VITEEE 2016 Question Paper

Vellore Institute of Technology Engineering Entrance Examination

SOLVED PAPER
(memory based)

VITE EE 2016

GENERAL INSTRUCTIONS

- This question paper contains total 125 questions divided into four parts :
  Part I : Physics Q. No - 1 to 40
  Part II : Chemistry Q. No - 41 to 80
  Part III : Mathematics Q. No - 81 to 120
  Part IV : English Q. No - 121 to 125
- All questions are multiple choice questions with four options, only one of them is correct.
- For each correct response, the candidate will get 1 mark.
- There is no negative marking for the wrong answer.
- The test is of 2½ hours duration.

PART - I (PHYSICS)

1. The potential energy of a system increases if work is done
   (a)upon the system by a non conservative for ce
   (b)by the system against a conservative force
   (c) by the system against a non conservative for ce
   (d)upon the system by a conservative force

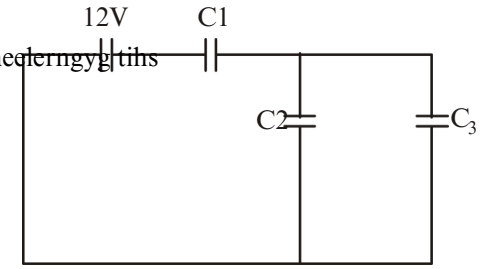
2. In photoelectric effect, initially when energy of electrons emitted is Eo, de-Broo. gNlioe ww,a evneclerngyg tihs associated with them is doubled then associated de-Broglie wavelength is

   (a) $\frac{o}{\sqrt{2}}$ (b) $\sqrt{2}$ o

   (c) o (d) $\frac{o}{2}$

3. In Wheatstone bridge, 4 resistors P = 10, Q = 5, R = 4, S = 4 are connected in cyclic order. To ensure no current through galvanometer(c)
   (a) (b5) (cr)e s(ids)t aInce is connected in series with Q
   given4 circeusiistt,a Cnce is connected parallel to S
   1 resistance is connected in series with P
   0 resistance is connected in series with R
   4

4. 1 = C2 = C3 = C initially. Now, a dielectric slab of dielectric constant $K \frac{3}{2}$ is inserted in C2.



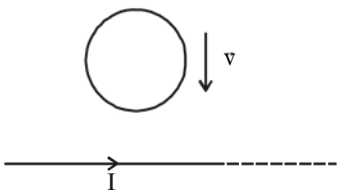
The equivalent capacitance become

(a) $\frac{5C}{7}$ (b) $\frac{7C}{5}$

(c) $\frac{2C}{3}$ (d) $\frac{C}{2}$

5. If the terminal speed of a sphere of gold (density = 19.5 kg/m3) is 0.2 m/s in a viscous liquid (density = 1.5 kg/m3), find the11. terminal speed of a sphere of silver (density = 10.5 kg/m3) of the same size in the same liaquid0.4
(b) 0.133 m/s
) m/s
) 0.2 m/s

6. I(cn sh0o.1wn fig, the circula(rd loop of wire is m)ovemd/ swith velocity tow)ards the infinite current carrying wire. Then



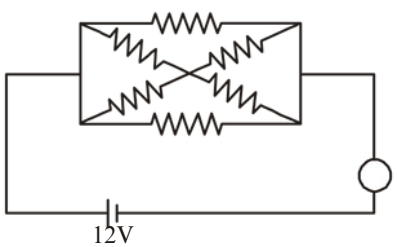
n(ao) current is induced in loop
c(bu)rrent is induced in loop clockwise
c(cu)rrent is induced in loop anticlockwise
e(dx)tra charges are induced on the wire loop

7. For a current carrying inductor, emf associated is 20mV. Now, current through it changes from 6A to 2A in 2s. The coefficient of mutual inductance is
(a) (2c0) mAH square cu(rbrent1 0c marHrying loop is chan1gmedH to a circular)loop2 i nm tHime t

8. (d
1.) Then
(a emf is induced in loop for time t
) emf is induced in loop for time t 1> t
(b no emf is induced in loop during whole process
) emf is induced due to change in magnetic
(c fi el d
(d
)

9. Hologram is based on phenomenon of
(a) diffraction
(b) polarisation
(c) interference
(d)total internal reflection

10. In given circuit, all resistances are of. 1C0urrent flowing through ammeter is



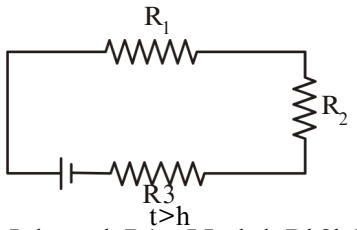
(a) (3c).6 TAhe waveleng(bth o1f. 8 aAn electron for trans2it Aion from) 1 A
(d
9)
a state nl to n 2is 8R. Which of the following wavelengths is possible for a transition from 2 n to n1

(a) $\frac{16}{15R}$ (b) $\frac{4}{3R}$

(c) $\frac{9}{8R}$ (d) $\frac{36}{5}$

12. Two solenoids are given – Rst has 1 turn per unit length and 2nd has n turns per unit length. Ratio of magnetic fields at their centres is
(a) n : 1 (b) 1 : n
(c) 1 : n2 (d) n2 : 1

13. Which statement is correct for the given circuit?



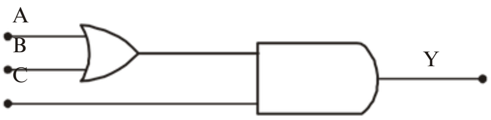
t>h
(a I through R1, rI Iothrough R2h R aRn23d 3 >
) Ithrough R
(b I through R, I is same in
) R1, R2 and R3

14. A (+)vely charged particle is placed near an indfimtely long straight conductor where i
) there is zero gravity. Then
(a the charged particle will not move it
) will move parallel to the straight
(b conductor it will move perpendicular to
) the straight conductor it will move with
((dc)) constant acceleration

15. A metallic bar is heated from 0°C to 100°C. The coeficient of linear expansion is 10–5 K–1. What will be the percentage increase in (lean) g0t.h0?1% (b) 0.1%
(c) 1% (d) 10%

16. If the wavelength is brought down from 6000 Å to 4000 Å in a photoelectric experiment then what will happen?
(a The work function of the metal will increase
) The threshold frequency will decrease
(b No change will take place
) Cut off voltage will increase
(c)
(d
)

17. For what value of A, B and C, the output Y = 1



(a) 0 0 1 (b) 1 0 1
) 1 0 0) 0 1 0

18. L(cet the energy of an e(mditted photoelectron be E) and the wave-length of incident light be . What will be the change in E if is doubled?

(a E (b E /
) 2 E) 2 E

19. A(c solid sphere of(drad/ i4us R carries a)uniform volume ch)arge density . The magnitude of electric field inside the sphere at a distance r from the centre is

(a) r / 3 0 (b) R / 30

(c) R2 / r 0 (d) R3 / r2 0

20. Two point dipoles pk^ and p^are located a 2k t (0, 0, 0) and (1m, 0, 2m) respectively. The resultant electric field due to the two dipoles at the point (1m, 0, 0) is

(a) 9p / 32 0 kk^^ (b) 7p / 32 0 k^

(c) 7p / 32 0 (d) none of these

21. An iron rod of length 2m and cross-sectional area of 50 mm2 stretched by 0.5 mm, when a mass of 250 kg is hung from its lower end. Young's modulus of iron rod is

(a) 19.6 1020 N/m2

N/m2

(b) (c1)9 1.691.60 118010 N/m2 (d) 19.6 1015 N/m2

22. Two resistances equal at 0° C with temperature coefficient of resistance1 and 2 joined in series act as a single resistance in a circuit. The temperature coefficient of their single resistance will be

(a) 1 2 (b) 1 2 / 1 2

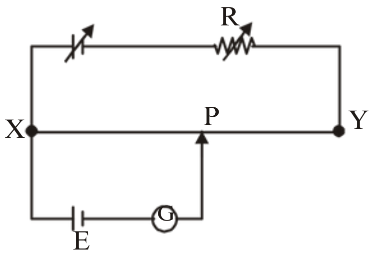
(c) 1 2 / 2 (d) 1 2 / 2

23. The current density varies with radial distance r as J = ar2, in a cylindrical wire of radius R. The current passing through the wire between radial distance R/3 and R/2 is

(a) 65 aR 4 / 2592 (b) 25 aR4 / 72

(c) 65 a2R3 / 2938 (d) 81a2R4 / 144

24. A potentiometer circuit shown in the figure is set up to measure emf of cell E. As the point P moves from X to Y, the galvanometer G shows deflection always in one direction, but the deflection decreases continuously until Y is reached. The balance point between X and Y may be obtained by



(a) decreasing the resistance R and decreasing V
(b) decreasing the resistance R and increasing V
(c) increasing the resistance R and increasing V
(d) increasing the resistance R and decreasing V.

