VITEEE 2008 Question Paper

Vellore Institute of Technology Engineering Entrance Examination

SOLVED PAPER

2008

PART - I (PHYSICS)

Two beams of light will not give rise to an

- 1. interference patern, if
 - (a) they are coherent
 - (b) they have the same wavelength
 - they are linearly polarized perpendicular to (c) each other
 - (d) they are not monochromatic
- A slit of width 'a' is illuminated with a fmronmo cahromatic light of wavelength distant source and the diffraction pattern is 2.

8 observed on a screen placed at a distance 'D' from the slit. To increase the width of the central1 maximum one should

d(ae)crease D d(be)crease a d(ce)crease

t(dh)e width cannot be changed

A thin film of soap solution (n = 1.4) lies on the 3. top of a glass plate (n = 1,5). When visible light is incident almost normal to the plate, two adjacent reflection maxima are observed at two wavelengths 420 and 630 nm. The minimum thickness of the soap solution is

(a	420	(b	450 nm
)	nm)	1260 nm
(_)		()	

If the6 s3p0eed of a wave doubles as it passes 4 from shallonwm water into deeper water, its wavelength will be

> (cu) nAc hliagnhgt ewdhose (a)

- fr(ebq)uehnaclyv eisd equal to 6 ×
- 5. 1014d oHuzb lies di ncident gmueatdarlu pwlheodse work o(nd) a function is

1.6 1019J 6.631034Js 1eV 2eVh

The maximum energy of the electrons emitted will be

4.49
٧
5.49
eV

6. An electron microscope is used to probe the atomic arrangements to a resolution of 5Å. What

should be the electric potential to which the

o be a deele atted ?	
 t	to be a deeleFated ?

(c) 2.5 kV (d) 5 kV

Which phenomenon best supports the theory that matter has a wave nature ?

- Electron momentum (a)
- (b
- Electron diffraction Photon diffraction **{**8}

9.

The radioactivity of a certain material drops to

of the initial value in 2 hours. The half life of 16 this radionuclide is (a) 10 min (b) 20 min

(c) 30 min (d) 40 min

An observer 'A' sees an asteroid with a

radioactive element moving by at a speed = 0.3 c

and mAe. aAsnuorethse trh oeb rsaedrio.tetadn t'libeinteges dmeocvaiyn BTh т

asteroid and measures its decay time as T TA and TB are related as below

- (a) T BT < TA Either (A) or (C) depending on
- (b &Ah e=>t hTTeBAr the asteroid is approaching or
- (B) moving away from A
- 10. 2U3 4has 92 protons and 234 nucleons total in its nucleus. It decays by emitting an alpha particle. After the decay it becomes

(a) 232U	(b) 232Pa
()	

- (c) 230Th (d) 230Ra
- K and K x-rays are emitted when there is a 11. transition of electron between the levels
 - (a) n = 2 to n = 1 and n = 3 to n = 1 respectively
 - (b) n = 2 to n = 1 and n = 3 to n = 2 respectively
 - (c) n = 3 to n = 2 and n = 4 to n = 2 respectively
 - (d) n = 3 to n = 2 and n = 4 to n = 3 respectively

12. A certain radioactive material XA starts emitting 18. and particles successively such that the end

product is Z3YA8 . The number of and particles emitted are. (a) 4 and 3 respectively (b 2 and 1 respectively) 3 and 4 respectively (c) 3 and 8 respectively 13.) 10k



In the circuit shown above, an input of 1V is fed into the inverting input of an ideal Op-amp A. The output signal Vout will be

- (a) +10 V (b) -10 V
- (c) 0 V (d) infinity
- 14. When a solid with a band gap has a donor level just below its empty energy band, the solid is
 - (a) an insulator
 - (b a conductor
 -) a p-type semiconductor
 - (c) an n-type semiconductor
- 15. Adp-n junction has acceptor impurity concentration of 1017 cm-3 in the p-side and donor impurity concentration of 1016 cm-3 in the n-side. What is the contact potential at the junction (kT = thermal econnecregnyt,i=aintitoar44% rtBieOr cm)?
 - (a) (kT/e) ln (4×1012)
 - (b (kT/e) ln (2.5×1023)
 - (kT/e) ln (1023)
 - (c) (kT/e) ln (109)
- 16. AdZener diode has a contact potential of 1V in the absence of biasing. It undergoes Zener breakdown for an electric field of 106 V/m at the

depletion region of p-n junction. If the width of the depletion region is 2.5 m, what should be the reverse biased potential for the Zener breakdown to occur? (a)3255(c) V (d) V

- 17. In Co1l.p5itt oscillator the fee0d.5back network consVists of V
 - (a) two inductors and a capacitor
 - (b) two capacitors and an inductor
 - (c) three pairs of RC circuit three
 - (d) pairs of RL circuit

- The reverse saturation of p-n diode
- (a) depends on doping concentrations
- (b depends on diffusion lengths of carriers
-) depends on the doping concentrations and
- (c) diffusion lengths
- (d) depends on the doping concentrations, diffusion length and device temperature
- A radio station has two channels. One is AM at 1020 kHz and the other FM at 89.5 MHz. For good results you will use
 - (a) longer antenna for the AM channel and shorter for the FM
 - (b)shorter antenna for the AM channel and longer for the FM
 - (c) same length antenna will work for both
 - (d) information given is not enough to say which one to use for which
- 20. The communication using optical fibers is based on the principle of
 - (a) total internal reflection
 - (b) Brewster angle
 - (c) polarization
 - (d) resonance
- 21. In nature, the electric charge of any system is
 - always equal to
 - (a) half integral multiple of the least amount of ch ar ge
 - (b) zero
 - (c) square of the least amount of charge
 - (d) integral multiple of the least amount of ch ar ge
- 22. The energy stored in the capacitor as shown in Fig. (a) is 4.5×10-6 J. If the battery is replaced by another capacitor of 900 pF as shown in Fig. (b), then the total energy of system is



23. Equal amounts of a metal are converted into 28. cylindrical wires of different lengths (L) and cross-sectional area (A). The wire with the maximum resistance is the one, which has (a) length = L and area = A

(c) length = 2L and area =
$$\frac{A}{2}$$

- (d all have the same resistance, as the amount of the metal is the same
- 24. If the force exerted by an electric dipole on a charge q at a distance of 1m is F, the force at a point 2m away in the same direction will be

(\cdot)	F	(1.)	F	
(a)	2	(b)	4	
	F		F	
(c)	6	(d)	8	

0 density r of radius B with negative surface charge density , such that the total charge in the system is 0 is a positive constant and r is the zdeisrota. nce from the centre of the sphere. The ratio

- R is
- 2 R

$$\frac{-}{0}$$
 (b) $\sqrt{2} / 0$

0/2 (d) (c)

26. A solid spherical conductor of radius R has a spherical cavity of radius a (a < R) at its centre. A charge + Q is kept at the centre. The charge at the inner surface, outer surface and at a position r (a < r < R) are respectively

(a)
$$+Q, -Q, 0$$
 (b) $-Q, +Q, 0$
(c) $0, -Q, 0$ (d) $+Q, 0, 0$

- 27. A cylindrical capacitor has charge Q and length L. If both the charge and length of the capacitor are doubled, by keeping other parameters fixed, the energy stored in the capacitor
 - (a) remains same
 - (b) increases two times
 - (c) decreases two times
 - (d) increases four times

T eharcehe areres isctoannnceecst eodf 4as shown in figure. If the point D divides the resistance into two equal halves, the resistance between point A and D will be



The resistance of a metal increases with 29.

- 25. A solid sphere of is a deinucsi oRse1d abnyd a v hoolullmowe scphhaergree
 (a) the collisions of the conducting electrons (b)
 - with the electrons increase the collisions of the conducting electrons with the lattice consisting of the ions of the metal increase
 - (dc)) the cnears ber of conduction electrons

the number of conduction electrons in cr eas es

- 30. In the absence of applied potential, the electric current flowing through a metallic wire is zero because
 - (a) the electrons remain stationary
 - the electrons are drifted in random direction (b) with a speed of the order of 10-2 cm/s
 - the electrons move in random direction with
 - (c) a speed of the order close to that of velocity of light
 - electrons and ions move in opposite (d) direction
- 31. A meter bridge is used to determine the resistance of an unknown wire by measuring the balance point length *l*. If the wire is replaced by another wire of same material but with double the length and half the thickness, the balancing point is expected to be

(a)	1	(b)(d) ₄ ¹
(a) (c)	_ 8	•
	8	16

- 32. Identify the INCORRECT statement regarding a superconducting wire
 - (a) transport current flows through its surface
 - (b) transport current flows through the entire
 - area of cross-section of the wire (c)
 - it exhibits zero electrical resistivity and (d) expels applied magnetic field

A sample of HCl gas is placed in an electric field 3×104 NC-1. The dipole moment of each HCl

- 33. molecule is 6×10-30cm. The maximum torque that can act on a molecule is
 - (a) $2 \times 10-34$ C2Nm-1(b) $2 \times 10-34$ Nm
 - (c) 18 × 10-26 Nm (d) 0.5×1034 C-2 Nm-1
- 34. When a metallic plate swings between the poles of a magnet
 - (a) no effect on the plate
 - (b) eddy currents are set up inside the plate and the direction of the current is along the motion of the plate
 - (c) eddy currents are set up inside the plate and the direction of the current oppose the motion of the plate
 - (d) eddy currents are set up inside the plate
- When an electrical appliance is switched on, it 35. responds almost immediately, because
 - (a) the electrons in the connecting wires move with the speed of light (b)
 - the electrical signal is carried by electromagnetic waves moving with the speed of light
 - (c) the electrons move with the speed which is

(d) close to but less than speed of light Two there leat incardesteen light bulbs are

- 36. connected as shown in the Figure. When the circuit is an AC voltage source of frequency f,
 - which of the following observations will be correct?



