VITEEE 2006 Question Paper

Vellore Institute of Technology Engineering Entrance Examination

SOLVED PAPER

2006

PART - I (PHYSICS)

- 1 A potential difference of 300 V is applied to a combination of $2.0\mu F$ and $8.0 \mu F$ capacitors connected in series. The charge on the $2.0\mu F$ capacitor is
 - (a $2.4 \times 10-4C$ (b) $4.8 \times 10-4C$) $7.2 \times 10-4C$ (d) $9.6 \times 10-4C$
 -) $7.2 \times 10-4$ C (d) $9.6 \times 10-4$ C
- T(cw)o point charges 4C and 2C are separated by a distance of 1 m in air. Then the distance of the point on the line joining the charges, where the resultant electric field is (a) 0.75
 (c) 0.67
 (d) 0.81
- Figure shows a triangular array of three point charges. The electric potential V of these source charges at the midpoint P of the base of the triangle is
 6.



A current of 5A is passing through a metallic wire of cross-sectional area 4 × 10-6m2. If the density of the charge carriers in the wire is 5 × 1026m-3, the drift speed of the electrons will be [e = 1.602 × 10-19C] (a) 1.56×10-2ms-1 (c) (b2) .14.29×81×01-02-

m2ms-s1-1 The

5. series combination of(dt)w 20.8 c4a×p1a0cit2omrss-s1hown in figure is connected across 1000V. The magnitude of the charges on the capacitors will be



(a
$$3 \times 10-9$$
 C (b) $2 \times 10-9$ C
) $2.5 \times 10-9$ C (d) $3.5 \times 10-9$ C

T(achr)eree resistances of values 2add 6 to be connected to produce an effective resistance of 4 . This can be done by connecting

- (a) 6 resistance in series with the parallel
- combination of 2 and 3 (b) 3 resistance in series w
- b) 3 resistance in series with the parallel
- (c) combination of 2 and 6
- (d) 2 resistance in series with the parallel combination of 3 and 6
 2 resistance in parallel with the parallel combination of 3 and 6
- 7. The resistance of a field coil measures 50 at 20°C and 65 at 70°C. The temperature coefficient of resistance is
 - (a) 0.0086/°C (b) 0.0068/°C
 - (c) 0.0096/°C (d) 0.0999/°C
- 8. The electrolyte used in Lechlanche cell is
 - (a) copper sulphate solution
 - (b) ammonium chloride solution
 - (c) dilute sulphuric acid
 - (d) zinc sulphate

9. A galvanometer has a resistance of 50 resistance of 1 is connected across its terminals, the total current flow through the ga rlevparneosmenetse rt hise [mIaximum current that can be passed through the galvanometer] (a 12 (bd))535IgIg1

- 10. I(cn) a 4t6angent galvanometer, a current of 1A produIces a deflection of 30°. The current required to produce a deflection of 60° is
 - (a) 3A (b) 2A
 - (c) 4A (d) 1A
- 11. In the presence of magnetic field 'B' and electric field 'E', the total force on a moving charged particle is
 - (a) F v[(q B) E]
 - q[(v E) B]
 - (c) q[(v B) E] F
 - (d) F B[(q E) v]
- 12. A circular coil of radius 40 mm consists of 250 turns of wire in which the current is 20mA. The magnetic field in the center of the coil is [= $4 \times$ 10-7 Hm-1]
 - 0.785 (b) 0.525 (a (d) G G
- 13. (RcM)S Ova.6lu2e9 of AC is 0 o.9f 0th0e peak vetore? (a) 7%G (b) 7.G7% (c) 70% (d) 70.7%
- 14. O-factor can be increased by having a coil of
 - (a) large inductance, small ohmic resistance
 - large inductance, large ohmic resistance (h)
 - small inductance, large ohmic resistance (c)
- (d) small inductance, small ohmic resistance 15. A small piece of metal wire is dragged across the gap between the pole pieces of a magnet in 0.5 second. The magnetic flux between the pole pieces is known to be $8 \times 10-4$ Wb. The emf induced in the wire is
 - (a) 16 m V
 - (b) 1.6 V (c) 1.6 m V (d) 16V
- 16. Current in the LCR circuit becomes extremely large when
 - (a) frequency of AC supply is increased
 - (b) frequency of AC supply is decreased
 - inductive reactance becomes equal to (c)
 - capacitive reactance inductance becomes equal to capacitance (d)

- . If a 17. Our eyes respond to wavelengths ranging from (a) (b**400** nm to 700
 - (d) nm 700 nm to 800 nm 0 to ŧo +
 - 18. A new system of units is evolved in which the values of 0 and 0 are 2 and 8 respectively. Then the speed of light in this system will be
 - (a) 0.25 (b) 0.5
 - (c) 0.75 (d) 1
 - 19. A ray of light strikes a piece of glass at an angle of incidence of 60° and the reflected beam is completely plane polarised. The refractive index of glass is

(a)
$$2\sqrt{3}$$
 (b) $\sqrt{3}$
(c) $\frac{\sqrt{3}}{2}$ (d) $\frac{1}{2}$

- 20. In an experiment on Newton's rings, the diameter of the 20th dark ring was found to be 5.82mm and that of the 10th ring 3.36 mm. If the radius of the plano-convex lens is 1 m, the wavelength of light used is
 - (a) 5646 A^o (b) 5896 A^o (d) 5900 A° (c) 5406 A^o
- 21. What is the angular momentum of an electron in the fourth orbit of Bohr's model of hydrogen
 - 2h ^(a) 2 (b) h (c) h (d)
- The transition of an electrom from 2 n = 5,6, 22. to n1 = 4 gives rise to
 - (a) Pfund series (b) Lyman series
 - (c) Paschen series (d) Brackett series
- 23. The ground state energy of hydrogen atom is -13.6 eV. What is the potential energy of the electron in this state?
 - (a -27.2 (b) -13.6 eV
 - (d) 0 eV eV)
- 24. T(ch)e l+on1g3e.6st wavelength that can be analysed by a seoV dium chloride crystal of spacing d = 2.82A° in the second order is
 - (a 2.82 (b) 5.64 A^o
 - A٥ (d) 11.28 A°)
 - (c) 8.46 A٥

25. Which is the incorrect statement of the following?

P(ah)oton is a particle with zero rest mass P(bh)oton is a particle with zero momentum P(ch)otons travel with velocity of light in vacuum

P(dh)otons even feel the pull of gravity

- The deBroglie wavelength associated with a 26. steel ball of mass 1000 gm moving at a speed of $1 \text{ ms}-1 \text{ is } [h = 6.626 \times 10-34 \text{ Js}]$
 - 6.626 × 10-(b) 6.626 × 10–37m (a
 - 31m 6.626 × (d) 6.626 × 1034m
- 27. T(ch)e v1e0lo-c3it4ym v, at which the mass of a particles an amplifier with proper negative feedbackdouble its rest mass is

(a)
$$v = c$$
 (b) $v \sqrt{\frac{3}{2}} dc$
(c) $v \sqrt{\frac{3}{2}} c$ (d) $v = 2c$

- 28. How much energy is produced, if 2 kg of a substance is fully converted into energy? $[c = 3 \times 108 \text{ ms} - 1]$
 - (a) 9 × 1016 J (b) 11 × 1016 J
 - (c) 15 × 1016 J (d) 18 × 1016 J
- 29. The difference between the rest mass of the nucleus and the sum of the masses of the nucleons composing a nucleus is known as
 - (a) packing fraction(b) mass defect
 - (c) binding energy (d) isotopic mass
- 30. The half life period of Radium is 3 minute. Its mean life time is