25. A current I flows in the anticlockwise direction through a square loop of side a lying in the xoy plane with its center at the origin. The magnetic induction at the center of the square loop is

(a) $\frac{2\sqrt{2}\ {}_0 I}{a}\hat{e}_x$ (b) $\frac{2\sqrt{2}\ {}_0 I}{a}\hat{e}_z$

(c) $\frac{2\sqrt{2}\ {}_0 I}{a^2}\hat{e}_z$ (d) $\frac{2\sqrt{2}\ {}_0 I}{a^2}\hat{e}_x$

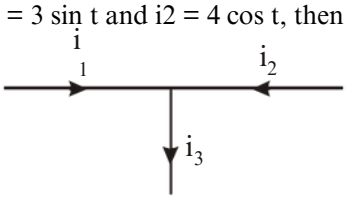
26. A particle of charge q and mass m moves in a circular orbit of radius r with angular speed . The ratio of the magnitude of its magnetic moment to that of its angular momentum depends on (a) (c)
and q (b , q and m
q and m) and m

27. A long straight wir(ed of radius R carries current i. The magne)tic field inside the wire at distance r from its centre is expressed as :

(a) $\frac{\mu 0 i}{R 2} . r$ (b) $\frac{2\mu i_0}{R^2} .r$

(c) $\frac{\mu i_0}{2 R^2} .r$ (d) $\frac{\mu_0 i}{2 R} .r$

28. If i1 = 3 sin t and i2 = 4 cos t, then i 3 is



(a 5 sint + (b 5 sin (t + 37°)
) (553°) t) 5 cos (t + 53°)

29. T(che seiqnu (atio+n 4 o5f°)AC (vdoltage is E = 220 sin
) t+ /6 and the A.C. current is I = 10 sin t
/6. The average power dissipated is

(a)150 W (b)550 W
(c)250 W (d)50 W

30. The current in an L–R circuit builds up to (3/4)th of its steady state value in 4 seconds. The time constant of this circuit is

(a) $\frac{1}{3}$ ln2 sec (b) $\frac{2}{4}$ ln2 sec

(c) ln2 sec (d) ln2 sec

31. The magnetic flux in a closed circuit of resistance 10 varies with time as = (2t –4t2 +1). The current in the loop will change its direction after a time of

(a) 0.25 sec (b) 0.5 sec
(c) 1 sec (d) none

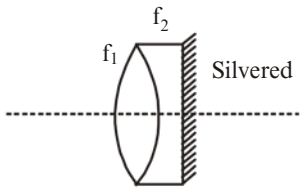
32. A fish looking up through the water sees the outside world contained in a circular horizon. If the refractive index of water is 4/3 and the fish is 12 cm below the surface, the radius of this circle (in cm) is

(a) $36\sqrt{5}$ (b) $4\sqrt{5}$
(c) $36\sqrt{7}$ (d) $36/\sqrt{7}$

33. A metal ball of mass 2 kg moving with a velocity of 36 km/h has a head on collision with a stationary ball of mass 3 kg. If after the collision, the two balls move together, the loss in kinetic energy due to collision is

(a) 140 J (b)100 J
(c) 60 J (d)40 J

34. 1T w=o 1 0le ncmse sa onfd ffo2c =al –length f 20 cm are kept as shown. The resultant power of combination will be



(a –10D (b 5 D
) 0) 10 D

35. W(chen a plastic thin f(idlm of refractive index 1.45 is placed in the path of one of the interfering waves then the central fringe is displaced through width of five fringes. The thickness of th6e.5 4fi4l m×, 10(f–14) 1e6la5n4g4t h× o10f –l4i gmht is 58906Å.5, 4w ×ill 1b0e–4 cm(d)6.5 × 10–4 cm

36. A(an) unpolarised beam of intensity I0 is incident o(cn) a pair of nicols making an angle of 60° with each other. The intensity of light emerging from the pair is

(a) I0 (b) I0/2
(c) I0/4 (d) I0/8

37. The half life of radioactive Radon is 3.8 days. The time at the end of whic $\frac{1}{2h0}$ th of the radon sample will remain undecayed is (given log10 e 0.4343)

(a) 3.8 days (b) 16.5 days
(c) 33 days (d) 76 days.

38. If the nuclear radius of 27Al is 3.6 Fermi, the approximate nuclear radius of 64Cu in Fermi is

(a) 4.8 (b) 3.6
(c) 2.4 (d) 1.2

39. A hydrogen atom is in an excited state of principal quantum number (n), it emits a photon of wavelength (), when it returns to the ground state. The value of n is

(a) $\sqrt{\frac{R}{R-1}}$ (b) $\sqrt{\frac{(R1)}{R}}$

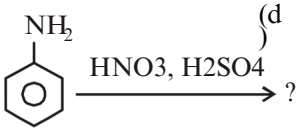
(c) $\sqrt{(R\ 1)}$ (d) $\sqrt{\frac{R}{R\ 1}}$

40. A marble block of mass 2 kg lying on ice when given a velocity of 6 m/s is stopped by friction in 10 s. Then the coefficient of friction is (Take g = 10 ms–2)

(a) 0.06 (b) 0.03
(c) 0.04 (d) 0.01

PART - II (CHEMISTRY)

41. IUPAC name of valeric acid is
(a) Propanoic acid (b) Butanoic acid
(c) Ethanoic acid (d) Pentanoic acid

42. 

The product P for the above given reaction will be
(a) m-nitroaniline
(b) p-nitroaniline
(c) nitroaniline both o &
(d) p nitroaniline

43. Coordination number of Co in [Co(NH3)6]Cl3
(a) + 2 (b) + 3
(c) + 5 (d) + 8

44. Which of the following complex will show fac & mer isomerism?

(a) Co(NH3)3(NO2)3

(b) CoCl2 (en)2

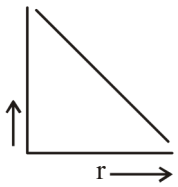
(c) (Co(NH3)Cl(en)$_2^2$

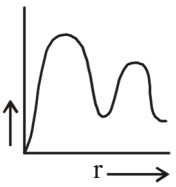
(d) Co(NH3)2 Cl2(en)

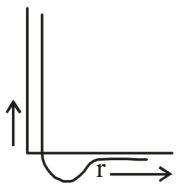
45. Which of these undergo polymerisation?
(a) CH3OH (b) C2H5OH
(c) $\begin{matrix} O \\ \| \\ CH3 \\ | \\ CH3 \end{matrix}$ (d) CH3CHO

46. Which of the following graph represents variation of 2p-orbital wave function with distance from the nucleus?

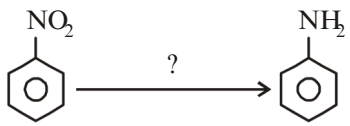
(a) 

(b) 

(c) 

(d) 

47. Name the catalyst used to bring down the r ea ct ion



(a) Sn/HCl (b) CuCl/HCl
(c) Cu2Cl2/HCl (d) Zn-Hg/HCl

48. The correct set of quantum numbers for Rb (atomic no. 37) is

(a) 5, 0, 0,12 (b) 5,1,0,12

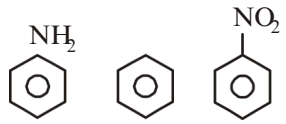
(c) 6, 0,1, $\frac{1}{2}$ (d) 5,1,1, $\frac{1}{2}$

49. XeF4 disproportionate in water to give
(a)Xe + HF (b)Xe and XeO3
(c) XeOF4 and HF (d)XeO2Fe and HF

50. An ionic compound has a unit cell consisting of A ions at the corners of a cube and B ions on the centres of the faces of the cube. The empirical formula for this compound would be

(a) A3B (b) AB3
(c) A2B (d) AB

51. Among the following the incorrect s(ata)tement is Density of crystals remains unaffected due to Frenkel defect.
(b)In BCC unit cell the void space is 32%.
(c) Density of crystals decreases due to Schottky defect. Electrical conductivity
(d)of semiconductors and metals increases with increase in tempera tur e.

52. 