- (a) both bulbs will glow alternatively
- both bulbs will glow with same brightness (b) $\frac{1}{2 \sqrt{1/LC}}$

provided frequency f

- (c) bulb b1 will light up initially and goes off,
- bulb b2 wwiilll bbelin OkN a ncodn bsutalbn btl2y will be ON (d

) bulb b

is

constantly 37. A transformer rated at 10 kW is used to connect a 5kV transmission line to a 240V circuit. The ratio of turns in the windings of the transformer

- (a) 5 (b) 20.8
- (c) 104 (d) 40

Three solenoid coils of same dimension, same 38. number of turns and same number of layers of winding are taken. Coil 1 with inductance L1 was

Mound using a Mn wire of resistance 11 2 was wound using the Coisl i2m wiliatrh winidreu cbtuatn tchee L direction of winding was reversed in each layer; Coil 3 with inductance L

was wound using a superconducting wire. The self inductance of the coils L1, L2, L3 are

Light travels with a speed of 2 × 108 m/s in 39. glass of refractive index 1.5. What is the speed

of light in dense flint glass of refractive index 1.8 ? (a) (c) 1.33 × 108 m/s (b) 1.67 × 108 m/s

- 2.0 × 108 m/s (d) 3.0 ×108 m/s
- A parallel beam of fast moving electrons is 40. incident normally on a narrow slit. A screen is placed at a large distance from the slit. If the speed of the electrons is increased, which of the following statement is correct?
 - (a) diffraction pattern is not observed on the screen in the case of electrons
 - (b) the angular width of the central maximum of the diffraction pattern will increase
 - (c) the angular width of the central maximum will decrease
 - (d the angular width of the central maximum
 - will remain the same)

PART - II (CHEMISTRY)

- 675K 41. CHCH₃ HNO₃
 - (a) CH **3**CCHH22NNOO22 + CH3NO2 (b) CH 23 =N COH22

 - (c) 2CH
 - (d) CH
- When acetamide is hydrolysed by boiling with 42. acid, the product obtained is :
 - (a) acetic acid (b) ethyl amine
 - (c) ethanol (d) acetamide
- 43. Which will not go for diazotization?
 - (a) C6H5NH2 (b) C6H5CH2NH2 (c)

$$\begin{array}{c} H \\ H \mathbb{K}_{2} \\ \hline C_{6} H_{4} \\ \hline ON2 \\ \hline ON2 \\ \hline C_{6} H_{4} \\ \hline ON2 \\ \hline ON2$$

44. Secondary nitroalkanes can be converted into ketones by using Y. Identify the Y from the following



- 45. Alkyl cyanides undergo Stephen reduction to produce
 - (b) secondary amine (a) aldehyde (c) primary amine (d) amide
- 46. The continuous phase contains the dispersed phase throughout, Example is
 - (a)Water in milk

(b) Fat in milk

- (c)Water droplets in mist
- (d) Oil in water
- 47. The number of hydrogen atoms present in 25.6 g of sucrose1 (C2H22O11) which has a molar mass of 342.3 g is (a) 22 (h) 9 91 × 1023

(a)
$$22$$
 (b) 7.91×102
(c) $1023 11$ (d) 44×1023

Milk c×h 1a0ng2e3s after digestion into : 48.

(a) cel	lulose	(b) frເ	uctose
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- (c) glucose (d) lactose
- 49. Which of the following sets consists only of essential amino acids?
 - Alanine, tyrosine, cystine (a)
 - (b) Leucine, lysine, tryptophane
 - Alanine, glutamine, lycine (c)
 - Leucine, proline, glycine (d)

- 50. Which of the following is ketohexose? (a) Glucose (b) Sucrose (d) Ribose (c) Fructose
- The oxidation number of oxygen in KO3, Na2O2 is 51. (a) 3. (b) 1,0 (c) 2 (d) -0.33, -1
- ReactOio,n of PCl3 and PhMgBr would give 52. (a) br1omobenzene c(bh)lorobenzene t(cri)phenylphosphine d(dic) hlorobenzene
- Which of the following is not a characteristic of 53. transition elements?
 - (a) Variable oxidation states
 - (b) Formation of colored compounds
 - (c) Formation of interstitial compounds
 - (d) Natural radioactivity
- Cl P Cl bond angles in PCl5 molecule are 54.
 - (b) 60° and 90° (d) 120° and 30° (a) 120° and 90°
 - (c) 60° and 120°
- The magnetic moment of a salt containing Zn2+ 55. ion is
 - (a) 0 (b) 1.87 (c) 5.92 (d) 2
- The number of formula units of calcium flouride 56. CaF2 present in 146.4 g of CaF2 are (molar mass of CaF2 is 78.08 g/mol)
 - (a) 1.129 1024CaF (2b) 1.146 1024 CaF
 - 7.808 1024CaF (d) 1.877 1024 2aF (c)
- The IUPAC name of th2 e given compound 57.

CoNH 3 5ClCl 2 is

- (a) pentaamino cobalt chloride chlorate
- (b) cobalt pentaamine chloro chloride
- (c) pentaamine chloro cobalt (III) chloride
- (d) pentaamino cobalt (III) chlorate

When SCN- is added to an aqueous solution 58. containing Fe(NO3)3, the complex ion produced is

- Fe OH2 2 SCN-(a)
- FeOH 2 5 SCN-(b)
- 2 FeOH 28 SCN-(c)
- 6 (d) FeOH 2 SCN

59.	Hair dyes cont aiop(a è(o)itrate (b gold chloride	68.	The electrochemical cell stops working after sometime because :
()	silver nitrate) copper sulphate Schottky defects occu (s I mainly in electrovalent		(a) electrode potential of both the electrodes(b) becomes zero
60.	compounds where)		(b) becomes zero(c) electrode potential of both the electrodes
	(a) positive ions and negative ions are of		(d) becomes equal
	(b) different size(c) positive ions and negative ions are of same		one of the electrodes is eaten away the cell reaction gets reversed
	(d) size	69.	The amount of electricity required to produce
	positive ions are small and negative ions	09.	one mole of copper from copper sulphate
	are big positive ions are big and negative ions are		solution will be
	small		(a)Faraday (b) 2.33 Faraday (c)Faraday (d) 1.33 Faraday
61.	The number of unpaired electrons calculated in	70.	Dipping iron article into a strongly alkaline
	CoNH3 $^{3}_{6}$ and CoF $^{3}_{6}$ are		solution of sodium phosphate
	Û Û		(a) does not affect the article(b forms Fe2O3. xH2O on the surface
	(a) 4 and 4 (b) 0 and 2 (c) 2 and 4 (d) 0 and 4) forms iron phosphate film
62.	The standard free energy change of a reaction		(C) forms ferric hydroxide
	is G 115kJ at 298 K. Calculate the	71.	(d Hydroboration oxidation of 4-methyl-octene would give
	equilibrium constant k 🌼 in log kp		(a) 4-methyl octanol
	R 8.314 Jk ¹ mol ¹		(b) 2-methyl decane
	(a) 20.16 (b) 2.303		(c) 4-methyl heptanol(d) 4-methyl-2-octanone
()	(c) 2.016 (d) 13.83	72.	When ethyl alcohol is heated with conc. H2SO4,
63.	If an endothermic reaction occurs spontaneously at constant temperature T and P, then which of	/	the product obtained is :
	the following is true ?		(a) CH 3COOC2H5 (bd)) C2CH2H42 (c) C2H6
	(a) $G > 0$ (b) $H < 0$ (c) $S > 0$ (d) $S < 0$	73.	Anisole is the product obtained from phenol by
64.			the reaction known as
	If a plot of log10C versus t gives a straight line for a given reaction, then the reaction is		(a) coupling (b) etherification (c) oxidation (d) esterification
	(a) zero order(b) first order(c) second order(d) third order	74.	Ethylene glycol gives oxalic acid on oxidation
65.	A spontaneous process is one in which the		with (a) acidified K2Cr 2O7
	system suffers :		(b)acidified KMnO 4
	(a) no energy change(b) a lowering of free energy		(c) alkaline KMnO4
	(c) a lowering of entropy	75.	(d periodic acid Diamond is hard
66.	(d) an increase in internal energy The half life period of a first order reaction is 1	, J.	becauldelie)four valence electrons are bonded to
00.	min 40 secs. Calculate its rate constant.		(b) each carbon atoms by covalent bonds(c) it is a giant molecule
	(a) $6.93 \times 10-3 \min -1(b) 6.93 \times 10-3 \sec -1$		(c) it is a giant molecule(d) it is made up of carbon atoms
67.	(c) 6.93 × 10–3 sec (d) 6.93 × 103 sec The molar conductivities of KCL NaCL and KNO.		it cannot be burnt
07.	The molar conductivities of KCl, NaCl and KNO are 152, 128 and 111 S cm2 mol-1 respectively.	76.	A wittig reaction with an aldehyde gives
	What is the molar conductivity of NaNO3? (a) 101 S cm2 mol-1(b)87 S cm2 mol-1		(a) ketone compound(b) a long chain fatty acid
	(a) 101 S cm2 mol−1(b)87 S cm2 mol−1 (c) −101 S cm2 mol−1(d)−391 S cm2 mol−1		(c) olefin compound
			(d) epoxide



84. If $\begin{vmatrix} z & 25 \\ z & 1 \end{vmatrix} = \begin{bmatrix} 5 \\ 0 & 1 \\ 0$

- 85. Argument of the complex number $\begin{pmatrix} 1 & 3i \\ 2 & i \end{pmatrix}$ (a) 45° (b) 135° (c) 225° (d) 240°
- 86. In a triangle ABC, the sides b and c are the roots of the equation $x^2 61x + 820 = 0$ and