- (c) 6 minute (d) (3 × 0.6931) minute
- 31. 'Pair production' involves conversion of a photon into
 - (a) a neutron-electron pair
 - (b) a positron-neutron pair
 - (c) an electron-proton pair (d) an electron-positron pair
- 32. The sub atomic particles proton and neutron fall under the group of
 - (a) mesons (b) photons
 - (c) leptons (d) baryons

- 33. When the conductivity of a semiconductor is only due to the breaking up of the covalent bonds, the semiconductor is known as (a) donor (b) extrinsic

 - (c) intrinsic (d) acceptor
- 34. In a P-type semiconductor, the acceptor impurity produces an energy level
 - (a) just below the valence band
 - (b) just above the conduction band
 - (c) just below the conduction band
 - (d) just above the valence band
- 35. An oscillator is essentially
 - - network circuits (c)
 - converts alternating current into direct (d) cur r en t an amplifier with no feedback network an amplifier with proper positive feedback network circuits
- 36. Which of the following gates can perform perfect binary addition?
 - (a) AND gate (b) OR gate
 - (c) EXOR gate (d) NAND gate
- 37. The frequency of an FM transmitter without signal input is called

 - (a) the centre frequency
 - (b) modulation factor
 - (c) the frequency deviation
 - (d) the carrier swing
- 38. The fundamental radio antenna is a metal rod
 - which has a length equal to
 - in free space at the frequency of operation (a)
 - in free space at the frequency of (b) operation
 - (c) in free space at the frequency of operation
 - 2

(d)
$$\begin{array}{c} 3 \\ 4 \end{array}$$
 in free space at the frequency of

operation

39. Vidicon works on the principle of

- (a) electrical conductivity
- (b) photoconductivity
- (c) thermal conductivity
- (d) SONAR

- 40. The maximum range, dmax, of radar is
 - proportional to the cube root of the peak (a)
 - (b) transmitted power
 - proportional to the fourth root of the peak (c) transmitted power
 - proportional to the square root of the peak (d) transmitted power not related to the peak transmitted power

at all

PART - II (CHEMISTRY)

- 41. **Tobe**assieurorivalent weight of permanganate when it acts as oxidising agent in ferrous ion estimation is (a) 158 (b) 31.
 - (c) 79 (d) 6
- The magnetic moment of l3a9n.thanide ions is 42. determined from which on5e of the following relation?
 - (a) √n(n 2) (b) gJ(J 1)
 - (c) (d) 2 ŋ(n – g ŋ(n 1) 1)
- Which one of the following has maximum number55. 43. of unpaired electrons? (a) Mag

(a) Mg2+	(b) Ti3+
(c) V3+	(d) Fe2+

- 44. Excess of NaOH reacts with Zn to form (a) ZnH^{2} (b) Na2ZnO2 (d) Zn(OH) (c) ZnO
- 45. How many isomers does Co(en)2Cl2+ have? (a) 1 (b) 3
 - (c) 2 (d) 4
- 46. NH3 group in a coordination compound is named as (b) ammina (a) ammonium

(a) ammonium	(b) ammine
(c) amine	(d) ammonia

- 47. Name3)t4he complex Ni(PF (a) tetrakis (phosphorus (III) fluoride) nickel

 - (b) tetra (phosphorus (III) fluoride) nickel
 - (c) Nickel tetrakis phosphorus (III) fluoride
 - (d) (phosphorus (III) tetrakis fluoride) nickel (0)
- 48. The purple colour of KMnO4 is due to
 - charge transfer (b) d-d transition (a
 - f-f transition) (d) d-f transition
 - (c)

- How many lattice points belong to a face 49 centered cubic unit cell?
 - (a) 1 (b) 2
 - (d) 3 (c) 4
- 50. Schottky defect in solids is due to
 - a pair of cation and anion vacancies (a)
 - occupation of interstitial site by a pair of (b)
 - cation and anion (c)
 - occupation of interstitial site by a cation (d) occupation of interstitial site by an anion
- 51. Which one of the following is amorphous?
 - (a) Polystyrene (b) Table salt
 - (c) Silica (d) Diamond
- 52. The metal that crystallises in simple cubic system is (a) Po (c) Cu

(b)	Na
(d)	Ag

- 53. When ideal gas expands in vacuum, the work done by the gas is equal to (a) PV (b) RT
 - (c) 0 (d) nRT
- 54. For a closed system consisting of a reaction N2O4(g) 2NO2(g), the pressure
 - remains constant(b) decreases (a
 -) increases (d) becomes zero (6c m)oles of an ideal gas expand isothermally and reversibly from a volume of 1 litre to a volume of 10 litres at 27°C. What is the maximum work done?
 - (a) 47 kJ (b) 100 kJ
 - (c) 0 (d) 34.465 kJ
- 56. The reaction.
 - Zn(s) + CuSO4(aq)ZnSO4(aq) + Cu(s) is an example of a
 - (a) spontaneous process
 - (b) isobaric process
 - (c) non-spontaneous process
 - (d) reversible process
- 57. For the reaction, H2 (g) + I2 (g)2HI (g) ((bd))X0 c = = 0Kp (a) Kpp == K-Kcc
- (c) K 58. The increase of pressure on ice
- water at a constant temperature will c(ausewater to vaporize(b) water to freeze no change (d) ice to melt
- 59. T(ch)e order of the reaction

N205	N2O4(g) +	02(g	g) is
(a) (c) 3	2	(b)	2 0

- 60. The reactions with low activation energy are always
 - (a) adiabatic (b) slow

 - (c) non-spontaneous
 - (d) fast
- 61. For a cell reaction to be spontaneous, the standard free energy change of the reaction must be (a) (c) zero (b) positive
 - infinite (d) negative
- 62. Equivalent conductance of an electrolyte containing NaF at infinite dilution is 90.1 Ohm-1cm2. If NaF is replaced by KF what is the value of equivalent c(ao)nd9u0c.t1a Onhcme?-<u>11cm2(b)m-1cm2</u> (c) 0 (d) 222.4 Ohm-1cm2
- 63. The tendencies of the electrodes made up of Cu, Zn and Ag to release electrons when dipped in their respective salt solutions decrease in the order
 - (a) Zn > Ag > Cu(b) Cu > Zn > Ag
- (c) Zn > Cu > Ag (d) Ag > Cu > ZnThe electrode reaction that takes place at the 64. anode of CH4 - O2 fuel cell is (a) 202+8H++8-e 4H2O
 - CO2 + 8H+ + 8e-
 - CH4 2HO² 4 + 2O2 (b) CO2 + 2H2O

(c) CH (d) 2H+ + 2e-H2

What is the hybridization of oxygen atom in an 65. alcohol molecule?