(A) (B) (C)
The correct order of electrophilic substitution for the compounds given above will be
(a A > B > C B > C (b C > B > A B > A > C

53. F(cor m> eAsotartaric acid, (tdhe correct configuration f)or chiral carbon is)
(a) 2R, 3S (b)2R, 3R
(c) 2S, 3R (d)1D, 2L

54. Which of the two acids form anhydrides?
(I) Oxalic acid (II)Succinic acid
(III)Benzoic acid (IV)Phthalic acid
(a) I & III (b)II & IV
(c) II & III (d)III & IV

55. By which reaction ketal is formed?
(a)Glycol with acetone
(b)Hydration of glycol
(c) Condensation of glycol
(d)Glycol with acetaldehyde

56. Which one of the following show ster eoi somer i sm ?
(a) 2-Butene
(b)3-Methyl but-1-ene
(c)2-Methyl butene
(d) Butanol

57. Acetophenone and Benzophenone can be distinguished by which of the following test
(a)Knoeveangel reaction
(b) Canizzaro's reaction
(c) Aldol condensation
(d)HVZ Reaction

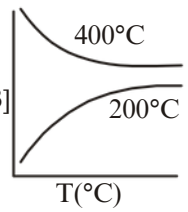
58. R NC LiAlH4 P
The product P in this reaction is
(a)R – NH 2 (b(R – N – CH3 H
(c) R – CH3)d R – N – (CH3)2

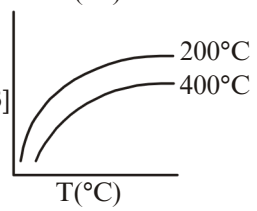
59. The protein present in the hair is
(a) Lysine (b) Myosine
(c) Keratin (d) Alanine

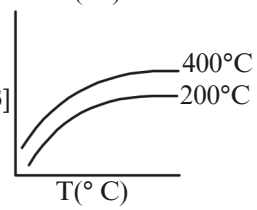
60. One mole of an ideal gas at 300 K is expanded isothermally from an initial volume of 1 litre to 10 litres. Then S (cal deg–1 mol–1) for this process is : (R = 2 cal K–1 mol–1)
(a) 7.12 (b) 8.314
(c) 4.6 (d) 3.95

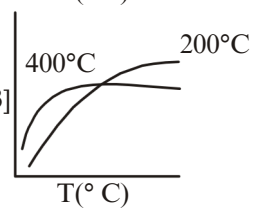
61. For a reaction A aBc;t Hiv a=ti o2n0 keJn merogyl– 1o tfh tehe The forward reaction is 85 kJ/mol. activation energy of the backward reaction will be
(a) (1c0) 5 IkfJ /mthoel (b 65 react4io5n k NJ/mol) kJ/mol

62. 2 + 3H2 = 2NH3 occur(sd at 72500°C and 1000 atm then th)e grkaJp/hm oshlowing the correct equilibrium yield at 400°C is

(a) 

(b) 

(c) 

(d) 

63. Group 15 elements have more electron gain enthalpy than group 16-elements. The correct reason for this is

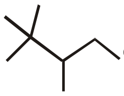
(a) Half -filled stability of gp. 15 elements. Poor shielding in gp. 15
(b) Poor shielding in gp. 16 Half -filled stability of gp. 16 elements
(c)
(d)

64. t-butyl CH CH C OH can't give
‖
O

decarboxylation while normally -unsaturated acid give this reaction because

(a) t-butyl gp. has large size and does not let the COOH group to leave.
(b) t-butyl gp. can't extract H from COOH.
(c) t-butyl gp. stabilise carbanion formed.
(d) t-butyl gp. does not allow this composition to convert to --unsaturated acid

65. Which type of carbocation is/are formed when

 OH is treated with an acid?

(a) 1° (b) 2°
(c) 3° (d) All the three

66. For hydrogen-oxygen fuel cell, the cell reaction is

2H2(g) O2(g) 2H2 O( )

If G(fH2O) = – 237.2 kJ mol–1, then emf of this cell is

(a) + 2.46 V (b) – 2.46 V
(c) + 1.23 V (d) – 1.23 V

67. At 298 K, the conductivity of a saturated solution of AgCl in water is 2.6 × 10–6 S cm–1. Its solubility product at 298 K.

Given : (Ag) 63.0 S cm2 mol1, (Cl) 67.0 S cm2 mol1

(a) 2.0 × 10–5 M2 (b) 4.0 × 10–10 M2
(c) 4.0 × 10–16 M2 (d) 2 × 10–8 M 2

68. aSntadn d5a0r Jd Ken–t1ro mpyo lo–2f,1 XY, r2e spnecdtiv Yel3y .a Freo 6r0 t,h 4e0 reactio

1/2 X2 3/2 Y2 XY3, H –30kJ, to be at equilibrium, the temperature will be

5(a0)0 K (b) 1250 K
1(c0)007 K (d) 50 K

69. The enthalpy change for a given reaction at 298 K is – x J mol–1. For the reaction to be spontaneous at 298 K, the entropy change at that temperature

(a) can be negative, but numerically greater than x/298 Jk1
(b) can be negative, but numerically smaller than x/298 Jk1.
(c) can not be negative
(d) can not be positive

70. a moles of PCl5 is heated in a closed container to equilibriate PCl5(g) ⇌ PCl3(g) + Cl2(g) at a pressure of P atm. If x moles of PCl5 dissociate at equilibrium, then

(a) x/a = Kp/(K P) (b) x/a = (Kp/(Kp P))^1/2
(c) x/a = (Kp/P)^1/2 (d) x/a = (Kp/(Kp p))^1/2

71. A plot of lnK against 1/T (abscissa) is expected to be a straight line with intercept on ordinate axis equal to

(a) S/2.303R (b) S/R
(c) S/R (d) R S

72. In a reaction A Products, when start is made from 8.0 × 10–2 M of A, half-life is found to be 120 minute. For the initial concentration 4.0 × 10–2 M, the half-life of the reaction becomes 240 minute. The order of the reaction is :

(a) zero (b) one
(c) two (d) 0.5

73. A reaction : A2 + B Products, involves the following mechanism :
(i) A2 ⇌ 2A (fast) (A being the intermediate)
A B k2 Products (slow). The rate law consistent to this mechanism is :

(a) rate = k[A2][B] (b) rate = k[A2]2 [B]
(c) rate = k[A2][½B] (d) rate = k[A2][B]2

74. The following data were obtained for a given reaction at 300 K.

Reaction	Energy of activation (kJ mol–1)
(i) uncatalysed	76
(ii) catalysed	57

The factor by which rate of catalysed reaction is increased, is

(a) 21 (b) 210

(c) 2000 (d) 0

75. The wave number of the first emission line in the Balmer series of H-Spectrum is :

(R = Rydberg constant) :

(a) $\frac{5}{36}R$ (b) $\frac{9}{400}R$

(c) $\frac{7}{6R}$ (d) $\frac{3}{4R}$

76. Which one of the following reactions of xenon compounds is not feasible?

(a) $3XeF_4 + 6H_2O \rightarrow 2Xe + XeO_3 + 12HF + 1.5O_2$

(b) $2XeF_2 + 2H_2O \rightarrow 2Xe + 4HF + O_2$

(c) $XeF_6 + RbF \rightarrow Rb[XeF_7]$

(d) $XeO_3 + 6HF \rightarrow XeF_6 + 3H_2O$

77. (Adn) isole is treated with HI under two different conditions.

$$C \quad D \xrightarrow{HI(g)} C_6H_5OCH_3 \xrightarrow{\text{conc. HI}} A \quad B$$

The nature of A to D will be

(a) A and B are C3HI and C6H5OH, while C and D are CH3OH and C6H5I

(b) A and B are C3HOH and C6H5I, while C and D are CH3I and C6H5OH

(c) Both A and B as well as both C and D are CH3I and C6H5OH

(d) A and B are C3HI and C6H5OH, while there is no reaction in the second case.

78. Phenol undergoes electrophilic substitution more easily than benzene because

(a) –OH group exhibits +M effect and hence increases the electron density on the o- and p- positions.