 $A = \tan -14$ 3 , then a2 is equal to

- (a) 1098 (b) 1096
- (c) 1097 (d) 1095
- 87. The shortest distance between the straight lines through the points A1 = (6, 2, 2) and $A_2 = (-4, 0, -1)$, in the directions of (1, -2, 2) and (3, -2, -2) is $\begin{pmatrix} 6\\ (2)\\ (3) \end{pmatrix}$
- (d) 88. The center and radius of the sphere $x^2 + y^2 + z^2 + 3x - 4z + 1 = 0$ are
 - (a) $\frac{3}{2}$, 0, 2; $\frac{\sqrt{21}}{2}$ (b) $\frac{3}{2}$, 0, 2; $\sqrt{21}$ (c) $\frac{3}{2}$, 0, 2; $\frac{\sqrt{21}}{2}$ (d) 3, 2, 0; 221
- 89. Let A and B are two fixed points in a plane then locus of another point C on the same plane such that CA +CB = constant, (> AB) is
 - (a) circle (b) ellipse
 - (c) parabola (d) hyperbola The directrix of the parabola $y^2 + 4x + 3 = 0$ is
 - (a) $\begin{array}{c} x \\ 3 \\ \end{array} \begin{pmatrix} 4 \\ 3 \\ \end{array} \begin{pmatrix} 0 \\ 4 \\ 4 \\ \end{array}$ (c) $\begin{array}{c} x \\ 4 \\ 4 \\ 4 \\ \end{array} \begin{pmatrix} 3 \\ 4 \\ 0 \\ \end{array}$ (d) $\begin{array}{c} x \\ 4 \\ 4 \\ 4 \\ \end{array}$
- 91. If g (x) is a polynomial satisfying g (x) g(y) = g(x) + g(y) + g(xy) - 2 for all real x and y and g (2) = 5 thenLt g(x) is
 - (a) 9 (b) 10
 - (c) 25 (d) 20

- 92. The value of f(0) so that $\frac{(ex 2x)}{x}$ may be continuous at x = 0 is
 - (a) log <u>12</u> (b) 0 (c) (d) $-1 + \log 2$ Λ
- 93. Let [] denote the greatest integer function and f (x) = [tan2 x]. Then
 - (a) $\lim_{x \to 0} f(x)$ does not exist
 - (b) f(x) is continuous at x = 0
 - (c) f(x) is not differentiable at x = 0
 - d f(x) = 1
- 99. 94. A spherical balloon is expanding. If the radius is increasing at the rate of 2 centimeters per minute, the rate at which the volume increases (in cubic centimeters per minute) when the radius is 5 centimetres is (a) 10 (b) 100
 - (d) 50 (c) 200
- 95. The length of the parabola $y_2 = 12x$ cut off by the latus-rectum is

96. If I
$$\frac{x5}{\sqrt{1 x3}}$$
dx, then I is equal to

(a)
$$\frac{2}{9}(1 \times x^3)^{\frac{5}{2}} + \frac{2}{3}(1 \times x^3)^{\frac{3}{2}} + C$$

(b)
$$\log \left| \sqrt{x} \sqrt{1 x^3} \right|$$
 C

(c)
$$\log \left| \sqrt{x} \sqrt{1 x^3} \right|$$
 C

(d) $\frac{2}{9}(1 \times x^3)^2 = \frac{2}{3}(1 \times x^3)^2$ C

 $4x \sqrt{2}^2 y^2$ 8 is (b) 2 (a) (c) ³ (d) 4 $\frac{a x}{x}$ dx is The value of 198. a 7 a 4 (a) (b) а а (d) (c) Δ 2

97. Area enclosed by the curve

Let y be the number of people in a village at time t. Assume that the rate of change of the population is proportional to the number of people in the village at any time and further assume that the population never increases in time. Then the population of the village at any fixed time t is given by

- (a) y = ekt + c, for some constants c < 0 and k>0
- (b) y = cekt, for some constants c > 0 and k < 0
- (c) y = ect + k, for some constants c < 0 and k>0(d) y = kect, for some constants c > 0 and k < 0

100.The differential equation of all straight lines touching the circle $x^2 + y^2 = a^2$ is

(a)
$$y \frac{dy^2}{a^2 1} \frac{a^2 1}{a^2 1} \frac{dy^2}{dx^2}$$

(b) $y \frac{xddyx^2}{a^2 1} \frac{a^2 1}{dx} \frac{dy^2}{dx^2}$
(c) $y \frac{xddxy}{a^2 1} \frac{a^2 1}{dx} \frac{dy}{dx}$

(d)
$$y \frac{dy}{dx} a^2 1 \frac{dy}{dx}$$

101. The differential equation

$$\left|\frac{dy}{dx}\right| |y| 3 0$$

admits

- (a) infinite number of solutions
- (b) no solution
- (c) a unique solution
- (d) many solutions

102.Solution of the differential equation

xdy	yd	x √	x2	y2dx	0 is	
(a)	y ,	x2	y2	Cx2		
(b)	у	vx2	y2	Cx2		
(c)	x,	√x2	y2	Cy2		
(d)	x	√x2	y2	Cy2		
103.Let P	, Q, R	and	S be	statem	ents a	and suppose
that	Р	Q	R	P. if ~	S	R, then
(a)	S	~ Q		(b)	~ Q	S
(c)	~S	~ Ç)	(d)	Q	~S
104.In ho	w ma	iny ni	umbe	er of wa	ys ca	n 10 students
					cont	aining four
students	and th	ne otł	ner tl	ree?		
(a)	400			(b)	700	

(a)	400	(b)	700
(c)	1050	(d)	2100
105.If R b	e a relation define	ed as	a R b iff a - b >
ther	the relation is		
(a) r	eflexive	(b) s	symmetric
(c)	transitive		•
(d)	symmetric and ti	ransit	tive

0,

106.Let S be a finite set containing n elements. Then 1 the total number of commutative binary operation on S is

<i>·</i> · ·	n(n 1	n(n 1
(a)	nn ² (n2)	((bd)) _{2n² (n2)}
(c)	(n2)	(n2)

107.A manufacturer of cotter pins knows that 5% of

his product is defective. He sells pins in boxes of 100 and guarantees that not more than one pin will be defective in a box. In order to find the probability that a box will fail to meet the guaranteed quality, the probability distribution one has to employ is (b) Poisson (a) Binomial (d) Exponential (c) Normal (d) Exponential 108.The probability that a certain kind of component

 $\frac{3}{-}$. The will survive a given shock test is

probability that exactly 2 of the next 4 components tested survive is

- 9 25 (a) (b) 41 128
- 1 27 (c) (d) 5 128

109.Mean and standard deviation of marks obtained in some particular subject by four classes are given below. Report the class with best performance

	(a)	80, (b) 75, 5
	(\mathbf{c})	18 (d) 76 7
110.	A rar	18 (d) 76, 7 nd8o0m, variable X follows binomial
		ri2bu1tion with mean and variance . Then
	(a)	0 < < (b) 0 < <
	(c)	< 0 < (d) < 0 <
111.	The s	system of equations
		x + y + z = 0
		2x + 3y + z = 0
		x + 2y = 0
	ha	a unique solution; x = 0, y = 0, z = 0
	S	infinite solutions
		no solution
	(b)	finite number of non-zero solutions
	(c)	
	(d)	_
	0 b、	a ⁴ Q ₁
112.	(a)	$a \stackrel{4}{=} 0$ a = 1 = 2b
	(c)	a = b2 (b) $a = b$
440		(d) $ab = 1$
113.		= diag (d 1, d2,, dn) where d1 0, for
	= 1	L, 2,, n, then D–1 is equal to
	(a) [
	(b)	D Adj (D)
	(C)	
		diag $(d_{1}, d_{2}, d_{1}, d_{1}, d_{1})$
114.	1† x, y	y, z are different from zero and
		$\begin{vmatrix} a & x & b & z \end{vmatrix} = 0$ then the value of
		abycaxbzaxbycc
		a b c expression _{x y z} is
	the	expression x y z is
	(a)	
	(c)	1 (d) 2
115		ability of getting positive integral roots of
±±0.		equation $x^2 - n = 0$ for the integer n, $1 < n < 40$
	is	
	(a)	1 (b) 10
		5 ^(D) 10
		1

1 3 (c) (d) 20 20

116.The number of real roots of the equation

 $\sqrt{x4}$ x4 20 22 is 4 (b) 2 (a) (d) 1 0 117.L(9) , be the roots of the equation $x^2 - ax + b = 0$ and An = n + n. Then An+1 - aAn + bAn-1 is equal to (b) b (d) a – b (a) –a (c) 0

118.If the sides of a right-angle triangle form an A.P., the 'Sin' of the acute angles are

(b)
$$\sqrt[3]{3,1}{\sqrt{3}}$$

(c)
$$\sqrt{\frac{\sqrt{5}}{2}}, \sqrt{\frac{\sqrt{5}}{2}}$$

(d)
$$\sqrt{\frac{\sqrt{3}}{2}}, \sqrt{\frac{\sqrt{3}}{2}}$$

119. The plane through the point (-1, -1, -1) and containing the line of intersection of the planes

(c) r.(i^{4j} 5k⁾ 0

(d) r.(i^ 3k^) 0

120. a
$$\hat{i}^{\hat{j}k5\hat{j}and b} 2\hat{i}^{4\hat{j}3k}$$
 are one of the

sides and m^edians respectively, of a triangle through the same vertex, then area of the triangle is $j^{\hat{}}$

(a)	$\frac{1}{2}\sqrt{83}$	(b)	<u>√83</u>
	1		
(c)	$2\sqrt{85}$	(d)	$\sqrt{86}$

SOLUTIONS

PART - I (PHYSICS)

1. Interference pattern if they are coherent, they have same wavelength/frequency in same phase of having a constant phase difference and same state of polarisation.
Interference pattern if and the theory of diffraction at a single sit, the width of the central maximum is given by 2.
W
$$\frac{2D}{a}$$
 W D,
W $\frac{2D}{a}$ W D,
W $\frac{2D}{a}$ W D,
W $\frac{2D}{a}$ W D,
Therefore, to increase the width of the central maximum a should be decreased.
3. (b)R 1 and R2 ard; ths eht nhtweese didetergiditist to confing $= 3.2 \times 10^{-19}$ for 2.1×12^{-1} for 1.2×10^{-19} J.
We re t is the thickness of the soap solution.
For constructive interference,
2 t $\frac{1}{2}$ m 1
or 2 t m $\frac{12}{1}$ (1)
Similarly, 2t m $\frac{3}{2}$ 2...(2)
Solving (1) & (2), we get
 $\frac{1}{1}$ R2 n = 1
 $\frac{1}{1}$ $\frac{1}{1}$ $\frac{1}{2}$ $\frac{1}{1}$ $\frac{1}{2}$ $\frac{1}{1}$ $\frac{1}{2}$ \frac

V

answer. But 5V is approximately equal to the exact potential. Therefore, option (b) should be the correct option.