(a) sp3	(b) sp
(c) sp2	(d) p2

- LiAlH4 ? 66. R-C-OH (a) RCH 2CH2OH (b) RCHO (d) RCH 20H (c) RCOR 67. Which one of the following is correct?
 - KMnO4 (a) RCHQH No reaction
 - 20H Na2Cr207,H2SO4 No reaction (b) CH CH
 - (c) CH3CHO Na2Cr207,H2SO4 No reaction

CH3 (d) СН 3-С-ОН снз



- 68. Which one of the following products obtained when diethyl ether is boiled with water in presence of dilute acid?
 - Glvcol (b) Ethy1 alcohol (a
 - Ethylene oxide (d) Peroxide
- 69 I(cd)entify the product for the following reaction

$$\begin{array}{c} 0 \\ CH 3 - C - CH_{3} + & CHOH & HCl & ? \\ \end{array}$$

$$\begin{array}{c} CH 3 & COOH \\ (a) CH 3 - CHOH & + & COOH \\ \end{array}$$

$$\begin{array}{c} CH 3 & COOH \\ + & COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ COOH \\ \end{array}$$

$$\begin{array}{c} CH 3 & COOH \\ + & COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ + & COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ + & COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ COOH \\ \end{array}$$

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$$\begin{array}{c} COOH \\ COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ + & COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ + & COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ + & COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ + & COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ + & COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ COOH \\ \end{array}$$

$$\begin{array}{c} COOH \\ COH \\ COH \\ \end{array}$$

$$\begin{array}{c} COOH \\ COH \\ COH \\ \end{array}$$

$$\begin{array}{c} COOH \\ COH \\ COH \\ COH \\ COH \\ COH \\ \end{array}$$

- 70. What is the reaction of acetaldehyde with concentrated sulphuric acid?
 - (a) No reaction
 - (b) Decomposition
 - (c) Charred to black residue
 - (d) Polymerisation
- Calcium Acetate on heating under distillation 71. gives
 - (a) Acetaldehyde and Calcium Oxide
 - (b) Calcium Carbonate and Acetic acid
 - (c) Acetone and Calcium Carbonate
 - (d) Calcium Oxide and CO₂
- 72. Identify the correct statement
- (a) Aldehydes on reduction give secondary (b) alcohols Ketones on reduction give primary alcohols kétones reduce Fehling's solution and give red cuprous oxide Ketones do not react with alcohols The O – H stretching vibration of alcohols 73. absorbs in the region 3700 - 3500 cm-1. The O -H stretching of carboxylic acids absorb in the r eg ion
 - (a) 3900 3700 cm-1(b)3000 2500 cm-1
 - (c) 3700 3500 cm-1(d)1700 2000 cm-1 Which among the following reduces Fehling's
- 74. solut ion?
 - (a) Acetic acid (b) Formic acid
 - (c) Benzoic acid (d) Salicylic acid

75. Determine the experimental condition for the following reaction



	$\frac{2}{x}$	1	2
А	1	х	2 xis&ingular, is
	1	1 *	2
(a)	± 1		(b) ± (d) 2
(c)	± 3		± 4

	x 3 7
82.	If $x = -9$ is a root of $\begin{vmatrix} 2 & x & 2 \end{vmatrix}$ 0, then other
	If $x = -9$ is a root of $\begin{vmatrix} 2 & x & 2 \\ 7 & 6 & x \end{vmatrix}$ 0, then other
83.	two roots are a (b) 2, y (d) 7 (cT)he 3va, lues of for which the2 s, ystem of equation x + y + 2 = 1, $x + 2y + 4z = 0$, $6x + 4y + 10z = 2$ is consistent are given by (a 1, -2 (b) -1, 2)) 1, 2 (d) 1, 1
	(c) 1 3 2
84.	Let A 2 5 t , then the values of t
	4 7t 6
Jiæ5.	for which inverse of A does not exist (a -2, (b) 3, 2) 12, (d) 3, -1 T(ch)e n-o3n integer roots of $x^4 3x^3 2x^2 3x 1 0$ (a) $\frac{1}{2}(3 \sqrt{\frac{13}{-}}, \frac{12(3}{-} \sqrt{13})$
	1 1/3
	(b) $\frac{1}{3}(3\sqrt{13}), \frac{1}{2}(3\sqrt{13})$
	(c) $\frac{1}{2}(3 \sqrt{\frac{17}{2}}), \frac{12(3}{2} \sqrt{17})$
	(d) $\frac{1}{2}(3 \sqrt{\frac{17}{2}}, \frac{1(3}{2} \sqrt{17}))$
86.	If ex $y = \sqrt{1 - y^2}$, then the value of y is
	(a) $\frac{1}{2(ex} \begin{pmatrix} e \\ x \end{pmatrix}$ (b) $\frac{12(ex ex)}{e}$
87.	x x (c) ex e 2 (d) ex e 2 Consider an infinite geometric series with the first term a and common ratio r. If its sum is 4 and
	the second term is $\frac{3}{4}$ then
	(a) $a = \frac{4}{7}, r = \frac{3}{7}$ (b) $a = 2, r = \frac{3}{8}$
	(c) $a = \frac{3}{2}, r = \frac{1}{2}$ (d) $a = 3, r = \frac{1}{4}$

x 3 7

ax2 + bx + c = 0, then the value of 3 + 3 is a³ 3abc b3 a³ (a) b 3 _a(3abc b3) 3abc b3 3 (c) (d) b c a3 а The volume of the tetrahedron with vertices 89. P (-1, 2, 0), Q (2, 1, -3), R (1, 0, 1) and S (3, -2, 3) is (b) 2 3 (a) 1 3 1 (d) 4 (c) 4 i²j^kand i^ 2j^ 3k^, b 90. If a 3i^j^then t such that a tb is at right angle С to c will be equal to (a) 5 (b) 4 (c) 6 (d) 2 91. An equation of the plane passing through the line of intersection of the planes x + y + z = 6 and 2x + 3y + 4z + 5 = 0 and passing through (1, 1, 1) is x(a +) y 2+x z + = 3 3y (b)z = 9 2(c0)x +x 2+3 2yy + + 2 36zz = 69 (d) 92. The length of the shortest distance between the lines r 3i^5j^7k^ (i²j^k)and i^j^k^ (7i^6j^k^)is r (a) 83 units (b) $\sqrt{6}$ units (C) $\sqrt{3}$ units (d) $2\sqrt{29}$ units 93. The region of the argand plane defined by |z i| |z i| 4is (a) interior of an ellipse (b) exterior of a circle (c) interior and boundary of an ellipse (d) interior of a parabola (in in1)where 94. The value of the sum n 1 i √1equals (a) i (b) i-1 (c) - i (d) 0

88. If and are the roots of the equation

95. If sin , cos , tan are in G.P. then cos9 + cos6 + 3cos5 - 1 is equal to (al) (b) 0 (c) (d) 2 96. If in a triangle ABC, $5\cos C + 6\cos B = 4$ and $6\cos A + 4\cos C = 5$, then $\tan \frac{A}{2} \tan \frac{B}{2}$ is equal to 2 3 (a) (b) 3 2 1 5 (c) (d) 5

97. In a model, it is shown that an arc of a bridge is semielliptical with major axis horizontal. If the length of the base is 9m and the highest part of the bridge is 3m from horizontal; the best approximation of the height of the arch, 2m from the centre of the base is

(a)	11 4 m	(b)	8 3m
(c)	7 m	(d)	2 m

The number of real tangents through (3,5) that can be drawn to the ellipses $3x^2 + 5y^2 = 32$ and $25x^2 + 9y^2 = 450$ is

meets the curve again at

(a)	0	(b)	2
(c)	3	(d)	4

99. If the normal to the rectangular hyperbola xy =

c2 at the point ct,ct

98.

ct', ct ', then (a) t3t' = 1 (b) t3t' = -1(c) tt' = 1 (d) tt' = -1

100.An equilateral triangle is inscribed in the parabola $y^2 = 4x$ one of whose vertex is at the vertex of the parabola, the length of each side of the triangle is

(a)	$\frac{\sqrt{3}}{2}$	(b)	$4\frac{\sqrt{3}}{2}$
(c)	$8\frac{\sqrt{3}}{2}$	(d)	8√3