(b) oxocation is more stable than the carbocation

(c) both (a) and (b)

(d) –OH group exhibits acidic character

79. Which of the following name reaction is not used for introducing a – COOH group?

(a) Cannizzaro reaction

(b) Benzilic acid rearrangement

(c) Baeyer – Villiger oxidation

(d) Iodoform reaction

E(cs)terification of acid chloride with ethanol (isd usually carried out in the presence of p)yridine. The function of pyridine is

(a) to remove HCl formed in the reaction

(b) to react with acid chloride to form an acylpyridinium ion

(c) both (a) and (b)

(d) as a catalyst

PART - III (MATHEMATICS)

81. The solution of the differential equation

$$(1 + y^2) + (x - e^{\tan^{-1} y})\frac{dy}{dx} = 0$$

(a) $(x - 2) = ke^{\tan^{-1} y}$

(b) $2xe^{\tan^{-1} y} = e^{2\tan^{-1} y} + k$

(c) $x e^{\tan^{-1} y} = \frac{1}{2} e^{2\tan^{-1} y} + k$

(d) $y = \tan(e^{\tan^{-1} y} + k)$

82. A tetrahedron has vertices at O (0, 0, 0), A (1, 2, 1) B (2, 1, 3) and C (–1, 1, 2). Then the angle between the faces OAB and ABC will be

(a) $\cos^{-1}\frac{17}{31}$ (b) 120°

(c) 30° (d) 90°

83. The foci of the ellipse $\frac{x^2}{16} + \frac{y^2}{b^2} = 1$ and the hyperbola $\frac{x^2}{144} - \frac{y^2}{81} = \frac{1}{25}$ coincide then value of b2 is

(a) 1 (b) 5

(c) 7 (d) 9

84. If the tangent to the function y = f(x) at (3,4) makes an angle of $\frac{3}{4}$ with the positive direction of x-axis in anticlockwise direction then f'(3) is

(a) –1 (b) 1

(c) $\frac{1}{\sqrt{3}}$ (d) $\sqrt{3}$

85. The probability of India winning a test match against Australia is $\frac{1}{2}$ assuming independence from match to match. The probability that in a match series India's second win occurs at third test match is

(a) $\frac{1}{8}$ (b) $\frac{1}{4}$ (c) $\frac{1}{2}$ (d) $\frac{3}{2}$

86. If $|a| = 3, |b| = 2, |c| = 1$ then the value of $|a.b + b.c + c.a|$ is (given that $a + b + c = 0$)

(a) –7 (b) 7

(c) 14 (d) –14

87. If $f(x) = x^2, g(x) = 2x, 0 \le x \le 2$ then the value of $I(x) = \int_0^2 \max f(x), g(x)$ is

(a) $\frac{10}{3}$ (b) $\frac{1}{3}$ (c) $\frac{11}{3}$ (d) 32

88. If A and B are matrices and $B = ABA^{-1}$ then the value of $(A + B)(A - B)$ is

(a) $A^2 + B^2$ (b) $A^2 - B^2$

(c) $A + B$ (d) $A - B$

89. The value of $(1 + \omega - \omega^2)^7$ is

(a) $128\omega^2$ (b) $-128\omega^2$

(c) 128ω (d) -128ω

90. The moment about the point $\hat{i} + 2\hat{j} + 3\hat{k}$ of a force represented by $\hat{i} + \hat{j} + \hat{k}$ acting through the point $2i + 3j + k$ is

(a) $3\hat{i} - 3\hat{j}$ (b) $3\hat{i} + \hat{j}$

(c) $\hat{i} + \hat{j}$ (d) $3\hat{i} - 3\hat{j}$

91. If g (x) is a polynomial satisfying
$g(x) g(y) = g(x) + g(y) + g(xy) - 2$
for all real x and y and g (2) = 5 then $\lim_{x \to 1} g(x)$ is

(a) 9 (b) 10

(c) 25 (d) 20

92. The equation of one of the common tangents to the parabola $y^2 = 8x$ and $x^2 + y^2 - 12x + 4 = 0$ is

(a)

(c) $y \equiv -x + 2$ (b) $y = x - 2$

(d)None of these

93. If $e^x - y = \sqrt{1 - y^2}$, then the value of y is

(a) $\frac{1}{2}(e^x - e^{-x})$ (b) $\frac{1}{2}(e^x + e^{-x})$

(c) $e^x - e^{2x}$ (d) $e^x + e^{2x}$

94. What is the area of a loop of the curve $r = a\sin 3\theta$?

(a) $\frac{a^2}{6}$ (b) $\frac{a^2}{8}$

(c) $\frac{a^2}{12}$ (d) $\frac{a^2}{24}$

95. Convert the hexadecimal numeral ABCD into binary numeral

(a) (1010101111001101)

(b) (1001000011111121)

(c) (1111110000010001)

(d) (1000100100111101)

96. The line $y = mx + c$ is a normal to the parabola $y^2 = 4ax$, cuts the parabola again at the point whose parameter is

(a) $-t_2 - t_1 - \frac{2}{t_1}$ (b) $-t_2 - t_1 - \frac{2}{t_1}$

(c) $-t_2 - t_1 - \frac{2}{t_1}$ (d)None of these

97. The distance moved by the particle in time t is given by $s = t^3 - 12t^2 + 6t + 8$. At the instant, when its acceleration is zero the velocity is :

(a) 42 (b) –42

(c) 48 (d) –48

98. The logical expression X, in its simplest form for the truth table

a	b	X
1	0	0
1	1	1
0	1	0
0	0	0

is

(a) X = a . b (b) X = a + b

(c) X = a'.b (d) X = a.b'

99. The value of $\cos\frac{\pi}{8}\cos\frac{3\pi}{8}$ is equal to

(a) –1/4 (b)3/4

(c) – 3/4 (d) 1/16

100. Consider the objective function Z = 40x + 50y. The minimum number of constraints that are required to maximize Z are

(a) 4 (b) 2

(c) 3 (d) 1

101.In a culture the bacteria count is 1,00,000. The number is increased by 10% in 2 hours. In how many hours will the count reach 2,00,000 if the rate of growth of bacteria is proportional to the number present.

(a) $\frac{2}{\log 11 \quad 10}$ (b) $\frac{2 \log 2}{\log 11}$

(c) $\frac{\log 2}{\log 11}$ (d) $\frac{\log 2}{\log 111 \quad 0}$

102.The value of $\sin^{-1}\frac{1}{\sqrt{5}}$ cot1(3)is

(a) 6 (b) 4

(c) 3 (d) 2

103.If a = cos 2 + i sin 2, b = cos 2 + i sin 2, c = cos 2 + i sin 2and d = cos 2 + i sin 2 , then

$\sqrt{abcd}\ \frac{1}{\sqrt{abcd}} =$

(a) $\sqrt{2}\cos(\quad + + +)$
(b) $2\cos(+ + +)$
(c) $\cos(+ + + \quad)$
(d)None of these

104.If the mean of a binomial distribution is 25, then its standard deviation lies in the interval

(a) [0, 5) (b) (0, 5]
(c) [0, 25) (d) (0,25]

105.Number of ways of selecting three squares on a chessboard so that all the three be on a diagonal line of the board or parallel to it is

(a) 196 (b) 126
(c) 252 (d) 392

106.If A and B are two matrices such than rank of A11 =3.If f(x) = (1 + x)2/x for x0 and f(0) = e2 is m and rank of B = n, then
r(a)nk (AB) = mn
(b)rank (AB) rank (A)
(c) rank (AB) rank (B)
(d)rank (AB) min (rank A, rank B)

107.A variable plane remains at constant distance p114.If y = 2x/In xthen $\frac{dy}{dx}$ at x = e is from the origin.If it meets coordinate axes at points A, B, C then the locus of the centroid of ABC is

(a) $x2 \quad y2 \quad z2 \quad 9p2$
(b) $\frac{}{3}$
(c) x y3 z3 9p3
(d) x2y2 z2 9p2
x3 y3 z3 9p3

108.While shuffling a pack of 52 playing cards, 2 are accidentally dropped. The probability that the missing cards to be of different colours is

(a) $\frac{29}{52}$ (b) $\frac{1}{2}$ (c) $\frac{26}{51}$ (d) $\frac{27}{51}$

109.Which of the following is INCORRECT for the hyperbola x2 2y2 2x 8y 1 0

(a) Its eccentricity is $\sqrt{2}$
(b) Length of the transverse axis is $2\sqrt{3}$
(c) Length of the conjugate axis is $2\sqrt{6}$
(d)Latus rectum is $4\sqrt{3}$

110.A box contains 20 identical balls of which 10 are blue and 10 are green. The balls are drawn at random from the box one at a time with replacement. The probability that a blue ball is drawn 4th time on the 7th draw is

(a) $\frac{27}{32}$ (b) $\frac{5}{64}$ (c) $\frac{5}{32}$ (d) $\frac{1}{2}$

111.The number of common tangents to the circles x2 + y2 – 6x – 14y + 48 = 0 and x2 + y2 – 6x = 0 is

(a) 1 (b) 2
(c) 0 (d) 4

112.The solution of the equation cos2 + sin + 1 = 0, lies in the interval

(a) $\frac{}{4}, \frac{}{4}$ (b) $\frac{}{4}, \frac{3}{4}$

(c) $\frac{3}{4}, \frac{5}{4}$ (d) $\frac{5}{4}, \frac{7}{4}$

113.If f(x) = (1 + x)2/x for x0 and f(0) = e2 is
(a)left continuous only at x = 0
(b)right continuous only at x = 0
(c) continuous at x = 0
(d)discontinuous at x = 0

