1 \\ & \text{Hence, the required tangents are } y = x + 2 \\ & \text{and } y = -x - 2. \end{array}$

$$R(s)R(t) = \begin{cases} e \cos s & \sin t \\ e \sin s & e \sin t \\ e \sin s & \cos t \\ e \sin s & \cos t \\ e \sin s & \cos t \\ e \sin s \sin t & \cos t \\ e \cos s \sin t + \sin s \cos t \\ e \sin s \sin t + \cos s \cos t \\ e \sin s \sin t + \cos s \cos t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \sin s \sin t \\ e \cos s \cos t \\ e \sin s \sin t \\ e \sin$$

$$\begin{array}{l} \stackrel{e}{=} \frac{e}{e} \cos(s+t) & \sin(s+t)\dot{u} \\ \stackrel{e}{=} \frac{e}{e} \sin(s+t) & \cos(s+t)\dot{u} \\ \end{array} R(s+t)$$

140. (d)
$$\mathbf{\check{O}}^{\mathbf{x}} \log \mathbf{\check{e}}^{\mathbf{\check{e}}} + \frac{1}{\mathbf{x}} \frac{\ddot{\mathbf{y}}}{\mathbf{\check{e}}} dx$$

$$= \log_{\mathbf{\check{e}}} + \frac{1}{\mathbf{x}} \frac{\dot{\mathbf{x}}^{2}}{\mathbf{\check{g}}} - \mathbf{\check{O}}^{\mathbf{x}} + 1\mathbf{\check{e}} \mathbf{\check{e}}^{\mathbf{\check{e}}} - \frac{1}{\mathbf{x}^{2}} \frac{\ddot{\mathbf{x}} \cdot \mathbf{\check{e}}}{\mathbf{\check{e}}} - \frac{1}{\mathbf{x}^{2}} \frac{\ddot{\mathbf{x}} \cdot \mathbf{\check{e}}}{\mathbf{\check{e}}} dx$$

$$= \frac{x^{2}}{2} \log_{\mathbf{\check{e}}} \frac{\mathbf{\check{e}}^{\mathbf{x}+1\ddot{o}}}{\mathbf{\check{e}}} \frac{\dot{\mathbf{x}}^{2}}{2} + \frac{1}{2} \frac{\mathbf{x}+1-1}{\mathbf{\check{e}}} dx$$

$$= \frac{x^{2}}{2} \log_{\mathbf{\check{e}}} \frac{\mathbf{\check{e}}^{\mathbf{x}+1\ddot{o}}}{\mathbf{\check{e}}} \frac{\dot{\mathbf{x}}^{2}}{2} + \frac{1}{2} \frac{\mathbf{x}+1-1}{\mathbf{\check{e}}} dx$$

$$= \frac{x^{2}}{2} \log_{\mathbf{\check{e}}} \frac{\mathbf{\check{e}}^{\mathbf{x}+1\ddot{o}}}{\mathbf{\check{e}}} \frac{\mathbf{\check{e}}^{\mathbf{x}+1\ddot{o}}}{\mathbf{\check{e}}} - \frac{1}{2} - \log(\mathbf{x}+1) + c$$

$$= \frac{\mathbf{\check{e}}}{\mathbf{\check{e}}} \frac{x^{2}-1}{2} \frac{\mathbf{\check{e}}}{\mathbf{\check{e}}} \log(\mathbf{x}+1) - \frac{x}{2} \log \mathbf{x} + \frac{1}{2} \mathbf{x} + c$$

141. (c) OA=a, OB=b&OC=c are unit vectors and equally inclined to each other at an acute angle q.



\ ABC is an equilateral triangle

and AB=
$$\sqrt{OA^4OB^2}$$
 2OA.OB.cosq
= $\sqrt{2} \cdot 2\cos q = \sqrt{2}\sqrt{1-\cos q}$
Area of DABC
= $\frac{\sqrt{4}}{4}AB^2 = \frac{\sqrt{3}}{4} \cdot 2(1-\cos q) = \frac{\sqrt{3}}{2}(1-\cos q)$
If G is the centroid of the D ABC, then
 $OG = \frac{1}{3} |_a^r + \frac{r}{b} |_c^r$
1
= $3\sqrt{a^2+b^2+c^2+2a.b+2b.c+2c.a}$

$$=\frac{1}{\sqrt{3}}\sqrt{1+2\cos q}$$

[dbc] = Volume of parallelopiped

= OG \times 2 ar (D ABC)

$$= 2 \cdot \frac{1}{\sqrt{3}} \sqrt{1 + 2\cos q} \cdot \frac{\sqrt{3}}{2} (1 - \cos q)$$