101. If f(2) = 4 and f'(2) = 1, 2f(x)xf(2) x 106.The value of the integral log(tanx)dx then lim is equal to 2 0 х (a) 0 (c) 0 (b) 1 (d) $(b)^{1}_{2}$ (a) 0 2 4 (c) 1 107.What is the area of a loop of the curve r = asin3? (d) 2 102.What is the least value of k such that the function a2 a2 82 (a) (b) 8 $x^2 + kx + 1$ is strictly increasing on (1,2) (b) -1 (d) -2 1 (a) 1 (c) 2 a2 (d) (c) 12 24 хх 103.The maximum value of is 108.The value of the integral ¹etdt 1 (a) e (b) ee (a) e3 (c) 4(e3 - e) (b) 4e3 (d) 4e3 – 2e 1 1 1 e 109. The differential equation that represents all (c) ee (d) parabolas each of which has a latus rectum 4a е and whose axes are parallel to the x - axis is x3 y3104.If u = tan-1 x y, then x ux y uy d²2 2dydx 0 (a) d &l2y dy3 (a) sin 2u (b) cos 2u 0 (b) dx2 dx (c) sec2 2u (d) tan 2u d2_y a dx2 dy ³ $\frac{x}{\sqrt{1 - x}}$ and f(0) = 0, then f(x) = 0 105.If f'x (c) dy ³ dx d2y (a) $\frac{2}{3}$ $(1 x)^{\frac{3}{2}}$ $\frac{1}{6(1 x)^{\frac{2}{2}}}$ 1 2a 0 (d) dx2 xcosec yx 110.The solution of y dx + xdy = 0(b) $\frac{2}{3} (1 x)^{\frac{3}{2}} 3(1 x)^{\frac{1}{2}} 2$ is log¦x∣ cos ỷ V (a) С (c) $\begin{array}{c} 2 \\ 3 \end{array} \begin{pmatrix} 1 \\ 1 \\ x \end{pmatrix}^{\frac{3}{2}} 4(1 x)^{\frac{1}{2}} 2$ (b) logx | cos — С (c) $\log k \mid \sin \frac{x}{v}$ С (d) $\begin{array}{cccc} 2 & 3 & 1 \\ 3 & (1 & x)^2 & 3(1 & x)^2 & 1 \end{array}$ sin yx logx | с (d)

111.The particular integral of $\begin{cases} d2 \\ y \end{cases}$ 2y x ² is	117.In rolling two fair dice, what is the probability of obtaining a sum greater than 3 but not exceeding 6 ?
(a) $x^2 - 1$ (b) $dx^2 + 1$ (c) $\frac{1}{2}(x^2 + 1)$ (d) $\frac{1}{2}(x^2 + 1)$	(a) $\frac{1}{2}$ (b) $\frac{1}{3}$
112.The solution of (D2 + 16) $y = \cos 4x$ is	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
(a) Acos4x + Bsin 4x + $\frac{x}{8}$ sin 4x	118.Team A has probability $\frac{2}{3}$ of winning whenever
(b) Acos4x + Bsin 4x $\frac{x}{8}$ sin 4x	it plays. Suppose A plays four games. What is the probability that A wins more than half of its ga m es?
(c) Acos4x + Bsin 4x $\frac{x}{4}$ sin 4x	(a) $\begin{array}{c} 16 \\ 27 \end{array}$ (b) $\begin{array}{c} 1 \\ 9 \end{array}$
 (d) Acos4x + Bsin 4x 4 sin 4x 113.Determine which one of the following relations 	19 2 (c) 81 (d) 7
on X = {1,2,3,4} is not transitive. (a) R12== ,X t hxe X e, mthpet yu nreivlaetrisoa (b) R (c) R34 == {{((11,,31)),, ((21,,12))}, (2,3), (1,3) (d) R	3 119.An unprepared student takes five-questions of Inltroletions type quiz and guesses every answer. What is the probability that the stydent will pass (the)quiz if at least four correct answers is the passing grade?
114.Find the number of ways in which five large books, four medium-size books, and three small books can be placed on a shelf so that all books of the same size are together.	(a) $\begin{array}{c} 1 \\ 16 \end{array}$ (b) $\begin{array}{c} 3 \\ 16 \\ 1 \end{array}$
(a $5 \times 4 \times 3$ (b) $5! \times 4! \times 3!$) $3 \times 5! \times 4! \times 3!$ (d) $3! \times 5! \times 4! \times 3!$	$\begin{array}{ccc} 1 & & 3 \\ (c) & _{32} & (d) & _{32} \end{array}$
115.C(ocn)sider the set Q of rational numbers. Let be the operation on Q defined by $a b = a + b - ab$.	120.The probability density f(x) of a continuous random variable is given by f(x) =
The identity element under is (a) 0 (b) 1	Ke $ x $, x . Then the value of K is
(c) 2 (d) not exist 116.The statement ~ p q is equivalent to (a) p q (b)~ p q	(a) 1/2 (b) 2 1
(c) $\sim p \sim q$ (d) $p \sim q$	(c) ⁴ (d) 4

2006 SOLUTIONS

3.

4.

PART - I (PHYSICS)

1. (b) V= 300 V, 1C= 2.0F, C2= 8.0F,

Net capacitance, $\begin{array}{ccc} 1 & 1 & 1 \\ C_s & C_1 & C_2 \end{array}$ Cs C1C2 C1 C2

$$Cs = \begin{array}{ccc} 2 & 8 & 1 \\ 2 & 8 & 6 \end{array} = 1.6 F.$$

С

Now total charge, $Q = V \ll C = s 300 \$ $0.6 \times 10^{6} = 4.8 \times 10^{7} C^{4}$. In series charge is same on capacitors

Charge on 2 F capacitor is
$$4.8 \times 10 - 40$$

Let the point P where resultant field is zero be x m from 4C charge and (1-x) m distance apart from -2C charge. Since field is zero at this point then,

$$0 \frac{1}{4_{0}} \frac{4}{x_{2}} \frac{-2C}{1-x^{2}}$$

$$4 C 2 C 2 1$$

$$x 2 1-x 2 x 2 1-x$$

$$2 1 - x 2x^{2}$$

2

$$Z I = X Z_X^2$$

Taking root $\sqrt{2}1 - x = x$

1.414 1-x x 1.414 -1.414x x 1.414 1 1.414 x x 1.414 2.414 x 0.58m (b) The net electric potential is algebraic sum of potential due to individual point charges.
 1, q₁ q₂ q₃

(a) In a metal, conduction current is due to electrons given by

I nAev
drift velocity, v
$$I$$

nAe
5
v $5 10^{26} 4 106$
1.602 10 $^{-19}$
1
4 1.602 101

5. (b) In series combination of capacitors, charges on both capacitors will be same.

$$V_{s} \begin{array}{c} Q & Q \\ C1 & C2 \\ 1000 Q 1 & C12 \\ C1 \\ 1000 Q C 1 C2 \\ Q \\ C1 \\ C2 \\ Q \\ 1000 \\ C1 \\ C2 \\ Q \\ 1000 \\ 3 \\ 6 \\ 10^{-12} \end{array} \begin{array}{c} 98 \\ 10^{-9} \\ 10^{-9} \\ 2 \\ 10 - 9C \end{array}$$

Parallel combination of 3 and 6 gives 6. (c) effective resistance, $R_{p} = \begin{array}{ccc} 3 & 6 & 18 \\ 3 & 6 & 9 \end{array}$. This in series with 2 gives net ressistance as 4 7. (b) The value of temperature coefficient of resistance is given by R2-R1 65 - 50 13. (d) R1 t2 –1 t 50 70-20 (t1 and t2 are in °C) 15 0.006/C 50 50 8 (b) In Leclanche cell a strong solution of ammonium chloride acts as an electrolyte. 14. (a) Ign = t hmea gxa. lcvuarnreonmteter, I (d) . through galvanometer, S = shunt resistance, G 9 = galvanometer resistance then 1 S Ig(galvanometer) =I G S 501 I I_g G S Ig 51Ig 1 10. (a) Current in tangent galvanometer I Gtan Where G = galvanometer constant H= earth's horizontal field = constant tan 1 I, 1 tan I_2 tan 2 I2 30 tan ^{1.732}60 2.999Å tan6 I_2 0 1 I2 ^{‡an3} 0.577 11. (c) Lorentz force on a charged particle in presence of magnetic and electic field is 17 18 F Fe Fm F qE qv B 12. (a) In a circular coil of n turns, magnetic field is OnI 4 10-7 250 20 10 -3 В 2 40 10-3 2r