114.If y = 2x/In xthen $\frac{dy}{dx}$ at x = e is

(ae) (b)2e log 2
(clo)g 2 (d)0

115. $\int \frac{1}{x^2(x^4+1)^{3/4}}\,dx$ is equal to

(a) $-(1+\frac{1}{x^4})^{1/4}+C$ (b) $(x^4+1)^{1/4}+C$

(c) $-(1+\frac{1}{x^4})^{1/4}+C$ (d) $(1+\frac{1}{x^4})^{1/4}+C$

116. If the letters of the word KRISNA are arranged in all possible ways and these words are written out as in a dictionary, then the rank of the word KRISNA is

(a) 324 (b) 341

(c) 359 (d) None of these

117. The shortest distance between the lines $x = y + 2 = 6z - 6$ and $x + 1 = 2y = -12z$ is

(a) $\frac{1}{2}$ (b) 2

(c) 1 (d) $\frac{3}{2}$

118. The domain and range of the function f given by $f(x) = 2 - |x - 5|$ is

(a) Domain = R+, Range = (–, 1]

(b) Domain = R, Range = (–, 2]

(c) Domain = R, Range = (–, 2)

(d) Domain = R+, Range = (–, 2]

119. The number of surjective functions from A to B where A = {1, 2, 3, 4} and B = {a, b} is

(a) 14 (b) 12

(c) 2 (d) 15

120. If $f(a+b-x) = f(x)$, then $\int_a^b xf(x)dx$ is equal to

(a) $\frac{a+b}{2}\int_a^b f(b-x)dx$

(b) $\frac{a+b}{2}\int_a^b f(b+x)dx$

(c) $\frac{b-a}{2}\int_a^b f(x)dx$

(d) $\frac{a+b}{2}\int_a^b f(x)dx$

PART - IV (ENGLISH)

Direction (Qs. 121-123) Read the passage carefully and anser the questions given below.

Laws of nature are not commands but statements of acts. The use of the word "law" in this context is rather unfortunate. It would be better to speak of uniformities in nature. This would do away with the elementary fallacy that a law implies a law giver. If a piece of matter does not obey a law of nature it is punished. On the contrary, we say that the law has been incorrectly started.

121. If a piece of matter violates nature's law, it is punished because

(a) it is not binding to obey it

(b) there is no superior being to enforce the law of nature

(c) it cannot be punished

(d) it simply means that the facts have not been correctly stated by law

122. Laws of nature differ from man-made laws because

(a) the former state facts of Nature

(b) they must be obeyed

(c) they are natural

(d) unlike human laws, they are systematic

123. T(hce) laws of nature based on observation are

(da) conclusion about the nature of the universe.

(b) true and unfalsifiable.

(c) figments of the observer imagination.

(d) subject to change in the light of new facts.

124. Direction: This question presents a sentence, part of which or all of which is underlined. Beneath the sentence you will find four ways of phrasing the underlined part. The first of these repeats the original; the other three are different. If you think the original is best, choose the first answer; otherwise choose one of the others.

The administration discussed whether the number of students studying European languages was likely to decline when the senior lecturer retired.

(a) whether the number of students studying European languages was likely

(b) whether the number of students studying European languages were likely

(c) if the students studying European languages were likely

(d) if the number of European language students were likely

125. Choose the best pronunciation of the word, Restaurant, from the following options.

(a) res-tu-rant (b) res-tuh-rawnt

(c) rest-rant (d) resto-raunt

SOLUTIONS

PART - I (PHYSICS)

1. (d)When work is done upon a system by a conservative force then its potential energy increases. de-Broglie
2. (a) wavelength is given by

$= \frac{h}{p}$,where h = Planck's constant and

p = momentum

Also, energy (E) and momentum are related as:

$E = \frac{p^2}{2m}$

$p = \sqrt{2mE}$

$\frac{h}{\sqrt{2mE}} = \frac{1}{\sqrt{E}}$ as h and m are constants

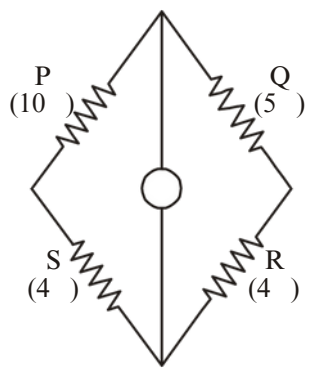
Hence, $\frac{\lambda'}{\lambda} = \sqrt{\frac{E}{E'}} = \sqrt{\frac{2E}{E}} = \sqrt{2}$

$\frac{9}{\sqrt{2}}$.

3. (a)For no current through the galvanometer, the wheatstone bridge should be balanced. For this, we must have

$\frac{S}{R} = \frac{P}{Q}$

This condition is satisfied with only option (a).



When a 5 resistor is connected in series with Q, the equivalent resistance in the P-arm becomes 10.

$\frac{P}{Q} = \frac{10}{10} = 1$

and $\frac{S}{R} = \frac{4}{4} = 1$

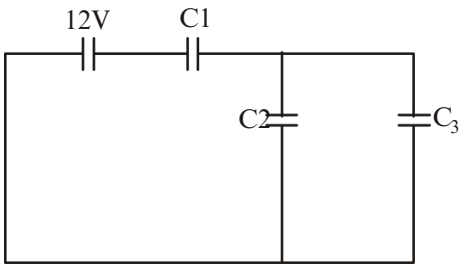
$\frac{P}{Q} = \frac{S}{R}$.

(a)When a dielectric slab of dielectric constant $K = \frac{3}{2}$ is inserted between the plates of ,C its new capacitance C_2 becomes

$C_2 = \frac{3}{2}C$

Equivalent capacitance of C_2 and C3 is

$C_{eq} = C2 + C3 = \frac{3}{2}C + C = \frac{5C}{2}$



Now, Ceq and C1 are in series. Therefore, their equivalent capacitance is

$C_{eq} = \frac{C_{eq} C_1}{C_{eq} + C_1} = \frac{\frac{5C}{2} C}{\frac{5C}{2} + C}$

$\frac{5C^2}{7C} = \frac{5C}{7}$.

5. (c) Terminal velocity,

$$v_T = \frac{2}{9}\frac{r^2(d - d_2)g}{\eta}$$

$$v_T = \frac{(1.50).5}{0.2} \quad v_{T2} \quad 0.2\ 918$$

$$0.2 \quad (19.5\ 1.5)$$

$$v_{T2}\ 0.1 \text{m/s}$$

6. (b)Mganetic field at the centre of the circular loop increases as it moves towards the current carrying wire as we know it varies inversely with the distance. Therefore, induced current in the loop should be such that it can reduce the increased magnetic field. This is possible only when the induced current is clockwise.

7. (b) $|e| = \frac{LdI}{}$

Here, e = 20 mV = $20 \times 1\ 0^{-3}$V

$$\frac{dI}{dt} = \frac{6\ 2}{2} \quad 2\ A/s$$

L = ?

$$20\ 103 \quad L\ 2$$

$$L\ 1010^{3}\ H = 10\ mH.$$

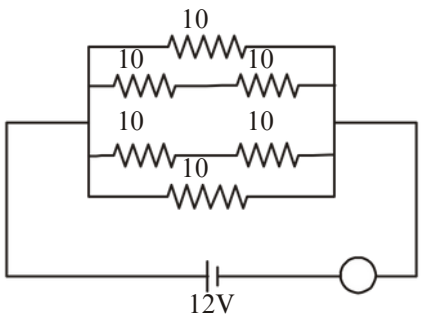
8. (a)1F,o arr tehae o tfi mloeo pt <ch tanges. Hence, magnetic flux linked with it changes during this time and emf is induced thereby.

9. (c Hologram is based on the phenomenon of in ter fer en ce.

10.) An equivalent of the given network is as shown in the figure.

(a If Rp be the net resistance, then

)



$$\frac{1}{R_p} = \frac{1}{10} + \frac{1}{10} + \frac{1}{10} + \frac{1}{10} + \frac{1}{10} + \frac{1}{10}$$

$$\frac{1}{10} + \frac{1}{20} + \frac{1}{20} + \frac{1}{10}$$

$$\frac{6}{20} \quad \frac{3}{10}$$

$$R_p = \frac{10}{3}$$

Hence, current flowing through ammeter is

$$I = \frac{V}{R_p} = \frac{12}{\frac{10}{3}} = 3.6\ A.$$

11. (c) Energy released in transition from state n2 to n1 is equal to the energy absorbed in transistion from state 2n to n1.