7. (b)Davison and Germer performed an experiment to prove that matter has a wave nature. The experiment was based on electron diffraction.

8 (c)We have, N =
$$_{t}$$
 N₀ $\frac{12T1/2}{-1}$,

When

NNt = number of atoms present after time t 0 = initial number of atoms

$$T1/2 =$$
 half life of the nuclide

$$\frac{N_{0t}}{N} = \frac{1}{2} \frac{T_{1/2}^{t} \text{ or } 1}{16} = \frac{1}{2} \frac{T_{1/2}^{2}}{16} = 13.$$
or $\frac{1}{2} \frac{4}{12} \frac{1}{2} \frac{7}{T_{1/2}} = 4 \frac{2}{T_{1/2}}$

$$T_{1/2} = \frac{2}{4} \text{Hr} = \frac{1}{2} \text{Hr} = T_{1/2} = 30 \text{ min.}$$

9. (c)Due to time dilation the interval between two events at the same point in a moving frame appears to be longer by a factor

$$\sqrt{1 \frac{v^2}{c^2}}$$
 to an observer in a stationary

frame. Time dilation is independent of the direction of velocity and depends only on its magnitude.

10. (c)The - decay in the case of 234U takes place as follows :

1

11. (a)When electron jumps from the level n = 2 to the level n = 1, K x - rays are emitted. Similarly, Kx-rays are emitted when there is atransition of electron from the level n = 3 to the level n = shown in the figure. 1. X- ray spectra has been shown below.



No option is matching with the exact 12. (b)Let the number of and particles emitted be m and n respectively. Then

A - 4m = A - 8 m = 2 the mass number of a radioactive nuclide decreases by 4 due to emission of one particle] Aga in , (Z - 2m) + n = Z - 3[the atomic number decreases by 2 due

to emission of 1 -particle but increases by 1 due to emission of 1 - particle] or

or or
$$-2m + n = -3$$

 $2m - n = 3$
 $(2 \times 2) - n = 3$ (m=2)
 $n = 1$



For the Op-amp shown above, we have

Rf Vo VI RI

Comparing this circuit with the given one, We get V **∄1**,Rf = 10k $= 10 \times 10^{\circ}$ $RI = 1k = 1 \times 103$

14.(d)The solid is an n-type semiconductor. In an ntype semiconductor, the impurity is pentavalent which is also called the Donar impurity because one impurity atom generate one electron. The Donor energy level lies just below the conduction band as



$$\begin{array}{cccc} \frac{I_D}{I_S} & 1 & e \overset{VO}{VT} & \text{or ln 1} & \frac{I_D}{I_S} & \frac{V_D}{nV_T} \\ \\ V_D & nVT \ln 1 & \frac{I_D}{I_S} & = VT \ln 1 & \frac{I_D}{I_S} \\ \\ & & = VT \ln & \frac{I_{majority}}{IS} \end{array}$$

Here, n_e (101 7 1016)cm 3

We know that, ne
$$n_h n_1^2$$

 $n_h \frac{n_i^2}{n_e} \frac{(1.4 \ 10^{10})2 \ \text{cm3}}{9 \ 10^{16}}$
Also, $\frac{\text{I maj ori tyn}^{\text{e h}}}{\text{IS} n_1}$

$$V_{\rm D} = \frac{k_{\rm T}}{-e_{\rm I}n} = \frac{9 \ 10^{16}}{(1.4 \ 10^{10})^2} \\ 9 \ 10^{16}$$

 $= \frac{\text{keTln}(4)}{10^{12}}$



1.9. (a)Antenna length =

Antenna length

Here, AM FM Antenna length for AM should be longer than that of FM.

1

20. (a)The principle of communication using optical fibers is based on the principle of total internal reflection.



- 21. (d)According to quantization of charge, the charge of any system is an integral multiple of the charge of electron which is the least amount of charge on any system.
- 22. (b)The charge on the capacitor when connected to the battery is given by



Q = CV = $(900 \times 10-12 \text{ F}) \times 100 \text{ V} = 9 \times 10-8 \text{ C}$ When the battery is replaced by another capacitor of 900 pF capacitance, the charge of 9 $\times 10-8 \text{ C}$ is distributed on both. Let Q and Q2 be the charge on each of them.

Q = Q1 + Q2= C1V + C2V, where V is the common potential.

or V =
$$\frac{Q}{C1 C2}$$

As the two capacitors are in parallel, the equivalent capacitance is given by C = C1 + C2

1

Total energy of the capacitors =
$$\frac{1}{62}$$
 V2
= $\frac{1}{2}$ C₁ C₂ Q²
= $\frac{1}{2}$ C₁ C₂ ² = 2(C1 C2)
9 10^{8 2}
= 2(900 10 12 900 10¹²)
(9)2 10¹⁶
= 2 2 9 10¹⁰ = 2.25 × 10-6 J
23. (c)We know that R = $\frac{1}{A}$
For $l = L$ and $A = A$; R1 $\frac{L}{A}$
For $l = L$ and $A = A$; R1 $\frac{L}{A}$

$$R2 = \frac{\frac{L}{2}}{2A} \quad \frac{1}{4} \quad \frac{L}{A} = \frac{1}{4}R1$$

For $l = 2L$ and $A = \frac{A}{2}$;
 $R_3 \quad \frac{2L}{A} \qquad \frac{L}{A} = 4R_1$

2 Thus R3 > R1 > R2 Therefore, the wire having length 2L and area A

24. (d)We know that the electric field at any point due to an electric dipole varies inversely with the cube of the distance of the point from the centre of the dipole, that is,



$$F = qE$$
 $F = \frac{1}{r3}$

When the distance of the charge becomes 2m, i.e. double of its initial value, then new force (F ') will become

$$F' = (2)3.F = 8$$

25. (c) Let us first calculate the total charge on the

soild sphere. Let us consider a concentric sphere of radius r and thickness dr. Then volume of the sphere, dV = 4r2dr

Given, the volume charge density of the sphere = $\frac{0}{r}$

Charge on this sphere,

$$dQ = .dV \quad \frac{0.4r^2}{r} dr = 4 \quad .rdr.$$

Total charge on the whole solid sphere,

$$Q_{s} = \begin{pmatrix} R^{1} \\ 0 \end{pmatrix} = \begin{pmatrix} R^{2} \\ 0 \end{pmatrix} \begin{pmatrix} R^{2} \\ 2 \end{pmatrix} = \begin{pmatrix} R^{2} \\ 0 \end{pmatrix} \begin{pmatrix} R^{2} \\ 2 \end{pmatrix} = \begin{pmatrix} R^{2} \\ 0 \end{pmatrix} R^{2}$$
(1)

Now, the total charge on the hollow sphere, Qh = -(4R22) ... (2) By question, Qs + Qh = 0 $2 - R_2^2 = 4R2_2$

$$\frac{R^{2}2^{2}}{2} = \frac{0}{2} = \frac{R^{2}}{2} \sqrt{\frac{0}{2}}$$

26. (b)A charge Q will be induced on the inner surface of the solid spherical conductor. An equal but opposite charge will be induced on the outer surface of the conductor. There will be no charge at a position between the inner and outer surface.



27. (b)The energy stored in a capacitor is given by

$$E = \frac{Q^2}{2C}$$

Here, C
$$\begin{array}{c} l2n \ OL \\ R2 \\ R1 \end{array}$$
 , where

L = length of the cylindrical conductor R R2 == oinunteerr rraaddiiuuss

When both Q and L are doubled, by keeping other parameters fixed, the energy stored (E $\dot{}$) becomes

_

С

28. (c)Redrawing the figure, we get



the same is the case with another 4 and 2 resistors. So, the four resistors are equivalent to following two resistors. Now, in fig (b) these two 6 resistors are in parallel.

6 Equivalent resistance, R б -6 = 12

36

- 29. (b) In a conductor, the charge carriers are electrons. As the temperature is increased, the collisions of these conduction electrons with the fixed ions of the lattice of the metal increases and hence the resistance of the conductor also increases.
- If there is no potential difference through a 30. (b) metallic wire, the current is zero because the electrons drift in a random direction with a speed of the order of 10-2 cm/s so that the net charge crossing a particular cross-section 34.(c) When a metallic plate swings between the in a given time is zero. If the wire is replaced by another wire of same
- material but with double the length and half 31. the thickness, the resistance of the wire as a whole will change. Let us calculate this ch a n ge.

Initial resistance, R =
$$egin{array}{cc} L & L \\ A & r2 \end{array}$$

Fubak resistance, R'

$$\frac{2L}{A} = \begin{array}{c} 2L \\ \Gamma \\ 2 \end{array}$$

$$r^{8L}_{r^2} = 8 \frac{L}{r^2} = 8R$$

Therefore, the resistance will increase by eight times.

=

In a meter-bridge, we have

$$\frac{R}{S} = \frac{l}{100 - l}$$
wh er eR = unknown resistor
S = known resistor
l = balancing length
l = \frac{100R}{S - R}
When the resistance of the negligible

w wire is 8R then the new balancing length will be

$$\frac{100 \text{ 8R}}{\text{S} \text{ 8R}} = \frac{100 \text{ 8R}}{(\text{S} \text{ R}) \text{ 7R}}$$

$$= \frac{100 \text{ 8R}}{100 \text{ R}} \text{ 7R}$$

$$\frac{100 \text{ 8R}}{100 \text{ 7R}}$$

No option is correct.

32.(b)The transport current flows through the ace of the superconducting wire and dot

33.(c)Here,
$$E = 3 \times 104 \text{ NC} - 1$$

 $p = 6 \times 10 - 30 \text{ Cm}$

max = ?