(n = no. of turns, I = current through coil, r = radius of coil) 250 20 10 ^{-7-3 3} R 2 40 250 3.14 10-7 785 10-7 0.785 10 ⁻⁴ tesla = 0.785 gauss RMS value of A.C is $\frac{10}{\sqrt{2}}$ 0.707I 0 \mathbf{I}_{V} IO = peak value it is 70.7% of peak value. 1 <u>L</u> _____R√ C Q-factor is given by Q If resistance R is decreased, Q increases 8 10-4 80 10-4 |e| = 05 5 =16 × 10- 4 =1.6×10-3 V = 1.6 mV Current through an LCR circuit is maximum when impedance is minimum. Now impedance is minimum at Ζ 1 and resonance frequency when L С Z= R = minium i.e., inductive reactance (L) is equal to capacitive reactance (1/C)Our eyes respond to visible range from 400 (a nm to 700 nm

Velocity of electromagnatic wave in space)

(a is c
$$\frac{1}{\sqrt{\frac{0}{1} 0}}$$
 c $\frac{1}{\sqrt{2} 8}$
) $\frac{1}{\sqrt{16}}$ $\frac{4}{-}$ 0.25

and inductance L is increased, Q increases.

16. (c)

.....

Е

-KZe2 Potential energy in the orbit P.E. r

24. (a) Bragg's condition is 2dsin = n for second order n = 2 , sin =1. For longest d = 2 =d

25. (b) Photon moves with speed of light ie, v = cand rest mass of a particle is

26. (c)

hence m0 (photon)= 0 photon has zero rest mass.

Momentum of photon = hde Broglie wavelength is given by

h
$$6.626 10^{-34}$$

mv $1000 10^{-3} 1$ $6.626 10^{-34}$ m

27. (b) Let the velocity of a particle be v where mass m is double the rest mass i.e., m = Qmthen

28. (d) By Einstein's equation E= mc2 where m = 2kg $E = 2 \times (3 \times 10.8)^2$

$$= 2 \times (3 \times 100)^2$$

= 2 × 3 × 3 × 1016 = 18 × 1016 J

- 29. (b) By definition, the difference between the sum of the masses of neutrons and protons forming a nucleus and mass of nucleus is called mass defect
- 30. (b)Mean life time = 1.44 T where T is half life period of an atom

$$= 1.44 T = \begin{array}{c} T & 3\\ 0.6931 & 0.6931 \end{array}$$

(d) (by conservation of charge) 31

(d) Baryons are proton, neutron, lamda, . 32

> –), Xi 0,– sigma (

33. (c) As donor and acceptor impurities are added to semiconductor to make an extrinsic semiconductor, intrinsic semiconductor is formed by internal generation of e- by breaking up of covalent bonds.

- 34. (d) In p-type semiconductor, valency = 3, thus there is one unYformed bond or hole created. This hole is in valence band and is able to cause hole current. The energy levels of acceptor are in forbidden gap just above valence band In an oscillator,
- 35. (d) L-C circuit is coupled with transistor amplifier in such a way that there is a positive feed back to the LC circuit i.e., proper energy supply to LC at proper timings. So that total energy of LC circuit remains same. The gates AND, OR, NAND do not give binary addition, however in
- 36. (c) EXOR gate

truth table is

Α	В	Y	_
0	0	0	-
0	1	1	
0 1	0	1	
1	1	0	

This shows it gives perfect binary addition

37. (d)In FM, carrier frequency is the constant frequency which is modulated by signal amplitude. It is also called carrier swing. (Centre frequency is fc in AM wave,

frequency deviation fmax - fc ,

modulationfactor max) fc

38. (c) The common antenna is a straight

conductor of length l held vertically

with its lower end touching the ground.

39. (b) The vidicon is a storage-type camera tube in which a charge-density pattern is formed43. by the imaged scene radiation on a photoconductive surface which is then scanned by a beam of low-velocity electrons. The fluctuating voltage coupled out to a video amplifier can be used to reproduce the scene being imaged. The electrical charge produced by an image will remain in the face plate until it is scanned or until the charge dissipates.

40. (b)Maximum range of radar d $\max \sqrt{l}$ and power transmitted by antenna of length lis

p l/ ² l \sqrt{p} and d p1/4

PART - II (CHEMISTRY)

41. (b) The oxidation of ferrous ion by KMnO takes place in acidic medium as per following reaction

2KMnO4 + 8H2SO4 + 10FeSO4

K2SO4 + 2MnSO4 + 8H2O + 5Fe2(SO4)3 Eq. mass of KMnO4

Molecular mass changein oxidation number

 $= \frac{\text{Molecular mass}}{5} \frac{158}{5} = 31.6$

42. (b) In case of lanthanoids, 4f orbitals lie too deep and hence the magnetic effect of the motion of the electron in its orbital is not quenched out. Here spin contribution S and orbital contribution L couple together to give a new quantum number J. Thus magnetic moment of lanthanoids is

given by, $g_{3}/J(J 1)$

where J = L - S when the shell is less than half fill

J = L + S when the shell is more than half fill

and g $\begin{array}{c} 11 \quad S(S \ 1) \quad L(L \ 1) \\ 2 \quad 2J(J \ 1) \end{array}$

(d)Mg2+ = 1s2, 2s2, 2p6 (No unpaired electrons)

Ti3+ = 1s2, 2s2, 2p6, 3s2, 3p6, 4s0, 3d1

(One unpaired electrons)

```
V3+ = 1s2, 2s2, 2p6, 3s2, 3p6, 4s0, 3d2
```

(Two unpaired electrons)

Fe2+ = 1s2, 2s2, 2p6, 3s2, 3p6, 4s0, 3d6

(Four unpaired electrons)

Fe2+ has highest number of unpaired el ect r on s.

44. (d) Zn + 2NaOH Na2ZnO2 + H2 Sod. zincate





- 46. (b) Neutral ligands are given the same names 58. (d)Ice as the neutral molecule. However, two very important exceptions to this rule are: H2O Aquo (Aqua) NH3 Ammine.
- (a) Ni(PF 3)4 tetrakis phosphours (III) fluoride 47 nickel (0). The colour of KMnO transfer. 59.
 - The configuration o4f ism dauneg taon (a) ecshea rgien permagnate ion is d0 but it is coloured because its electrons are photo-60.
- 48 exited. In face centred cubic lattice, the atoms are present at eight corners of faces
- 4.9. (c) and one each at 6 faces.

Lattice points belonging to face centred

 $\frac{1}{cubic}$ unit cell = 8 6 4

- 50. (a) Schottky defect is caused when equal number of cations and anions are missing from their lattice sites.
- 51 Polystyrene is thermoplastic substance. (a)
- Po Simple cubic lattice (a) Na – bcc 52
 - Cu fcc

RP1T2 P2T1 Wirr Pext 53. (c) P1P2

> During expansion in vaccum $P_{ext} = 0$ work done = 0.