12. (b)Magnetic field no. of turns per unit length

Required ratio = 1 : n.

13. (d)R1, R2 and R3 are in series. Therefore, same current will flow through all the

14. (a) resistors. As the charged particle is at rest, no force will act on it due to the magnetic field produced by the conductor at the site of the charge. Hence, it will remain at rest.

15. (b) $T = 10\ 5 \quad 100 \quad 10\ 3$

$$100\% \quad 10^{3} \quad 100$$

$$101 \quad 0.1\%$$

16. (d)When wavelength decreases, frequency increases. Also, we know that cut-off voltage (or stopping potential) increases when frequency increases.
Hence, option (d) is correct. Note that work function and threshold frequency are constant for a given metal.

17. (b) Clearly,

Y = (A + B) . C = (A.C) + (B.C) For A = 0, B = 0 & C = 1, A = 1, B = 0 &Y C = (10,.1) + (0.1) A = 1, B = 0 & C == 0 , 0A Y= = (1.1) + (0.B) = 1 & C = 0) + (0.0) = 0 Y =

So, option (b) is corr(e0c.t0.) + (1.0) = 0

18. (b)We have

h = Wo + E, where E is the energy of emitted ph otoelectr on

$$hc \quad W_o \quad E$$

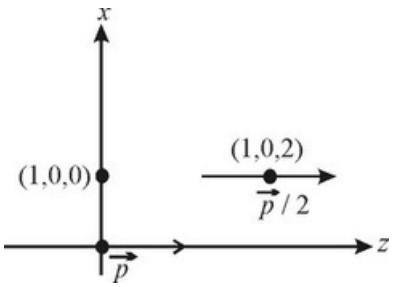
As hc and Wo are constant,

$$E \quad \frac{1}{}$$

Therefore, as is doubled, E will become half.

19. (a) $E \quad \frac{1}{4 \quad _0} \frac{qr}{R^3} = \frac{q}{4 \quad R^3} \frac{r}{3} = \frac{r}{3 \quad _0} \quad 0$

20. (b) The given point is on axis of dipole and at equatorial line of p dipole so that field at given point is $(E_1 \quad E2)$



$$E1 \quad \frac{2K(p/2)}{23} \quad \frac{Kp}{8}(\hat{k})$$

$$E_2 \quad \frac{Kp}{1}(\hat{k})$$

$$E1 \quad E^2 \quad \frac{7}{8}Kp(\hat{k}) = \frac{7p}{32 \quad _0}\hat{k}$$

21. (c) $Y \quad \frac{F/A}{/} \quad \frac{250 \ 10 \ 6}{0.5 \ 10 \ 3} \quad 2$

$$\frac{250 \ 9.8}{50 \ 10 \ 6} \quad \frac{2}{0.5 \ 10^{3}} \quad 19.6 \ 1010 \ N/m2$$

22. (d)R1 = R0(1 + 1t) + R0(1 + 2t)

$$= 2R_0 \ 1 \quad \frac{1}{2} \quad ^2 t$$

Comparing with R =0 R(1+ t)

$$\frac{1}{2} \quad 2$$

23. (a) Given $J = ar.\hat{z}$

$$i = \int_1^2 J \ 2 \ rdr \quad \int_2^{R/} ar2 \ 2 \ rdr$$

$$= 2a \int_{R3/}^{R2/} rd3r \quad \frac{R/}{2} \left| \frac{ra^{4R/2}}{4} \right|_{R/3}$$

$$= \frac{a}{2} \quad \frac{R}{2} \quad \frac{4}{3} \quad \frac{R}{} \quad \frac{4}{}$$

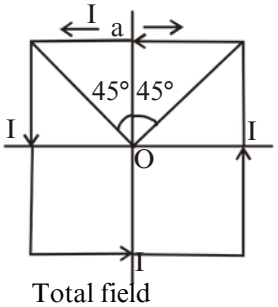
$$= \frac{aR^4}{2} \quad \frac{65}{81} \quad \frac{65}{16} \quad \frac{aR^4}{2592}$$

24. (b)Decreasing R increases current in XY and there by increases the potential drop across XP and the balance point may be obtained. The current may be increased also by increasing V.

25. (b)Field due to one side of loop at O

$$= \frac{_0 I}{4} \quad \frac{a}{2} \quad (2\sin 45)$$

Field atO due to all four sides is along unit vector $e\hat{z}$



Total field

$$= 4. \quad \frac{_0 I}{4} \quad \frac{a}{2} \quad (2\sin 45) \quad \frac{2\sqrt{2} \ 0I}{a}$$

26. (c) The angular momentum L of the particle is given by
L = mr2 where = 2n.

Frequency n = $\frac{}{2}$;

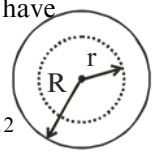
Further i = q × n = $\frac{q}{M}$

Magnetic moment, = iA= $\frac{q}{2}$ r2;

$$M = \frac{qr^2}{2}$$

So, $\frac{M}{L} = \frac{qr^2}{2mr^2} = \frac{q}{2m}$

27. (c) Using Ampere's law, we have



$$B.d = \mu_0 i_{in}$$

or $B \times 2r = \mu_0 \frac{i}{R^2} r^2$

$$B = \frac{\mu_0}{2} \cdot \frac{ir}{R^2}$$

28. (a) From Kirchhoff's current law,

$i_3 = i_1 + i_2 = 3\sin t + 4\sin(t + 90)$

$= \sqrt{3^2 + 4^2 + 2(3)(4)\cos 90 \sin(\quad t \quad)}$

where $\tan = \frac{4\sin 90}{3 + 4\cos 90} = \frac{4}{3}$

$i_3 = 5 \sin (t + 53°)$

29. (b) We know that, $Z = \frac{E_0}{I_0}$

Given, E0 = 220V and I0 = 10 A

so $Z = \frac{220}{10} = 22$ ohm

$=$

$6 \quad 6 \quad 3$

$p_a \quad \frac{E_0}{\sqrt{2}} \quad \frac{I_0}{\sqrt{2}} \cos$

$= \frac{220}{\sqrt{2}} \quad \frac{10}{\sqrt{2}} \quad \cos\frac{}{3} = 550$ W

30. (b) $I \quad I_0(1 - e^{t/})$

where, time constant

$\frac{3}{4}$

$3I0 \quad I0(1 - e^{t/})$

4

$1 - e^{t/} \quad e^{t/} \quad \frac{1}{4}$

$t \ln e \quad \ln\frac{1}{4} \quad 4 \quad 2\ln 2$

2

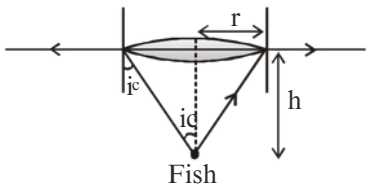
$\ln 2$

31. (a) $e = \frac{d}{dt} [\ 2 \quad 8t \quad 0]$

$8 t = 2 \quad t = \frac{1}{4}$ sec = 0.25 sec

32. (d) $\sin i_c \quad \frac{1}{} \quad \frac{r}{\sqrt{r2 \quad h2}}$

Using h = 12 cm, μ = 4/3



We get $r = \frac{36}{\sqrt{}}$ cm.

33. (c) Apply conservation of momentum,
m1v1 = (m1 + m2)v

$v = \frac{m1v1}{(m1 \ m2)}$

Here v1 = 36 km/hr = 10 m/s,
m1 = 2 kg, m2 = 3 kg

$v \quad \frac{10 \quad 2}{5} \quad 4 \text{ m/s}$

K.E. (initial) $= \frac{1}{2} \quad 2 \quad (10)2 \quad 100$J

K.E(Final)2)(4)2(.3 = $\frac{1}{2}$ 40J

Loss in K.E. = 100 – 40 = 60 J
Alternatively use the formula

$$E_k \quad \frac{1}{2}\frac{m1m2}{m_1 \quad m2} \quad u_1 \quad u_2 \quad ^2$$

34. (d) $P = \frac{2\ 10010\ 100}{20} \quad 0$

P= 10 dioptre.

35. (a) $X0 \quad (\quad 1)t \quad 5 \quad \frac{(0.45)t}{5890 \quad 10^{10}}$

$t = \frac{5 \times 5890 \times 10^{-10}}{0.45} = 6.544 \times 10^{-4}$ cm

36. (c) According to Malus' law

$I = I_0 \cos^2\theta = I_0 (\cos 60°)^2$

$= I_0 \times \left(\frac{1}{2}\right)^2 = \frac{I_0}{4}$

37. (b) $t_{1/2} = 3.8$ day

$\frac{0.693}{t_{1/2}} = \frac{0.693}{3.8} = 0.182$

If the initial number of atom is $a = A_0$ then after time t the number of atoms is $a/20 = A$. We have to find t.