We have. torque acting on a dipole = pE sin

, i.e. max = pE

- poles of a magnet, eddy currents are set up inside the plate. These currents set up their own magnetic field which opposes the magnetic field of the poles. Thus, the direction of the current opposes the motion of the plate.
- 35.(b)When an electrical appliance is switched on, the electrons in the conducting wires move with their drift speed which is very less than the speed of light. But as soon as the switch is on, an electromagnetic wave is set up inside

the conductor and the electrical signal is carried by them. The speed of electromagnetic wave is, of course, equal to the speed of light and hence the appliance responds almost immediately after the

switch 36.(b):The dir curit shown is a parallel resonant

circuit. The frequency is
$$f = \frac{1}{2 \sqrt{LC}}$$
 at

resonance. Also, at resonance, the capacitative reactance is equal to the inductive reactance. Therefore, equal current will flow through both the bulbs b1 and b2. So, both will glow with same brightness. 41 37. (b)In a transformer, the ratio of turns in the windings is given by NPVP NSVS Ν 5kV 5000V $240V = \frac{0000V}{240V} = 20.8$ Р NS 38. (a)Self - inductance (L) of a solenoid = oN_{TA} where o = absolute permittivily of space/ 42. air N = number of turns in the coil A = area of cross-section of the solenoid *l* = length of solenoid. This expression shows that for all three solenoids, the self-inductances will be equal. 43. 39. (b)We know that the refractive index of a medium is given by CO С Where c = velocity of light in the medium co = velocity of light in vacuum For crown glass, $1.5 \frac{c_0}{2 108}$... (1) For flint glass, 1.8 $\frac{c_0}{c}$...(2) 2 108 1. Dividing (2) by (1), we get 8 1. or c = $\frac{1.5}{1.8} \frac{2}{10^8} \frac{10^8}{m/s} = 1.67 \times 108 \frac{1}{m/s}$ 40.(c)Fast moving electrons create electromagnetic waves. So, the diffraction pattern will be

observed. Also, the angular width of the central maximum is given by

 $W = \frac{1}{a}$, where a = width of the slit

= wavelength of the light. When the speed of electrons will increase, the frequency will increase which will result in decreasing the wavelength as the speed of light is a constant. Therefore, the angular width will decrease.

PART - II (CHEMISTRY)

(b)Aliphatic nitro compounds are prepared by vapour phase nitration of alkanes at 693-793K, under pressure. Alkanes though less reactive do undergo nitration to give a mixture of nitro alkanes resulting through cleavage of carbon-carbon bond alongwith oxidation product like CO2. NO2. H2O etc.

۷0 ₂ (20%)

(a)Amides are hydrolysed rapidly by acids to produce carboxylic acid and ammonium salt;

H30 RCONH 2 RCOOH NH 4 Hence acetamide will give acetic acid on hydrolysis.

(b)Diazotisation reactions are shown by primary aromatic amine only as the arene diazonium salt formed is stable at 273-278 K. Compound CH5CH2NH2 is not an aromatic amine, hence

will not give the test/reaction.

44. (aS)econdary nitro alkanes upon hydrolysis with boiling HCl gives a ketone & nitrous oxid e. 2R2CHNO2

45. (a) Stephen reduction is partial reduction of alkyl or aryl cyanides to give corresponding aldehydes with a suspension of anhydrous stannous chloride in ether.

46. (a)In a colloidal system, the substance present in large amount in the mixture is called the dispersed medium & the solute is called dispersed phase. In case of milk and water solution the dispersed phase is milk protein & fat and water is dispersed medium.

47. (b)No. of moles of a compound

given mass (gm) Molar mass (gm)

i.e. $\frac{25.6}{342.3}$ = 0.0748 moles.

× 1023 molecules of it.

Hence 0.0748 moles contains = 6.022 × 1023 × 0.0748

= 0.4504 × 1023 molecules.

1 molecule of sucrose by formula is having 22 atoms of hydrogen.

0.4504 × 1023 × 1023 × 22 = 9.91 × 1023 atoms of hydrogen.

48.(c)Milk contains lactose as milk sugar. After digestion of milk lactose is broken down by enzymes lactase to form glucose and galactose before it enter the blood stream.

49.(b)Out of 20 amino acids, the 10 amino acids which human body cannot synthesize are called essential amino acids. The ten essential amino acids are :

1) Valine 2) Leucine 3) Isolucine 4) Histidine 5) Phenylanaline 6) Methionine 7)

Tryptophan 8) Lysine 9) Arginine 10) Th reon in e.

50.(c)Among the given examples, glucose is an alcohexose, sucrose is a disaccharide. fructose is a ketohexose while ribose is a aldopentose.

51.(d)To find the oxidation number of a given compound we have to equate the charge on the overall compound with the charge on individual atom of which the compound is made of.

In KO 3. K is an alkali metal. hence its oxidation number is +1.

$$(+1) + 3 \times (x) = 0 \text{ or } x = \frac{1}{3}$$
 0.33

hence oxidation number of oxygen i.e. x = -0.33. In Na2 O2, again Na is an alkali metal. Hence $2 \times (+1) + 2 \times x = 0$

electronegative than magnesium. Hence the

$$x = \frac{2}{2}$$
 1

52.(c)In a reaction the alkyl part of grignard

reagent acts as a nucleophile as carbon is more

х

Hence the Ph- will attack the phosphorous in PCl 3 to form organic phosphine with formula Ph3P. 3PhMgBr PCl₃ PhP 3MgBrCl

Triphenylphosphine

53.(d)Transition elements or d-block elements have 1 mole of sucrose (C12 H22O11) contains 6.022 riable oxidation states, they form coloured

> compounds because of partially filled d- orbitals and also because of small size they form interstitial compounds. They are stable elements and does not show radio activity.

(a)In PCl, ph s undergoes spd ³ 5osphorou hybridization and has trigonal bipyramidal géometry. It has two axial chlorine atoms & three equatorial chlorine atoms bonded to the central P.

Hence bond angles for axial are 90°, Cl–P–Cl & for equatorial Cl–P–Cl it is 120°.



55.(a)Magnetic moment of a salt depends upon the number of unpaired d-electrons. In Zn2+

salt configuration of cation is 4s03d10. Hence

total no. of unpaired electron, n is zero. So magnetic moment i.e.

B.M. √n(n 2) 0.

56.(a)Formula unit = no. of molecules of CaF 2.

massingm 146.4gm 1.875 Moles = molarmass 78.08gm

Molecules = Mole × 6.022 × 1023 $= 1.875 \times 6.022 \times 1023$

$$= 1.129 \times 1024$$
 units of CaF,

complex here. [Co(NH)Cl]2+35 The names of ligands will come first in alphabatical order, followed by metal ion with its oxidation state written in bracket or parentheis in Roman number i.e. Co (III) here.

IUPAC name for cationic complex Pentaamine chloro cobalt (III).

alkyl part will get attached to the electron This will follow the name of anion with a gap. deficie3n,t cshpleocriinees. is more electronegative than I.e. Pentaamine chloro cobalt (III) chloride. In PCl phosphorous.

- (b)Fe (III) ion from ferric nitrate will react with 65. (b)The driving forces which are responsible for 58. thiocyanate, SCN- ion to form a blood red complex i.e. FeSCN2+. But in presence of water it forms a complex containing five water molecules. i.e. [Fe (H2 SOi)lv5e (rS nCiNtr-)a]2.t+e has been ndency for maximum randomness. i.e.
- 59. (c) used since the begining of nineteenth maximum entropy century to dye hair. Silver salts darken when 66. (b) For 1st order reaction. exposed to light and silver combines with protein yeilding a dark coloured proteinate.
- 60. (b)Schottky defect is generally shown by compounds which have ionic nature and small difference in the size of cations & anions. In this defect equal no. of cations & anions is found missing from their lattice sites.
- and $\{CoF6\}^{3-}$ both the 61. (d)In [Co(NH)]3⁺₅₆ and {CoF6} ³⁻ both the oxidation state of cobalt ion is +3. In first case NH stronghefineedult lag aliget nchevelocehishe electrons in Co (+III) i.e. 4s03d6 get paired to form inner unpaired electron. On the otherahand mole a week field ligand hence it forms an outer orbital complex with 4 68. (c)As we know that unpaired electrons.
- 62. (a) $G^{\circ} = -115 \text{ kJ at } 298 \text{K}.$ Now, $G^{\circ} = -2.303 \text{ RT} \log kP$ R = 8.314 JK-1 mol -1 & I = 298K.

63. (c) For a reaction to take place spontaneously the value of G must be negative i.e. G< 0. Now, G = H - TS. As the reaction is endothermic, so value of

> H must be positive, i.e. H > 0. Hence to have a negative G. As T & P are constant. H < TS. TS must be positive to give the total value a negative sign. Hence S> 0.

64. (b)Any first order reaction follows the equation

$$log[A] = 2.303 t + log[A]$$

it resembles equation of straight line y = mx + Cy = log [A] i.e. log 10 C m = 2.303 if x = t & C = log [A]0

hence the plot is for a 1st order reaction.

a process to be spontaneous are :

i)Tendency for minimizing energy

maximum entropy

$$t\frac{1}{2}$$
 (half life time) $=\frac{0.693}{K}$

Hence K =
$$\frac{0.693}{t_{12}^{1/2}} = \frac{0.693}{(60 \quad 40)\text{sec}} = 0.693 \times t_{12}^{1/2}$$

67. (b)Since NaNO 3 is formed by the reaction Nacl KNO3 NaNO3 KCl

hence, using Kohlrausch's law

Ecell = Ecathode - Eanode when Ecathode = Eanode

If Ecell = 0 no net reaction occurs. The reactants and products are at equilibrium and no current will flow.

Note that it is only possible to obtain electrical work from a system that is not at equilibrium. In order for current to flow, there must be a net reaction occurring. As the oxidation- reduction reaction proceeds toward equilibrium, and the concentrations of the reacting species approach their equilibrium values, the EMF of the cell decreases to zero. When the system is at equilibrium, the cell potential is zero and we have a dead battery.