54. (b) As the system is closed, hence the reaction will be reversible, hence according to Le-chatelier principle pressure decreases since the volume is increasing. (d)W = - 2.303 nRT loVg2 55. V1

> Given n = 6, T = 27°C = 273 + 27 = 300 K V1 = 1 L, V2 = 10 L

$$W = -2.303 \times 6 \times 8.314 \times 300 \log_{10}^{10}$$

= 34.465 kJ

- 56. (a) It is spontaneous process because zinc is more reactive than copper, hence can easily repace Cu from CuSO4.
- $K_n = K pc ((gR)T -) nr(g) = 2 2 = 0$ 57. (c) n = n Kp = Kc
 - Water The volume of ice is more than water. Therefore when pressure is increased the equilibrium shifts in forward direction. It favoures melting of ice.
 - (c) It is a first order reaction because rate of reaction [N2O5]
 - The reactions with low activation energies (d) are always fast whereas the reactions with
- high activation energy are always slow. 61. (d)

For spontaneous reaction free energy change is pegative.

- 62. (a) Because at infinite dilution the equivalent conductance of strong electrolytes furnishing same number of ions is same.
- Reducing character i.e tendency to loose 63. (c) electron decreases down the series, hence
- the correct order is Zn > Cu > Ag. (b) 64.
- £Ht +a n2oHdOe the CfOol l+o w8Hin g+ +r e8aec -tion takes Oppaycgeen atom in²alcohol molecule is sp3 65. (a)
- hybridised. 66.
 - (d) In this reaction LiAlH 4 acts as reducing

O LiAlH4 agent. RCOH RCH2OH



80. (d) On acetylation aniline is converted into acetamide which is resonance stablised and therefore less reactive.



PART - III (MATHEMATICS)

81. (a)We know that, A is singular if |A| = 0

2 1 2 $\overline{\mathbf{x}}$ |A| |1 x 2 |x Q2 $\begin{vmatrix} 1 & \frac{1}{x} \end{vmatrix}$ 2 $|A| = \frac{2}{x} \frac{2}{2x} \frac{2}{2x} \frac{12}{2x^2} \frac{2x^2}{2x^2} \frac{1}{2x^2} x = 0$ 2 x[0] 2 2x2 2 2x 2 2x 2 2x 2 2x 0 2x2x 2x3 2 2x2 0 x3x2x10 x2(x 1) 1(x 1) (x 1) (x 2 1) 0 0 Х 1 x 3 7 82. (b) Given 2 x 2 0 76 x x[x2 12] 3[2x 14] 7[12 7x] 0 ^{x3} 67x 126 0 But given (x = 9) is a root of given determinant. (x + 9) is a factor x3 9x² 9x² 81x 14x 126 0 x2(x 9) 9x(x 9) 14(x 9) 0

 $(9)(x^2 9x 14) 0$ 9)(x² 7x 2x 14) 0 Х $(x \ 9)(x \ 7)(x \ 2) \ 0$ X X 9,7,2 83. (c)We have 1 1 1 A:B 1 1 2 2 4 1410 111: 1 ~ 103 : 1 039: 2 1 applying R2 R2 R₁ & R3 R3 R1 1 1 1 : 1 ~ 0 1 3 : 1 2 0 00: 3 2 applying R ₃ R₃ 3R2 But the system is consistent ² 3 2 0 1) 0 2or 1 (2)(84. (c)We know that inverse of A does not exist only when |A| = 01 3 2 2 5 t 0 4 6 7t $(30 7t t^2) 3(12 4t)$ 2(14 2t 20) 0 30 7t ^{t2} 36 12t ^{12 4t} 0 t² t 6 ⁰ t² 3t 2t 6 0 t(t 3) 2(t 3) 0

(t 3)(t 2) 0 t 2, 3

85. (a) Given
$$x4 - 3x3 - 2x2 + 3x + 1 = 0$$

By using Hit & trial method, we have
 $(x - 1)$ is a factor of given equation
 $(x - 1)(x3 - 2x2 - 4x - 1) = 0$
 $(x - 1)(x^{-3} - x^{-2} - 3x - 2x - 1) = 0$
 $(x - 1)(x - 1)(x^{-2} - 3x - 1) = 0$
 $(x - 1)(x - 1)(x^{-2} - 3x - 1) = 0$
 $x - 1 - 1 \text{ or } x^{-3} - 3x - 1 = 0$
Now $x^{-3} - 3x - 1 = 0$
 $x - \frac{3 - \sqrt{9-4}}{2}$
 $x - \frac{b - \sqrt{b - 4ac}}{2a}$
88.
 $x - \frac{3 - \sqrt{1-3}}{2}$
non-integer roots of given equation are
 $\frac{1}{2}(3 - \sqrt{1-3}), \frac{12}{2}(3 - \sqrt{1-3})$
86. (b) Given ex $y - \sqrt{1-y^2}$
 $ex y - \sqrt{1-y^2}$
Squaring both side, we have
 $e^{2x + y^2 - 2exy = 1 + y^2}$
 $2ex y = e^{2x - 1}$
 $y - \frac{1}{2ex} y - \frac{1}{2} e^x e^x$
87. (d) First term = a & common ratio = r
Given S $4 & a_{-2} - \frac{3}{4}$
 $\frac{a}{1-r} - 4$...(1)
 $& ar - \frac{3}{4} - S - \frac{a}{1-r} & an - ar^{n-1}$

3 4r a

.

_

.

Equation (1) becomes
$$\frac{3}{4r(1 r)}$$
 4
 $16r^{2} 16r 3 0$
 $(4r 3) (4r 1) 0$
 $r \frac{3}{4} \text{ or } r \frac{1}{4}$
when $r \frac{1}{4}$ then $a \frac{3}{4 \frac{1}{4}}$ 3
 $a 3 \& r \frac{1}{4}$
(c) Given : & are roots of equation
 $ax^{2} + bx + c = 0$
 $b \& c \\ a$
Now, $3 3 ()^{3} 3 ()$
 $3 3 b \frac{3}{3} 3ca. b$
 $a^{3} a b \frac{3}{3} 3ca. b$
 $a^{3} a b \frac{3}{3} 3ca. b$
 $a^{3} a b \frac{3}{3} 3bc$
 $a^{3} a \frac{3}{4} a^{3} a^{3}$
(b) Given : The vertices of tetrahedron are P(-1, 2, 0), Q(2, 1, -3), R(1, 0, 1) \& S(3, -2, 3)
Volume of tetrahedron $\frac{1}{7}$ PQPRPS
Now,
PQ (2 1)i^{(1} 2)j^{(3)}k^{3} 3i^{2} 3k^{3}
Similarly, PR 2i^{2}j^{k}
 $\&PS 4i^{4}4j^{3}3k^{7}$
Volume of tetrahedron
 $\frac{1}{6}\begin{vmatrix} 3 & 1 & 3 \\ 4 & 2 & 1 \\ 4 & 3 \end{vmatrix} \frac{2}{3}$