$t = \frac{2.303}{} \log \frac{A_0}{A} = \frac{2.303}{0.182} \log \frac{a}{a/20}$

$= \frac{2.303}{0.182} \log 20 = 16.46$ days

38. (a) Nuclear radius, $r \propto A^{1/3}$ where A is mass number

$\frac{r_{Cu}}{r_{Al}} = \left(\frac{A_{Cu}}{A_{Al}}\right)^{1/3} = \left(\frac{64}{27}\right)^{1/3} = \frac{4}{3}$

$r_{Cu} = 3.6 \times \frac{4}{3} = 4.8$ Fermi

39. (d) As $\frac{1}{} = R\left(\frac{1}{n_1^2} - \frac{1}{n_2^2}\right)$

$\frac{1}{} = R\left(\frac{1}{1^2} - \frac{1}{n^2}\right)$

Multiply both sides by

$1 = R\left(1 - \frac{1}{n^2}\right)$ or $\frac{1}{R} = 1 - \frac{1}{n^2}$

or $\frac{1}{n^2} = 1 - \frac{1}{R} = \frac{R - 1}{R}$

or $n = \sqrt{\frac{R}{R - 1}}$

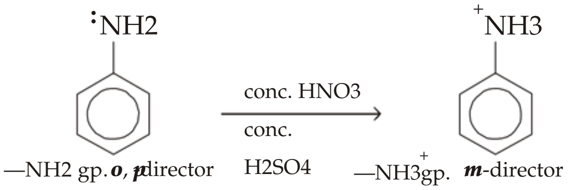
40. (a) $a = \frac{g}{10^6}$ [using v = u + at]

$\frac{6}{10} g \quad \frac{6}{10 \quad 10} = 0.06$

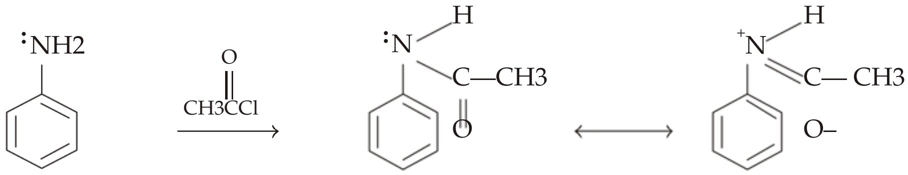
PART - II (CHEMISTRY)

41. (d) The common name of Pentanoic acid is valeric acid.

42. (d) Nitric acid not only nitrates, but also oxidizes the highly reactive ring as well, with loss of much material as dark-coloured tar. Furthermore, in the strongly acidic nitration medium, the amino group is converted to the —NH_3^+ group, which directs the entering group to the meta- position instead of ortho, and para.

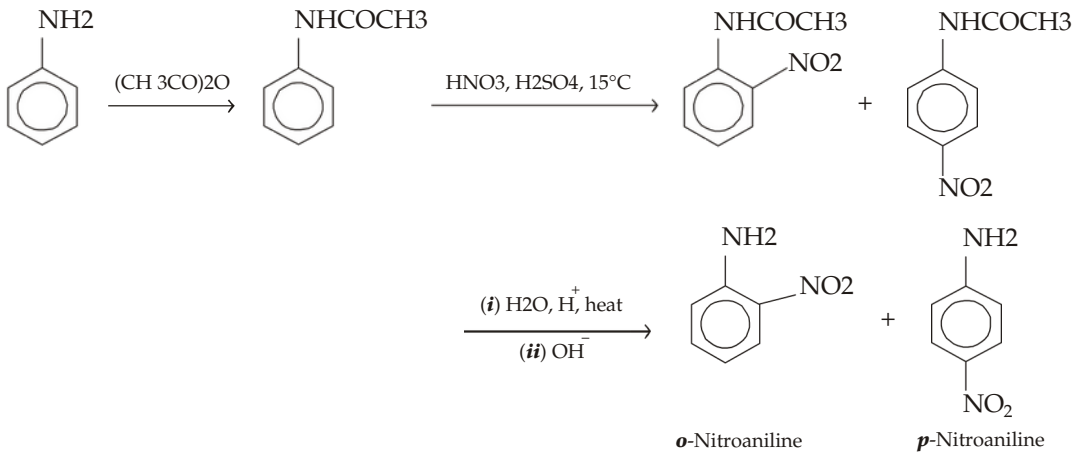


However, all these difficulties are overcome by protecting the amino group by acetylation, with either acetyl chloride or acetic anhydride. Acetylation converts —NH_2 group into —$NHCOCH_3$ group, which is less activating towards electrophilic aromatic substitution than the parent —NH_2 group.



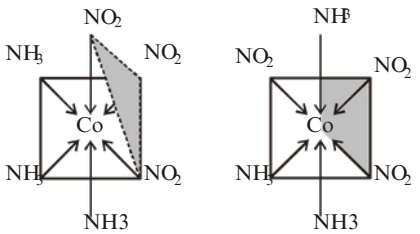
Aniline (electron pair can delocalize only to benzene ring making *o*, *p*-positions highly reactive)

Acetanilide Resonance in acetanilid due to amide group (note that electron pair on N can also delocalize to amide group, hence —$NHCOCH_3$ gp. becomes weak activator than the —NH_2 group)

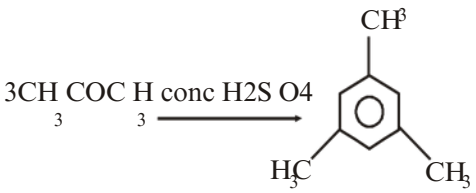


43. (c) The number of atoms of the ligands that are directly bound to the central metal atom or ion by coordinate bond is known as the coordination number of the metal atom or ion. Hence the coordination no. of the given

44. (a)compound will be 6. Comp leexxiesst ionf twthoe ge Mpeometrical forms which are named as facial A3B3 (fac-) and meridonal (mer-isomers). $Co(NH_3)_3(NO_2)_3$ may be represented in fac- and mer-isomeric forms as follows.



45. (c, d) Acetone on polymerisation give mesitylene



3 molecules of acetaldehyde produce paraldehyde $(C_3HCHO)_3$ and 4 molecules of it produce metaldehyde $(C_3HCHO)_4$.

46. (a)

47. (a) The most widely used method for preparing aromatic amines is the reduction of the nitro group to the amino group. This reduction can be achieved by catalytic hydrogenation, or most frequently with an acid and a metal (Fe, Zn, Sn) or a metal salt like SnCl2.

$$\underset{\text{Nitrobenzeneor}}{C_6H_5NO_2} \xrightarrow[\text{(i) Sn, HCl, (ii) OH}]{\text{H2, catalyst}} \underset{\text{Aniline}}{C_6H_5NH_2}$$

48. (a) The electronic configuration for Rb (37) is
Rb (37)
= 1s2 2s2 2p6 3s2 3p6 4s2 3d10 4p6 5s1

For 5s1, n = 5, $= 0$, m = 0, s1
2

49. (b) XeF4 disproportionates in water giving solid XeO3 on evaporation.

$$6XeF_4 \quad 12H2O \quad 2XeO_3 \quad 24HF \quad 4Xe \quad 3O_2$$

50. (b)Number of A ions in the unit cell

$= \frac{1}{8} \quad 8 \quad 1$

Number of B ions in the unit cell

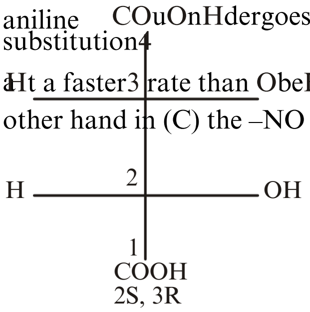
$= \frac{1}{2} \quad 6 \quad 3$

Hence empirical formula of the compound
$= AB_3$

51. (d)The electrical resistance of metals depends upon temperature. Electrical resistance decreases with decrease in temperature and becomes zero near the absolute temperature. Material in this state is said to possess super conductivity.