$$= (1-\cos q) \sqrt{1+2\cos q}$$
142. (b) The given product

$$= \frac{1}{2^4} + \frac{2}{8} + \frac{3}{16} + \frac{4}{2} + 2... = 2s \text{ (say)}$$
Now S = $\frac{1}{4} + \frac{2}{8} + \frac{3}{16} + \frac{4}{32} + ... \dots \dots \dots (1)$
P $\frac{1}{2}$ S = $\frac{1}{8} + \frac{1}{16} + \frac{3}{32} + ... \dots \dots \dots (2)$
Apply: (1) – (2)
P $\frac{1}{2}$ S = $\frac{1}{4} + \frac{1}{8} + \frac{1}{4} + 6 + ... \dots$

$$= \frac{1/4}{1 + 1/2} = \frac{1}{2} \qquad \forall S = 1$$

$$p = \frac{1-1/2}{2} = 2$$

143. (a)
$$\frac{{}^{n}C_{r}}{{}^{r+3}C_{r}} = 3! \frac{1}{(r+3)(r+2)(r+1)} \cdot \frac{{}^{n}C_{r}}{(n+1)}$$

$$= 3! \frac{1}{(r+3)(r+2)} \cdot \frac{{}^{n+1}C_{r+1}}{(n+1)} [See Formulae]$$

$$= 3! \frac{1}{(r+3)(n+1)} \frac{{}^{n+1}C_{r+1}}{r+2}$$

$$= 3! \frac{3!}{(r+1)(n+2)} \cdot \frac{{}^{n+2}C_{r+2}}{n+2}$$

$$= \frac{3!}{(n+1)(n+2)(n+3)} \cdot \frac{{}^{n+2}C_{r+3}}{r+3}$$

$$= \frac{3!}{(n+1)(n+2)(n+3)} {}^{n+3}C_{r+3}$$

$$\land \qquad \underset{r=0}{\overset{a}{\rightarrow}} (-1)r \frac{{}^{n}C_{r}}{{}^{r+3}C_{r}}$$

$$= \frac{6}{(n+1)(n+2)(n+3)} \bigoplus_{r=0}^{n} (-1)^{r} \sum_{r=3}^{n+3} C_{r+3}$$

$$= \frac{6}{(n+1)(n+2)(n+3)} \sum_{r=0}^{n+3} C_{1} + \dots + (1)^{n+3} C_{1} + \sum_{r=3}^{n+3} C_{1} + \dots + (1)^{n+3} C_{1} + \sum_{r=3}^{n+3} C_{1} + \dots + (-1)^{n+3} C_{1} + \sum_{r=3}^{n+3} C_{1} + \sum_{r=3}^{n+3}$$

Similarly P(B/A) =
$$\frac{{}^{3}C_{2}}{C2} = \frac{3}{10}$$
,
P(B/A 4) = $\frac{{}^{4}C_{2}}{5C_{2}} = \frac{3}{5}$
P(B/A 5) = $\frac{{}^{5}C_{2}}{5C_{2}} = 1$.
By Bave's theorem.

,

$$P(A5/B) = \frac{P(A5)P(B/A5)}{P(A2)P(B/A2)+P(A3)P(B/A3)} + P(A4)(B/A4)+P(A5)P(B/A5)$$

$$=\frac{4.1}{\frac{1}{4} \stackrel{\text{é}1}{\underset{\text{e}10}{\text{e}10}} + \frac{3}{10} + \frac{3}{5} \stackrel{\text{i}3}{\underset{\text{f}}{\text{i}}} = \frac{10}{20} = \frac{1}{2}.$$

146. (b) As given plane $x + y - z\frac{1}{2}$ divides the line joining the points A (2, 1, 5) and B (3, 4, 3) at a point C in the ratio k : 1. 1 P

$$\begin{array}{c} k \\ C \\ \end{array} \begin{pmatrix} 1 \\ B \\ B \\ (3, 4, 3) \\ \end{array}$$

A• (2, 1, 5)

Then coordinates of C
$$a^{3}k+2$$
 4k+1 $3^{3}k+5$ $\ddot{0}$

$$\underbrace{k+1}_{k+1}, \underbrace{k+1}_{k+1}, \underbrace{k+1}_{\phi}$$

Point C lies on the plane,

Coordinates of C must satisfy the equation of plane.

So,
$$\underbrace{\underbrace{a}_{k+1}^{\otimes k+2} \overset{\otimes}{e}_{k+1}^{\otimes k+2} \overset{\otimes}{e}_{k+1}^{\otimes k+1} \overset{\otimes}{\varphi}_{k+1}^{\otimes k+1} \overset{\otimes}{\varphi}_{k+1}^{\otimes k+1} \overset{\otimes}{\varphi}_{k+1}^{\otimes k+2} \overset{\otimes}{\varphi}_{k+1}^{\otimes$$

$$P \quad 3k + 2 + 4k + 1 - 3k - 5 = (k+1)$$

^b
$$4k - 2 = \frac{1}{2}(k + 1)$$

 \flat 8k – 4 = k + 1 \flat 7k = 5

$$k = \frac{5}{7}$$

Ratio is 5 : 7.