- 69. (c)In4 C suoSluOtion, oxidation state of Cu is +2. Hence one mole of copper sulphate will require charge equal to two moles of electrons to form metallic Cu. Mole charge = IF. Hence 2 Faraday is required.
- 70. (c)Rusting of iron is generally promoted in an acidic aqueous medium. Alkaline medium prevents availability of H+ ions. Sodium phosphate will cause formation of a protective film of iron phosphate on the iron preventing rusting. These solutions are used in car radiators to prevent rusting of iron parts.

71. alcohols containing same number of carbon atoms. The addition follow anti-Markowi Koff's rule. Boron atom act as an electrophile. Main two steps re involved. Reagent used BH3 & NaOH/H2O2.

4 - methyl octene

- 72. (d)Et2hSyOl a4lcohol on treating with conc. H undergoes dehydration to form alkene i.e. ethylene
 - Conc C2H5OH C2H4 H2O H§0 4

0 CH3

73. (b)An, Pishoelen yişl mOethyl ether. It

can be prepared by treating phenol first with a base like NaOH to form phenoxide ion. The phenoxide ion will then substitute the halide of an R-X molecule, to form methyl phenyl ether.

74. (c)Alkaline Potassium permanganate is a strong oxidising agent. It oxidises ethylene glycol to oxalic acid.

75. (a)In the structure of diamond each carbon atom in sp3 hybridised & is covalently bonded with four other carbon atom held at the corners of a regular tetrahedron by covalent bonds. This results in a very big three dimensional polymeric structure in which C - C distance is 154 pm and bond angle is 109.5°. Owing to very strong covalent bonds by which atoms are held to gether diamond is the hardest substance known.

(a)Hydroboration-oxidation of alkenes give 76. (c)The witting reaction is a chemical reaction of aldehyde or ketone with triphenyl an phosphonium ylide to give an alkene and triphenyl phosphine oxide.

$$C = O + (C6 \text{ H5})3 \text{ P} = C$$

$$R'$$

$$OR$$

$$CH0)P_{53} - C$$

$$R'$$

$$CH0)P_{53} - C$$

$$R'$$

$$CH0)P_{53} - C$$

$$R'$$

$$CH0)P_{53} - C$$

$$R'$$

$$R'$$

$$R'$$

$$CH0 + C$$

$$CH0$$

77. (a)Cannizaro's reaction is for those aldehydes which does not contain - hydrogen atom. This is also called self oxidation - reduction reaction. Among the given carbonyl compounds only HCHO does not have - h ydr ogen .

oxide

78. (c)
$$\bigcirc + CO$$
 $\xrightarrow{AlCl_3} \bigcirc + CI$

When a mixture of CO and HCl gas is passed through benzenenportsheathaylydset consisting anhydrous AICI

HOCL AICl 3 C6H5CHO CH₆ HCl

79.(b)Maleic acid & fumaric acid are both the isomers of butene dioic acid. Maleic acid is



80. (c)Alkali formate i.e. HCOONa with soda-lime i.e. NaOH + CaO will react to give Na 2CO3 and hydrogen gas is liberated.

> CaO HCOONa NaOH Na2CO3 H

PART - III (MATHS)

81. (c) a (b c)
$$\frac{1}{2}b$$

(a.c)b
(a.b)c
(a.bcos
(b.bet tan-1x =
x tan $\frac{sin}{cos} \frac{sin}{\sqrt{1} sin2}$
sin²
(1 x²)
sin²
(x²) sin²
(1 x²)
sin²
(x²) sin²
(x²

$$\sin \frac{1}{\sqrt{1 - x^2}}$$

$$\tan \frac{1}{x} - \frac{\sin 1}{\sqrt{1 - x^2}}$$
Now, sin (tan-1x) = sin sin $\frac{1}{\sqrt{1 - x^2}}$

$$= \frac{x}{\sqrt{1 - x^2}}$$
84. (c)Given that
$$\left|\frac{z - 25}{z - 1}\right| - 5 - |z - 25| - 5|z - 1|$$
Let Z = x + iy, then
$$|x - 25| - 5|x - 1| - 1|$$
Squaring both sides, we get
$$(x - 25)2 + y^2 = 25\{(x - 1)2 + y^2\}$$

$$x^2 - 50x - 625 - y^2$$

$$25x^2 - 50x - 25 - 25y^2$$

$$24x^2 + 24y^2 - 600 = 0$$

$$x^2 + y^2 - 25 = 0$$

$$|x + iy|^2 = 25 - |z|^2 = 52$$
85. (c)We
have, 1 - 1 - 3i - 2 - i - 4 - i^2
Now, let us put -1 = r cos, -1 = r sin
Squaring and adding, r2 = 2 i.e., r = \sqrt{2}
So that cos $= -\frac{1}{2}$, sin $= -\frac{1}{2}$
Thus, argument is 225°.
86. (c)Since b and C are the roots of
$$x^2 - 61x + 820 = 0$$
, so
$$b + c = 61$$
, bc = 820
A tan $\frac{1}{3}$ tan A $\frac{4}{3}$ cos A $\frac{3}{5}$
Now, using the formula,
$$\cos A = \frac{b^2 - c^2 - a^2}{2bc}$$

a2 = b2 + c2 - 2bc cos A
= (b + c)2 - 2bc - 2bc cos A
= (b + c)2 - 2bc (1 + cos A)
= (61)2 - 2 × 820 1
$$\frac{3}{5}$$

= 3721 - 2624 = 1097

87. (d)Equation of first line,

 $\begin{array}{rrrr} \frac{x}{1} & \frac{y}{2} & \frac{z}{2} & \frac{z}{2} & k \text{ (s ay)} \\ x = k + 6, \ y = -2k + 2, \ z = 2k + 2 \\ \text{Hence, general point on the first line,} \\ P & (k + 6, -2k + 2, 2k + 2) \\ \text{Equation of second line,} \end{array}$

$$\frac{x - 4}{3} - \frac{y}{2} - \frac{z - 1}{2} / (say)$$

x = 3l - 4, y = -2l, z = -2l - 1

Hence, general point on the second line, Q (3l-4, -2l, -2l-1)Direction ratios of PQ are 3l - 4 - k - 6, -2l + 2k - 2, -2l - 1 - 2k - 2 i.e. 3l - k - 10, -2l + 2k - 2, -2l - 2k - 3 Now |PQ| will be the shortest distance between the two lines if PQ is perpendicular to both the lines. Hence,

$$1(3l \ k \ 10) \ (2)$$

$$(2l \ 2k \ 2) \ 2(2l \ 2k \ 3) \ 0$$
and $3(3l-k-10) + (-2)(-2l$

$$+ 2k-2) + (-2)(-2l-2k-3) = 0$$
i.e. $3l - 9k = 12 \text{ or } l - 3k = 4$...(i)
and $17l - 3k = 20$...(ii)
Subtracting equation (i) from (ii), we get
 $16l = 16$ $l = 1$
Putting this value of l in equation (i), we get
 $-3k = 3, \ k = -1$
P $(-1+6, -2(-1) + 2, 2(-1) + 2)$
 $(5, 4, 0)$
Similarly, $Q = (-1, -2, -3)$
Hence, shortest distance, PQ,
 $= \sqrt{(15)^2 (24)^2 (30)^2}$
 $= \sqrt{(6)^2 (6)^2 (3)^2} = \sqrt{36 36 9}$
 $= 9 \text{ units}$
88. (c) Since the centre and radius of the sphere
 $x^2 + y^2 + z^2 + 2 \text{ ux} + 2\text{vy} + 2\text{wz} + d = 0 \text{ are}$

$$(-u, -v, -w)$$
 and $\sqrt{u2 v2 w2} d$
respectively. So, for the sphere

x2 + y2 + z2 + 3x - 4z + 1 = 0,
Centre
$$\frac{3}{2}$$
, 0,2 , and
Radius = $\sqrt{\frac{3}{2}^{2}}$ 02 (2)2 1
 $\sqrt{\frac{9}{4}}$ 4 1 $\frac{\sqrt{21}}{2}$

89. (b)Let two fixed points be A (ae, 0) and B (-ae, 0). Let C (x, y) be a moving point such that AC + CB = constant = 2a (say)

i.e.,
$$\sqrt{(x \ ae)^2 \ (y \ 0)^2}$$

 $\sqrt{(x \ ae)^2 \ (y \ 0)^2}$ 2a
Or $\sqrt{x^2 \ y^2 \ a^2e^2 \ 2ae}$
 $\sqrt{x^2 \ y^2 \ a^2e^2 \ 2ae}$ 2a ...(1)
Or $l + m = 2a$...(2)
Where, $l^2 = x^2 + y^2 + a^2e^2 - 2aex$...(3)
and $m^2 = x^2 + y^2 + a^2e^2 + 2aex$...(4)
From, (3) and (4)
 $m^2 - l^2 = 4aex$
or $(m - l) \ (l + m) = 4 \ aex$
 $2a \ (m - l) = 4aex[From (2)]$
 $m - l = 2ex$...
Adding (2) and (5), we get (5)
 $m = a + ex$...
From (4) and (6), ()6a)ex
 $a^2 + e^2 x^2 + 2aex = x^2 + y^2 + a^2e^2 + 2$
 $x^2 \ (1 - e^2) + y^2 = a^2 \ (1 - e^2)$, we get
 $\frac{x^2}{a^2} \ \frac{y^2}{a^2(1 \ e^2)} \ 1$
Or $\frac{x^2 \ y^2}{a^2 \ b^2}$ 1, where $b^2 = a^2 \ (1 - e^2)$

This is the equation of ellipse. 90. (d)The equation of the parabola is

$$y^{2}$$
 4x 3 0
or y^{2} 4 x $\frac{3}{4}$...(1)

The directrix of the parabola

$$Y2 = -4aX$$
 ... (2)
is X = a.