90. (a)We have, a tb $(i^{2}j^{3}k^{1})t(\hat{1}2j^{k})$ (1 t)i^ (2 2t)j^ (3 t)k^ It is to c 3i^j^ If 3(1 t) (2 2t) (3 t)(0) 0 3 t 5 3t 2 2t 0 91. (d) The equation of the plane through the line of intersection of the given planes is (x2 x + +y 3 + y z + - 4 6z) + 5) = 0 ... (1)If equation (1) passes through (1, 1, 1), we have 3 3 14 0 14 $\frac{3}{14}$ in (1), we obtain the Putting 93. (c) equation of the required plane as (x y z 6) ³/₁₄(2x 3y 4z 5) 0 20x 23y 26z 69 0 92. (d) Shortest distance^{PQ} $\frac{\begin{array}{c|c} b_1 & b_2 & a_2 & a_1 \\ \hline & b_1 & b_2 \\ \hline & b_1 & b_2 \\ \hline \end{array}}$ 94. (b) Now, a₂ a₁ îjî kî 3iî 5jî 7kî a₂ a₁ 4iî 6jî8kî $\overrightarrow{P} = -\overrightarrow{i} - \overrightarrow{j} - \overrightarrow{k} + \mu(7\overrightarrow{i} - \overrightarrow{6}\overrightarrow{j} + \overrightarrow{k})^{\circ} \qquad B(a_2)$ 95. A (a) $L_1 = (3\hat{i} + 5\hat{j} + 7\hat{k}) +$ $(\hat{i} - 2\hat{i} + \hat{k})$ And $b_1 \ b_2 \ \begin{vmatrix} \hat{i} & \hat{j} & k \\ 1 & 2 & \hat{i} \\ 7 & 6 & 1 \end{vmatrix}$

$$\begin{array}{c|ccccc} b_1 & b_2 & \hat{i}(2\ 6) & \hat{j}(1\ 7) & k^{\,(}\ 6\ 14) \\ b_1 & b_2 & 4i^{\,6}\ 6j^{\,7}\ 8k^{\,7} \\ \text{Shortest distance} \\ PQ & \left| \frac{(4i^{\,6}\ 6j^{\,7}\ 8k^{\,7}).(\ 4i^{\,6}\ 6j^{\,7}\ 8k^{\,7})}{\sqrt{16} & 36 & 64} \right| \\ PQ & \left| \frac{16 & 36 & 64}{\sqrt{116}} \right| \\ PQ & \left| \frac{11}{\sqrt{6}} \right| & \sqrt{116} & 2\sqrt{29} \\ & p_Q^{\,11} & 2\sqrt{29} & \text{units} \\ \text{Given, } |z & i| & |z & i| & 4 \end{array}$$

 $\begin{array}{c|c} |z & (0 i)| & |z & (0 i)| & 0 \\ \hline \text{This equation represent the interior and} \\ \text{boundary of ellipse with foci at } (0, 1) \& \\ (0, -1), \text{ whose major axis is along the y-axis.} \\ \begin{array}{c} 13 & 13 \\ i^n & \text{in } 1 & 1 \end{array} \begin{array}{c} 13 & 13 \\ \text{in } & 1 & 1 \end{array}$

(b)
$$i^{1}$$
 i^{1} i^{1} i^{1} i^{1} i^{1} i^{1}
 i^{1} i^{1} i^{2} i^{13}
 i^{1} i^{1} i^{1} i^{1}
 $i^{(1(1i)}$ $\begin{pmatrix} i \\ i \end{pmatrix}$
 i^{0} $\begin{pmatrix} i \\ i \end{pmatrix}$ i^{0} i^{0}
(b) Given : sin 1, cos , tan are in G.P.
 \cos^{2} sin tan cos 3 sin 2

_{cos}³ 1 cos2

Cubic both sides, we have

COS

 \cos $\cos 6$ $3\cos^5$ $(\cos^3$ $\cos^2)$ 1

cos⁶ 3cos⁵ ¹

[Using equation (1)]

cos cos6 3cos5 1 0

96. (c) Given : 5cosC + 6cosB = 4 $6\cos A + 4\cos C = 5$ (1) Adding eq. (1) & (2), we have ... $9\cos C + 6(\cos A + \cos B) = 9$ (2)9cosC 6 2cos A B.cosA В 9 2 A 2 ℓ.cos В 9cosC 9 12cos 0 2 2 12sin C.cosA В 9(cosC 1) 0 2 2 А_В 9 1 2sin2C2 12sin C.cos 1 0 2 2 B 18sin2 Ç 12sin C2 .cos A 0 2 3sinC 2cosA B 2 2 В 2cosA B 3cos 2 2 A 3 cos A.cos B .sinB2 sin 2 2 2 2 cos A.cos B sin A.sin B 2 2 2 2 5sin A.sinB2 cos A.cosB2 2 2 5tan A.tanB2 1 2 tan A.tan B $\frac{1}{5}$ 2 97. (b) Equation of the semielliptical bridge x2 y2 1 (1) a2 b2 Here, 2a = 9 b = 3 а 2, x2 y2 1 9 81

4

```
4x2 y2
81 9 1 ..... (2)
```



Here, OQ = 2 m, let $PQ = y_1$ P(2, y1) Since point P lies on the ellipse (2)

Hence, best approximation of the height of

the arch
$$\frac{8}{3}$$
 m.

98. (c) Given : Equations of ellipses

 $3x^2 + 5y^2 = 32$...(1) & $25x^2 + 9y^2 = 450$...(2)

Tangents to the ellipse (1) & (2) are passing through the point (3, 5)

3(3)2 + 5(5)2 - 32 = 27 + 75 - 32 > 0

So the given point lies outsides the ellipse. Hence, two real tangents can be drawn from the point to the ellipse,

& 25(3)2 + 9(5)2 - 450 = 225 + 225 - 450 = 0

The point lie on the ellipse. Hence one real tangent can be drawn. No. of real tangents = 3 99. (b) The equation of tangent at ^{ct, ct} is ty = t3x - ct4 + cIf it passes through ct',ct' then tc t3ct'ct4 c ť t t3t'2 t4t't' t _ tt3't'(t'.t) t3t' 1 Note : If we take the co-ordinate axes along the asymptotes of a rectangular hyperbola, then the general equation $x^2 - y^2 = a^2$ becomes xy = c2, where c is a constant. 3 Let AB = , then AM $\cos 30^{\circ} - \frac{\sqrt{2}}{2}$ 100. (d) & BM sin30° 2 <u>_</u>30° М A X ⇒X 130° Y So, the coordinates of B are $\frac{\sqrt{3}}{2}$, $\frac{1}{2}$ Since, B lies on $y_2 = 4x$ 2 $4 - \frac{\sqrt{3}}{2}$ $\frac{16}{2} \cdot \sqrt{3}$ 8√3 101. (d) Let f(x) = ax + bGiven f(2) = 4 & f'(2) = 1 $f(2) = a \cdot 2 + b = 4$ 2a + b = 4 ...(1)

f'(x) = a f'(2) = a = 1 a = 1 $2 \times 1 + b = 4$ b = 2 [using equation (1)] f(x) = x + 2limxf(2) 2f(x) Now, x 2 x 2 2) lim2x 4 lim 4x 2(x x 2 x 2 x 2 2x lim2(x 2)2 x 2 (x 2) 102. (d) Let $f(x) = x^2 + kx + 1$ f'(x) = 2x + kf(x) is strictly increasing on (1, 2) if f'(x) > 0 for x (1, 2)2x + k > 0 for x (1, 2) k > -2x for x (1, 2)Now, 1 < x < 2 2 < 2x < 4-2 > -2x > -4-4 < -2x < -2k 2 Hence least value of k = -2. 1x[×] v xx Let y 103. (c) Then $\log y = -x \log x$ 1dy (1 logx) ydx dy or dx y(1 logx) d y.1x (1 logx).dydx у & dx2 (1 logx).dydx 1 ^{× 1} d y Х d x 2 Now, dy 0 1 logx 0 loge ^{log 1e} logx 1 1 Х е