rn)e en equally likely we have $P(\underline{A}) \doteq P(\underline{A}) = P(\underline{A})$

$$(A_{4}) = P(A_{5}) = \frac{1}{4}$$

P(B/A) is probability of event that the urn contains 2 white balls and both have been drawn.

$$P(B/A) = \frac{{}^{2}E_{2}}{{}^{5}E_{2}} = \frac{1}{10}$$

147. (c) Let I =
$$\overset{p/2}{\underset{0}{\circ}} \frac{\sqrt{\sin x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx$$
 ... (i)

Th en,

$$I = \bigotimes_{0}^{p/2} \frac{\sqrt{\sin(p/2 - x)}}{\sqrt{\sin(p/2 - x)} + \sqrt{\cos(p/2 - x)}} dx$$
$$\Rightarrow I = \bigotimes_{0}^{p/2} \frac{\sqrt{\cos x}}{\sqrt{\cos x} + \sqrt{\sin x}} dx$$

Þ

$$\overset{p/2}{\overset{}{}_{0}} \underbrace{\frac{-\sqrt{\sin x}}{\sqrt{\cos x} + \sqrt{\sin x}}}_{0} dx + \overset{p/2}{\overset{}{\underset{}{}_{0}}} \frac{\sqrt{\cos x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx$$

$$\overset{0}{\overset{}{\underset{}{}_{0}}} \underbrace{\overset{0}{\sqrt{x} + \sqrt{\cos x}}}_{\sqrt{x} + \sqrt{\cos x}} dx = \overset{0}{\overset{0}{\underset{}{}_{0}}} 1.dx = [x]_{0}^{p/2} = \overset{p}{2} - 0$$

$$\overset{sin}{\overset{sin}{\overset{}{\underset{}{}_{0}}}} \underbrace{\overset{p/2}{\sqrt{\sin x} + \sqrt{\cos x}}}_{\sqrt{y} - x} dx = \overset{p}{4}$$

148. (a) Let the required vector be

and
$$\sqrt[4]{i^{+}+j^{+}+4k} = 8 \not = 2x + y + 4z = 8 ...(iii)$$

Subtracting (ii) from (i), we have
 $-2y - z = -5 \not = 2y + z = 5$...(iv)
Multiply (ii) by 2 and subtracting (iii) from
it, we obtain

5y - 8z = 2 ...(v) Multiply (iv) by 8 and adding (v) to it, we have 21y = 42 P y = 2 ...(v) Substituting y = 2 in(iv), we get $2 \times 2 + z = 5 P z = 5 - 4 = 1$ Substituting these values in (i), we get x + 2 - 3 = 0 P x = 3 - 2 = 1

$$r_{V} = xi_{+}^{2}yj_{+}^{2}zk_{-}^{2}i_{+}^{2}2j_{+}^{2}k_{-}^{2}$$

149.(c)Equation of lines are $\begin{cases} x \\ a \end{cases} = \begin{cases} y \\ b \end{cases} = 1 \text{ and } \end{cases}$

$$\frac{x}{b} - \frac{y}{a} = 1$$

$$pm1 = \frac{b}{a} \text{ and } m_2 = \frac{a}{b}$$

Therefore

$$q = \tan^{-1} \frac{\frac{b}{a} \cdot \frac{a}{b}}{1 + \frac{a}{b} \cdot \frac{a}{b}} = \tan^{-1} \frac{b^2 \cdot a^2}{2ab}$$

150. (d) Given points are A (k, 1, -102kB 0, 2)
and C (2 + 2k, k, 1)
Let rl = length of line
$$AB = \sqrt{(2k - k)^2 + (0 - 1)^2 + (2 +)^2} 1$$
$$= \sqrt{\frac{k^2 + 10}{r_2 \ k}} = \text{length of line BC}$$
$$= \sqrt{(2)2 + (-1)^2}$$
$$= \sqrt{k^2 + 5}$$
Now, let 11, m1, n1 be direction-cosines of

line ABand l

cosines of BC. Since AB is perpendicular to BC \ | 112+m1m2+n1n2=0

Now,
$$_{1}1 = \frac{k}{\sqrt{k^{2} + 10}}$$
, $m_{1} = \frac{-1}{\sqrt{k^{2} + 10}}$,
 $n_{1} = \frac{3}{\sqrt{k^{2} + 10}}$

and
$$|_{2} = \frac{2}{\sqrt{k+5}}, m_{2} = \frac{k}{\sqrt{k^{2}+5}}, \frac{-1}{\sqrt{k^{2}+5}}$$

So, $|_{1} |_{2} + m m_{2}, m_{1} |_{2} = 0$

$$\frac{2k}{\sqrt{k^2+10\sqrt{k^2+5}}} - \frac{k}{\sqrt{k^2+10\sqrt{k^2+5}}} - \frac{3}{\sqrt{k^2+10\sqrt{k^2+5}}} = 0$$

$$\Rightarrow \quad 2k - k - 3 = 0$$

$$\Rightarrow \quad k = 3$$

Fork = 3, ABis perpendicular t**B**C.