On comparing the equation (1) and (2), we $\frac{3}{4}$ 4a = 4 and X get Х 3 and X or a = 1 Х 4 Hence the directrix of the parabola (1) is x $\frac{3}{4}$ lorx $\frac{1}{4}$ 0. 91. (b) g(x). g(y) = g(x) + g(y) + g(x y) - 2 ...(1)Put x = 1, y = 2, then g(1). g(2) = g(1) + g(2) + g(2) - 2 5g(1) = g(1) + 5 + 5 - 24g(1) = 8g(1) = 21 X 1 X 1 Put y in equation (1) , we get $g(x) g \frac{1x}{1}$ g(x).g g(1) 2 g(x).g – $g(x) g - \frac{x}{2}$ 2 2 [g(1) 2]This is valid only for the polynomial g(x) = 1 + xn... (2) Now g(2) = 5(Given) 1 <u>+</u> 2n = 5 n = 5 [Using equation (2)] + 2n = 4, 2n = 4, -4 Since the value of 2n cannot be -Ve. So, 2n = 4, n = 2 Now, put n = 2 in equation (2), we get g(x) = 1 + x2= Lt (1 x2) x 3 = 1 + (3)² = 1 + 9 = 10, -8ex 2^x 92. (d) f(x) х (1 x1! x2 x3 (1 2! 3! = 1 x log21! ..) 1 (bg2)2 x2 (log2)3 x3 3! 2! $f(x) = \log 2$ 1 x {(log2)2 1} 2! x32!{(log) 2³1}.... Putting x = 0, we get $f(0) = \log 2 - 1 + 0 + 0 + \dots = -1 + \log 2$.

93. (b)Check the continuity of the function f(x) = [tan 2 x] at x = 0.L.H.L. (at x = 0)lim[tan2(0 = lim[tan2x] h)] h 0 x 0 lim[tan2 h] [tan2 0] [0] 0 $= \frac{1}{h} 0$ R.H.L. (at x = 0) lim[tan2(0 h)] = lim[tan2x] h 0 x 0 = lim[tan2 h] [tan20] [0] 0 h 0 Now, determine the value of f(x) at x = 0. $f(0) = [tan 2 \ 0] = [0] = 0$ Hence, f(x) is continuous at x = 0. 94. (c)Let r and V be the respectively radius and volume of the balloon. Let t represents the time. The rate of increament in radius is dr 2 cm/minute. The volume of the dt balloon is given by 43 r³ ٧ Differentiating w.r. to t, we get d٧ 4 (3r2ddrt) dt 3 Substituting the values of and $\frac{dr}{dt}$, we get d٧ 52 ₂₎ 200 cm3 /minute (3 3 dt 95. (a)On comparing the equation of the parabola $y_2 = 12 \times \text{with the standard equation},$ y2 = 4 ax, we get 4 a = 12 or a = 3. îу A (3, 6) Х C(3,0) (0,0)0 B (3,-6)

Hence, the focus, point C will be at (3, 0)and the extremities of the latus-rectum AB will be at (a, 2a) and (a, -2a). So the coordinates of A and B are (3, 6) and (3, -6)respectively. Now we need to find the length (curve AOB) of the parabola. As it is not a straight line so we cannot directly find the length of this curve as we cannot directly apply Pythagorous theorem. Let us consider a small length ds on the parabola. Using pythagorous theorem for this length,

96.

97.

ds = $\sqrt{(dx)^2 (dy)^2} = \sqrt{\frac{dx}{dy}^2 1dy}$ s $\frac{6}{6}\sqrt{\frac{dx}{dy}^2 1.dy}$...(1)

From y2 = 12 x x =
$$\frac{y^2}{1}$$

 $\frac{dx}{dy} = \frac{2y}{12} = \frac{y}{6}$ Putting in (1),
s $\frac{6}{6} \sqrt{\frac{y}{6}^2} = 1 dy = 2\frac{6}{0} \sqrt{\frac{y^2 = 36}{36}} dy$
= $\frac{2}{6} \sqrt{y^2 = 6^2} dy$
Using $\sqrt{x^2 = a^2} = \frac{x}{2} \sqrt{a^2 = x^2}$
 $\frac{a^2}{2} \log x = \sqrt{a^2 = x^2} = C$
We get s $\frac{1}{3} = \frac{y}{2} \sqrt{62 = y^2} = \frac{62}{2}$
 $\log y = \sqrt{6^2 = y^2} = C = \frac{6}{0}$
= $\frac{1}{3} = \frac{6}{2} \sqrt{62 = 62} = 18 \log 6 = \sqrt{6^2 = 6^2}$
C 0 18 log 0 $\sqrt{6^2 = 0} = C$

$$= \frac{1}{3} 3.6\sqrt{2} 18\log 6 \quad 6\sqrt{2} \quad 18\log 6$$

$$= 6\sqrt{2} \quad 6\log \frac{6(1 \quad \sqrt{2})}{6}$$

$$= 6 \quad (\sqrt{2} \quad \log(1 \quad \sqrt{2}))$$
(d) I $\frac{x5}{\sqrt{1 \quad x3}} dx \quad \frac{x3.x2}{\sqrt{1 \quad x3}} dx$
Let $1 + x3 = t2$, so that $3x2 dx = 2t dt$
 $x2dx \quad \frac{2}{3}tdt$
I $\frac{(t^2 \quad 1) 2tdt}{1} \quad \frac{2}{3} \quad t^2 \quad 1)dt$

$$= \frac{2}{3} \frac{t3}{3} \quad t \quad c \quad \frac{2}{3} \quad \frac{(1 \quad ^{3}3)^{1/2}}{3} \quad (1 \quad x^3)^{\frac{1}{2}} \quad c$$
(d) The given curve is
 $[4(x \quad \sqrt{2})^2 \quad \frac{2}{3}(1 \quad x^{3\frac{1}{2}/2} \quad C)$
(d) The given curve is
 $[4(x \quad \sqrt{2})^2 \quad \frac{2}{y} \quad 1 \quad 8 \quad 4(x \quad \sqrt{2})^2 \quad \frac{y^2}{2} \quad \frac{2}{2}$
 $\frac{(x \quad \sqrt{2})^2}{\sqrt{\frac{2}{2}}} \quad \frac{y^2}{2\sqrt{\frac{2}{2}}} \quad 1 \quad ...(1)$
This is the equation of the ellipse having control ($\sqrt{2}$ 0)

centre $(\sqrt{2},0)$. Observe the figure of ellipse (1). The centre P is $(\sqrt{2},0)$. A and B are $\sqrt{2}$, $\sqrt{\frac{2}{-}}$,0 and

$$\sqrt{2}$$
 $\sqrt{\frac{2}{-}}, 0$ respectively.



The required area = $4 \times \text{area of figure PQB}$

$$= 4 \quad \frac{\sqrt{2}}{\sqrt{2}} \sqrt{\frac{2}{7}} y dx$$

$$= 4 \quad \frac{\sqrt{2}}{\sqrt{2}} \sqrt{\frac{2}{7}} \sqrt{\frac{8}{7}} \frac{4(x - \sqrt{2})^2}{\sqrt{x}} dx$$

$$= 4 \quad \frac{\sqrt{2}}{\sqrt{2}} \sqrt{\frac{2}{7}} \sqrt{\sqrt{\frac{2}{7}}} \frac{\sqrt{2}}{\sqrt{x}} \sqrt{\frac{2}{7}} \frac{\sqrt{2}}{\sqrt{x}} dx$$

$$= 8 \quad \frac{x - \sqrt{2}}{\sqrt{2}} \sqrt{\frac{2}{7}} \frac{\sqrt{x}}{\sqrt{2}} \sqrt{\frac{2}{7}} \frac{\sqrt{2}}{\sqrt{2}} \frac{\sqrt{2}}{\sqrt$$

$$=8 \frac{1}{\sqrt{2}} (0) + \frac{1}{2} \sin^{-1}(1) - 0 - 0$$

$$8 \frac{1}{2} - \frac{1}{2} 4 \text{ square units.}$$
98. (c) Let x = cos2, so that dx = -2a sin cos d
Now $a^{0}\sqrt{\frac{x}{x}}dx = \frac{0}{2}\sqrt{\frac{a \cos^{2}}{a\cos^{2}}}$ (asin cos)d
[$-\frac{1}{2}atx = 0; \quad 0atx = 1$]
= $a_{0}^{1/2}\sqrt{\frac{1}{2}\cos^{2}}2sin \cos d$
 $\frac{1}{2}f(x)dx = \frac{1}{0}f(x)dx$
= $a_{0}^{1/2}2csions = cos$
= $a_{0}^{1/2} = a_{0}^{1/2}(1\cos^{2})d$
[$\cos^{2} - 1 2sin2$]
= $a -\frac{sin2}{2} - \frac{1}{0}^{2}$
= $a -\frac{sin2}{2} - \frac{1}{0}^{2}$
= $a -\frac{1}{2} - \frac{1}{2}$
99. (b)According to the question,
 $\frac{dy}{dt} = y - \frac{a}{2}$
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95. (c)According to the question,
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 $\frac{dy}{dt} = \frac{a}{2}$
92. (c)According to the question,
 \frac{dy}

population never increases in time. And

another constant C cannot be negative because of eM > 0 always. Hence y = Cekt, for some constants C > 0 and k < 0.

100.(b)The given circle is, x2 + y2 = a2 Differentiating with respect to x, we get

$$2x \frac{2y ddxy}{2} 0 \qquad x \qquad y dd xy}{2} 0 \qquad (Squaring both sides)$$

$$x^{2} \frac{2xy}{dx} \frac{dy}{dx} \qquad y^{2} \frac{dy dx^{2}}{2} \qquad 0$$

$$2xy \frac{dy}{dx} \qquad x^{2} \qquad y^{2} \frac{dd x^{2}}{2} \qquad 0$$

$$2xy \frac{dy}{dx} \qquad x^{2} \qquad y^{2} \frac{dd x^{2}}{2} \qquad 0$$

$$2xy \frac{dy}{dx} \qquad x^{2} \qquad y^{2} \frac{dd x^{2}}{2} \qquad y^{2} \qquad y^{2}$$

Hence $\left|\frac{dy}{dx}\right| = |y| = 3$ 0 is not possible. Therefore, the given differential equation has

no solution.