Let 1 + x = t2 x = t2 - 1 Also, $\begin{array}{ccc} d^2 & 1 & 1 \\ y & at x & e \end{array}$ is $e^{1} e^{1} 0$ dx = 2t.dt $f(x) = t^2 \frac{1}{t} 2t dt 2(t^2 - 1)dt$ dx dy dx 0 2 f(x) 2 3 t c So, x 1 is a point of local maxima. Maximum value $f(x) = \frac{2(1x)^{3/2}}{3} (1 x)^{1/2} c$ 1 = value of ywhen $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$ ee(1) Euler's theorem x $\begin{array}{ccc} z \\ x \end{array}$ y $\begin{array}{ccc} z \\ y \end{array}$ nz But $f(0) 0 2^{13} 1 c 0$ 104. (a) x3 y3Given : U = tan⁻¹ x y $\frac{4}{3}$ c 0 c $\frac{4}{3}$ Equation (1) becomes tanU x3 y3 x y z(let) $f(x) = \begin{array}{ccc} 2 (1 x) 3/2 & (1 x)^{1/2} & 4 \\ 3 & 3 \end{array}$ n = 3 – 1 = 2 $x \begin{array}{c} z \\ x \end{array} y \begin{array}{c} y \\ y \end{array} z 2z$ $f(x) = \frac{2}{3}(1x) = \frac{3}{2} - 3(1x) = \frac{1}{2}$ x tanU y .tanU 2 tan U x ... y 106. (a) Let I ² log(tanx)dx ...(1) x.sec2U. U y.sec2 U. U y 2 tan U sec2U.x X y Uy 2tanU Then, I $\begin{array}{c} 2 \\ \log \tan x \\ 0 \end{array}$ dx $\begin{array}{ccc}
a & a \\
f(x)dx & f(a & x)dx \\
0 & 0
\end{array}$ U y sin2U x y I ²log(cotx)dx 105. (b) Given : f'(x) $\frac{x}{\sqrt{1-x}}$, f (0) 0 $f'(x)dx = \frac{x}{\sqrt{1-x}}dx$ I $\log_{0}^{2} \tan x dx$ $f(x) = \frac{x}{\sqrt{1-x}} dx$



Putting value of (y - k) from (2) in (3), we get

$$\begin{array}{ccc} d^2y & dy & ^3 \\ 2a & dx^2 & dx & 0, which is required \\ equation. \end{array}$$

110. (b) Given: $x \cos ec x^{y}$ y dx xdy 0

$$x y dx x dy 0$$

$$x y dx x dx 0$$

$$x y dx x dx x dy 0$$

$$x y dx x dx x dy 0$$

$$y dx x dy 0$$

$$y dx x dy 0$$

$$dy x dx x dy 0$$

$$(1)$$

$$x$$

$$Fut x ddx x dy dx x dy 0$$

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Particular integral (P.I.)
$$\begin{bmatrix} 1 \\ D^2 \\ 2 \end{bmatrix}^{X^2}_{2}$$

$$\begin{bmatrix} 1 \\ D^2 \\ 21 \\ 2 \end{bmatrix}^{X^2}_{2}$$

$$(1 D)^{-1} 1 D D^2 D^3 \dots D^2_{2}$$

$$(1 D)^{-1} 1 D D^2 D^3 \dots D^2_{2}$$

$$P.I. \frac{1}{2} 2 D^2_{2} D^2_{2} \dots (X^2)_{2}$$

$$P.I. \frac{1}{2} X^2 D^2_{2} (X^2)_{2}$$

$$P.I. X^2 1$$
(a) If $(D^2 + 16)y = \cos 4x$
Here the auxiliary equation is $m^2 + 16 = 0$
 $m = \pm 4$
Complementary function
 $= (A \cos 4x + B \sin 4x)$
& Particular Integral (P.I.)
 $D^2^{-1} a^2 \cos ax 2 a \sin ax$
 $P.I. \frac{x}{2} 4 \sin 4x$
Solution $y = Complementary function$
 $+ Particular Integral
 $y = A \cos 4x + B \sin 4x + \frac{x}{8} \sin 4x$
(c)
(d) Let us make one packet for each of the
books on the same size. Now, 3
packets can be arranged in P(3, 3) = 3!
ways 5 large books can be arranged in 5! ways 4 medium size books can be
arranged in 4! ways 3 small books can$

112.

11 3.

11

4.

be arranged in 3! ways Required number of ways

 $= 3! \times 5! \times 4! \times 3!$ ways

115. (a)	An identity relation is one in which every element of a set is related to itself only. a * b = a + b - ab As in identity relation 'a' is related to 'a', so the correct option will be the one which gives the value of the relation = 'a'. So, equating $a + b - ab = a$, we get $b(1 - a) = 0$. Now putting the values of a, we find b and the option in which $a = b$, will be the answer. For $a = 0$, $b = 0$, so the correct option. For $a = 1$, $b(1 - 1) = 0$ b can have multiple values. For $a = 2$, $b(1 - 2) = 0$	${}^{4}C_{3} \begin{array}{c} 2 \\ 3 \end{array}^{3} \cdot \begin{array}{c} 13^{4} \\ {}^{3} \\ {}^{4}C_{4} \end{array} \begin{array}{c} 2 \\ 3 \\ {}^{4}C_{4} \end{array}^{4} \begin{array}{c} 2 \\ 3 \\ {}^{4}C_{4} \end{array} \begin{array}{c} 2 \\ 3 \\ {}^{4}C_{4} \end{array} \begin{array}{c} 2 \\ {}^{4}C_{4} \end{array} \begin{array}{c} 3 \\ {}^{4}C_{4} \end{array} \begin{array}{c} 2 \\ {}^{4}C_{4} \end{array} \begin{array}{c} 3 \\ {}^{4}C_{4} \end{array} \begin{array}{c} 2 \\ {}^{4}C_{4} \end{array} \begin{array}{c} 3 \\ {}^{4}C_{4} \end{array} \begin{array}{c} 2 \\ C \end{array} \begin{array}{c} 2 \\ {}^{4}C_{4} \end{array} \begin{array}{c} 2 \\ C \end{array} \end{array} \begin{array}{c} 2 \\ C \end{array} \end{array} \begin{array}{c} 2 \\ C \end{array} \begin{array}{c} 2 \\ C \end{array} \end{array} \end{array} \begin{array}{c} 2 \\ C \end{array} \end{array} \begin{array}{c} 2 \\ C \end{array} \end{array} \end{array} \begin{array}{c} 2 $
116. (a)	b=0buta=2. p q ~p ~pvq p q T T F T T T F F F F F T T T T F F T T T	= 5C ₄ +5 _{C5} 5! 5! 4!1! 5!0! 5 1 6 m 6 Since to pass the quiz, student must give 4
117. (b)	Let S be the sample space	or 5 true answers.
(,	n(S) 36 Events [sum greater than 3 but not exceeding 6] 120.(a) = {(2, 2), (3, 1), (1, 3), (4, 1), (1, 4), (5, 1) (1, 5), (3, 2), (2, 3), (4, 2), (2, 4), (3, 3)}	Hace, p m 6 3 n 32 p 16 Since f(x) is the probability density function of random variable X.
	n(E) 12	f(x) 1
	Required probability = $\frac{n(E)}{n(S)}$ 12 1	Now we have
118. (a)	Let 'p' denote the probability of winning of team A whenever it plays ^{1 3} p ² & q 1 ² p ³ & q 1 ²	Ke $ x $ dx 1 2 K.e $ x $ dx 1 0 2 K.e x dx 1
	Let X denotes the number of winning games out of 4 games i.e. n = 4 The probability of r success P(X = r) = nr cpr nq - r, r = 0, 1, 2, 3, 4 Probability of winning more than half games = P(X > 2) = P (X = 3) + P(X = 4)	2 K.e UX 1 0 2K.e ^X 1 2K 1 K 1 2