102.(b)The given differential equation is

$$xdy \quad ydx \quad \sqrt{x^2 \quad y^2 dx} \quad 0$$
$$xdy \quad y \quad \sqrt{x^2 \quad y^2} \quad dx$$
$$\frac{dy}{dx} \quad \frac{(y \quad \sqrt{y^2})^2}{x}$$

This is the linear differential equation.
and Put y= vx, so that
$$\frac{dy}{dx} \vee \frac{xdv}{dx}$$
. Then
 $v \frac{xdvdx}{-} \frac{vx}{\sqrt{x^2 - v^2x^2}} \frac{\sqrt{x^2 - v^2x^2}}{x}$
 $v \frac{xdvdx}{-} v \sqrt{1 - v^2} \frac{\sqrt{x^2 - v^2x^2}}{x}$
Integrating both sides, we get
 $\frac{dv}{\sqrt{1 - v^2}} \frac{dx}{x}$
 $\log(v \sqrt{1 - v^2}) \log x \log C$
 $v \sqrt{1 - v^2} Cx$
 $\frac{y}{x} \sqrt{1 - \frac{y^2}{x^2}} Cx$ [y vx]
 $y \sqrt{x^2 - y^2} Cx^2$
103. (b) $\sim Q$ S $\sim S$ Q
But $\sim S$ R
 Q R, True [As P Q R P]
Hence $\sim Q$ S is true
104.(d)We know that the number of ways of

104.(d)We know that the number of ways of dividing (m+n+p) things into three groups containing m, n and p things respectively

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Further if any two groups out of the three have same number of things then number of ways

(m n p)! m!n!p! 2

Hence number of ways to divide 10 students into three teams one containing four students and each remaining two to three

105.(d)We observe the following properties : Reflexivity - Let a be an arbitrary element. Th en ,

|a a| 0|0 aR/a

This, R is not reflexive on R.

Symmetry – Let a and b be two distinct elements, then (a,b) R |a - b| > 0|b - a| > 0a b |b a| (b,a) R Thus, (a, b) R (b, a) R. So, R is symmetric. R. Transitivity – Let (a, b) R and (b, c) Then |a - b| > 0 and |b - c| > 0|a - c| > 0(a, c) R So, R is transitive. 106.(a) Let S = {ai } where i = 1.2....n From commutative operations, ai*aj aj*ai ... (i) i.j1.2.3....n where * represents a binary operation Number of distinct elements in S × S i.e., {ai} {aj} subject to the condition (i) i 1,2...n j 1,2...n =n{(a1,a1),(a1,a2).....(a1,an), (a2, a2), (a2,a3),....(a2,an), ...(an 1,an 1),(an 1,an),(an,an) n(n 1) n (n 1) (n 2) 2 1 No. of commutative binary operations = No. of functions f: S × S S subject to (i) = n.n.n...n(n 1) times n(n 1) 2 n 2 107.(b) Poisson distribution is a probability distribution which is obtained when the probability (p) of the happening of an event is same in all the trials and there are only two 112.(d)Here, events in each trials generally says successes and failures probability (p) of the happening of the event in trial is very less but number of trials (n) is very large. Here, p = 5% = $\begin{array}{c} 5 & 1\\ 100 & 20 \end{array}$ is very less and 20 n = 100, is very large. Hence, one has to employ the Poisson distribution in the given question. 108.(d)The probability that a component survives 1 is $p = \int_{1}^{1} .$ Then q = 1 - p = 144 [pq1] n takes the value 4 and r = 2. Hence the

required probability is

nCprnq r ${}^{4}C_{2} \begin{pmatrix} 3 & 2 & 1 & 2 \\ 4 & 4 & 4 \end{pmatrix}$ = 6 $\frac{3 & 3 & 1}{4 & 4 & 4} \frac{27}{128}$

109.(b)Performance of the class will be best if mean of the marks obtained is maximum but standard deviation of the marks obtained is minimum. Hence the class which has mean and

standard deviation of the marks obtained as 75 and 5 respectively performs best.

110.(b)Mean, np = ; and variance, npq = where n = number of trials and p + q = 1.

npa (1 p) q So, np 0 p 1 -1 < -p < 0 0 < 1 - p < 10 - 1 0 < < 111.(b) x + y + z = 0...(1) 2x + 3y + z = 0...(2) x + 2y = 0... (3) From equation (3), we have x = -2yPutting this value of x in equations (1), we -2y + y + z = 0 y = zget Hence x = -2zThus, the solution of the given system of equations is (-2z, z, z), where z is a parameter (Z R). Hence the system has infinite number of solutions including zero solution. a ² $0 a 0 a^{2}$ 0 b b 0 b 0 0

0 ab 0 = 0 0 a		0 ab	
0 Similarly, b a2b2 = 0 0	$\begin{array}{c} & 0\\ a & ab\\ 0 & 0\\ 0 & 0\\ 0 & 0\\ a & b^2 \end{array}$	$ \begin{array}{ccc} 0 & ab \\ ab & 0 \\ & a^2b^2 \\ = & 0 \end{array} $	0 ab 0 a 2 b ²
Now,			
0 a ⁴	a ² b ²	0	1 0
b O ^I	0	a ⁴b²	0 1
a2b2 = 1	ab = 1		

113.(d)D = diag (d 1, d2, ..., dn) d_1^1 0 0 0 d10 0 0 d_2^1 0 0 0d2 0 0 0 0 0 d_3^1 0 0 0 0 d3 D 0 0 0 0 0 d1n 0 0 0 0 = diag $(d11, d_2^1, \dots, d_n^1)$ 0 d1 0 0 0 d2 0 0 y b с z а 0 0 d3 0 |D| 0 114. (d) а Х b С z a x b y С a(bc bc bz cy yz) 0 0 0 0 0 (b y) (c z) (ac cx ac az cx zx) = d1 d2 d3 dn (ab ay bx xy ab bx) 0 d2 d 3d 4 ...dn 0 0 0 abz + acy - ayz - abz + bzx + ayz d1d 3d 4 ...dn 0 0 0 xyz - acy + cxy + ayz - xyz = 00 0 d1d2d4...dn 0 adj(D) ayz bzx cxy 2xyz 0 0 d1d 2 d 3 .n..d1 0 0 0 $\frac{a}{x}$ b y c z 2 0 (Dividing by xyz) d ¹ 🕂 adj (D) b а С 2 Х у Ζ 1 adj(D) d1d2d3....dn 115.(c) x2 - n = 0 x √n For each integral value of x [1, 40], There is d2 d3d 4 . ..dn 0 0 0 a positive root. Hence for 40 integral values 0 d1d3 d 4 ...dn 0 0 of x from 1 to 40, there are 40 positive roots, 0 0 d1d2d4...dn 0 out of which only six roots 1, 2, 3, 4, 5 and 6 are positive integral roots. Hence, probability 0 0 0 0 d1d2d3...d 1 of getting positive integral roots = $\frac{3}{40}$ 1 $x4 \sqrt{x4} \quad 240 \quad 2$ 0 0 0 d_1 116. (a) 1 $x4 - 22 = \sqrt{}$ 0 0 0 or d_2 Put x4 = y and square both the sides. 1 (y - 22)2 = y + 20 y2 + 484 - 44y = y + 20 0 0 0 $\overline{d_3}$ $y^2 - 45y + 464 = 0$ $y^2 - 29y - 16y + 464 = 0$ (y - 29) (y - 16) = 0 1 y = 16, 29 0 0 0 0 dn x4 = 16, 29 or x = <u>+</u> 2, <u>+</u> 2.31

3 20 117.(c) Since , be the roots of the equation $x^2 - ax + b = 0$, so each of them must satisfy the equation. Therefore

$$\sum_{n+1}^{2} \sum_{n+1}^{2} b \quad 0...(1) \text{ and } \sum_{n+1}^{2} b \quad 0 \quad ...(2) \\ \sum_{n+1}^{n-1} a \text{ An } + b \text{ An} - 1 = + \sum_{n+1}^{n+1} \\ -a (n - n) + b (n - 1 + n - 1) \\ = n - 1(2 - a + b) + n - 1(2 - a + b) \\ = n - 1(0) + n - 1(0) = 0 \quad [From (1) \& (2)]$$

118.(a) Let the sides of the triangle be a - d, a, a+d, where d is greater than zero. From the figure, it is clear that the angles A and C are acute angles. Now, by the theorem of Pythagorus, AC2 = AB2 + BC2 (a + d)2 = a2 +(a - d)2 a2 + d2 + 2ad = a2 + a2 + d2 - 2ad4ad = a2

$$d = a/4$$

A
 $a + d$
B
 $a - d$ C

119.(a) The plane containing the line of intersection of the planes3 and

С

- r.(j 2k) 0 is
- r.(i 3j k) [r.(j 2k)] 0

r.[i (3)j (2 1)k] 0 ...(1) Since the plane (i) passes through the point (-1, -1, -1) or (i j k), so this point must satisfy (i). Hence,

i j k.[i (3)j (2 1)k] 0 1 (3) (2 1) 0 3 0 3 1 Substituting this value for in (i), we get the required plane r.(i 2j 3k) 0 120.(d)In the figure, OAC is a triangle and OB is a median such that OA a i ĵ^k^ b ²ⁱ 4j^{3k²} OB 0C c (say) 0 ลี Б OA OC 20B a c 2b c 2ba $2(2i^{4}j^{3}k^{3})(i^{5}k^{3})$ = (3i[^] 9j[^]5k[^]) Now, the area of the triangle, ¹ 2φA oc∣ ____a c Her e, $\begin{array}{c|cccc} & \hat{i} & \hat{j} & k \\ a & c & 1 & 1 & 1 \\ 3 & 9 & 5 \end{array}$ $=\hat{i}(5 \ 9) \ \hat{j}(5 \ 3) \ k^{(93)}$ = 14i²j¹²k <u>2(</u>7i[^] j⁶k⁾ $|ac| = 2\sqrt{(7)2(1)2(6)2}$ = 2 \sqrt{49} 1 36 2\sqrt{86} 2,86 ,86. 2