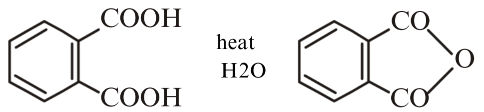
52. (a) An electron releasing group stablilises the carbocation by dispersing its positive charge and thus activates the ring while an electron-withdrawing group destabilises the carbocation by intensifying its positive charge and thus deactivates the ring. –NH 2 being electron releasing group releases electron and thus tend to neutralise positive charge of the ring and itself becomes somewhat positive. The –NO 2 group (an electron withdrawing group) intensifies positive charge on the ring and destabilises the carbocation and hence its formation is less than (B). Since no substituent is not present in benzene, its reactivity is more than (C). Hence nitrobenzene undergoes electrophilic substitution at a slower rate than benzene. Hence aniline undergoes electrophilic substitution at a faster rate than benzene. On the other hand in (C) the –NO

53. (c)



2S, 3R

54. (b) CH_2COOH | CH_2COOH $\xrightarrow[H_2O]{heat}$ CH_2CO | CH_2CO >O Succinic anhydride



Phthalic anhydride

Oxalic on heating produces formic acid.

55. (a) CH_2 | CH_2 + O = C(CH_3)(CH_3) ... CH_2 O R ... O R CH_2

56. (a) CH_3 C = C CH_3 H H cis-2-butene CH_3 H C = C H CH_3 trans-2-butene

57. (c) Aldehydes and Ketones containing -hydrogen undergo aldol condensation, since benzophenone does not have -hydrogen hence do not undergo aldol condensation whereas acetophenone show this reaction due to presence of -H atom.

58. (b)Isonitriles on reduction with $LiAlH_4$ give 2° amines

$R - N \equiv C \xrightarrow{LiAlH_4} RNHCH_3$

59. (c) Keratin

60. (c) For an isothermal process

$\Delta S = 2.303\, nR \log_{10} \frac{V_2}{V_1}$

$= 2.303 \times 1 \times 2 \log$

$= 4.6$ cal deg–1 mol–1

61. (b) Energy of activation for forward reaction (Ea) = 85 kJ/mol

Energy of activation for backward reaction = Ea –H = 85 – 20 = 65 kJ m–o1l

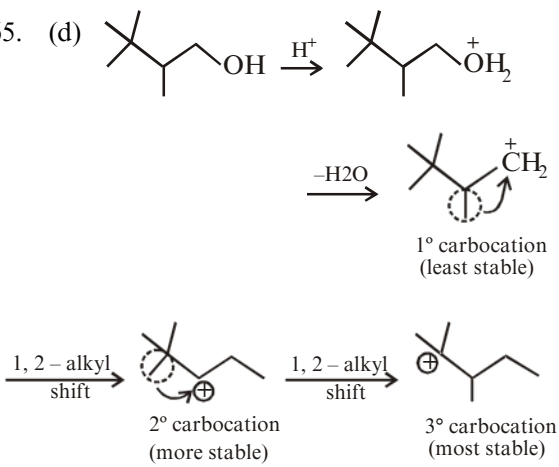
62. (a)Since the formation of amnonia is an exothermic reaction hence on increasing temperature, reaction will proceed in backward direction i.e. decreases. The amount of NH_3

63. (a) Atoms having half-filled and fully filled orbitals are comparatively more stable, hence more energy is required to remove

the electron from such atoms. Therefore group 15 have more I.E. than gp. 16 el em en ts. Because of +I effect, t-butyl group destabilises the carbanion.

64. (c)

65. (d)



66. (c)We know G° = – nFE°

$$E \quad \frac{G}{nF}$$

$$\frac{237.2\ 1000J}{2\ \ 96500} = 1.23\ V\ [\quad n = 2]$$

67. (b) Solubility S $\overset{\circ}{}_{AgCl}$ $1000k$ $\overset{\circ}{}_{Ag}$ 1000 $\overset{\circ}{}_{Cl}$ $2.6\ 10^{6}$

$$\frac{2.6\ 103}{63\ \ 67} \quad 2\ 10\ m5ol\ L \quad 1;\ Ksp = S\ 2$$

68. (c) For a reaction to be at equilibrium G = 0.
Since G H–T Sso at equilibrium
H – T S 0
or H TS
For the reaction

$$\frac{1}{2}X2 \quad \frac{3}{2}Y2 \qquad XY3; \qquad H \quad -30kJ$$

(given)
Calculating S for the above reaction, we get

$$S \quad 50 \quad \frac{1}{2} \quad 60 \quad \frac{3}{2} \quad 40\ JK\ 1$$

=50 – (30 + 60) JK–1 = – 40 –J1K
At equilibrium, TS H

[G 0]

T (–40) –30 1000 [1kJ 1000J]

or T $\frac{-30\ 1000}{-40}$ or 750 K

69. (b)

70. (d) $PCl_{5(g)} \rightleftharpoons PCl_{3(g)} + Cl_{2(g)}$

1 –

$= a \overset{x}{}$ (degree of dissociation)

Total moles =1– + + = 1 +

$$K_p \quad \frac{P_{PCl_3}\ PCl2}{P_{PCl5}} \quad \frac{p}{1} \quad \frac{1}{1} \quad \cdot p \quad \frac{1}{1} \quad p$$

$$1 \quad \frac{2}{1} \quad \frac{p}{2} \qquad K \quad P \qquad pKp^{1/2}$$

71. (b) RTlnK= -G° = T S°- H°;

$$\ln K \quad \frac{S}{R} \quad \frac{H}{RT}$$

Thus, a plot of ln K versus 1/T(abscissa) will be straight line with slope equal to

$$\frac{H}{R} \quad \text{and intercept} \quad \frac{S}{R}$$

72. (c)

$$\frac{(t_{1/2})_1}{(t_{1/2})_2} \quad \frac{a_2}{a_1}^{n\ 1} \quad ; \quad \frac{120}{8\ 10^{2}} \quad \frac{4\ 10^{2}}{}^{n\ 1} \quad ; n \quad 2$$

73. (c) From slow step :
rate = k2[A][B] ... . (i)
From fast step :

$$\frac{[A]2}{[A2]} \quad K_2 \qquad \text{or } [A] \quad ½Ke[A½] \quad .....(ii)$$

From (i) and (ii)

rate k2k½e [A2½] [B] k[A2]½[B]

74. (c) Using Arrhenius equation,

$$K \quad A.eRt, \text{ we get}$$

$$\log k \quad \log A \quad \frac{E_a}{2.303RT}$$

$\log k_1 \quad \log A \quad \frac{E_{a(1)}}{2.303RT}$ ....(i)

and $\log k_2 \quad \log A \quad \frac{E_{a(2)}}{2.303RT}$ ...(ii)

or $\log \frac{k_2}{k_1} \quad \frac{1}{2.303RT}[E_{a(1)} \quad E_{a(2)}]$

(from (i) and (ii))

$\frac{1}{2.303 \quad 8.314 \quad 300}(76000 \quad 57000)$

or $\log \frac{k_2}{k_1} \quad \frac{19000}{2.303 \quad 8.314 \quad 300}$

190

6.9 8.314

or $\frac{k_2}{k_1}$ 2000 [taking antilog]

75. (a) $\bar{v}$ RZ21 $\frac{}{22}$ $\frac{1}{32}$

= $\frac{R1149}{}$ = $\frac{5R}{36}$

76. (d) The products of the concerned reaction react each other forming back the reactants.

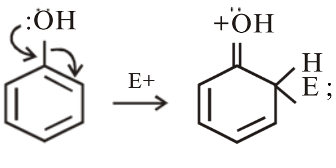
$XeF_6 \; 3H_2O \quad XeO_3 \; 6HF$

77. (c) Althou 6gHh5 iOnHbatswthos preroacdtuiocst ... and C different mechanism.

$C_6H_5 \; O \; CH_3 \xrightarrow{HI(g)} CH_3I \; C_6H_5OH$

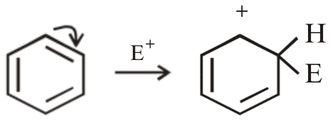
$C_6H_5 \; O \; CH_3 \xrightarrow[S_{N1}]{N_2 \text{ conc . HI}} CH_3I \; C_6H_5OH$

Remember that during N S1 reaction, CH_3 is formed because it is more stable than C_6H_5 .

78. (c) 

+ M effect in phenol activates benzene ring

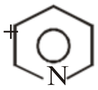
Oxonium ion (more stable)

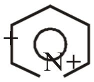


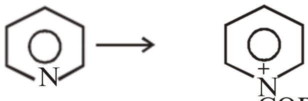
Carbonium ion (less stable)

High stability of oxonium ion (oxocation) is because here every atom (except H) has a complete octet of electrons, while in carbocations, carbon bearing positive charge is having six electrons.

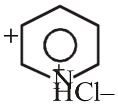
79. (c) Baeyer - Villiger oxidation involves the conversion of a cyclic ketone to a lactone, or an acyclic ketone into ester.

80. (c) $RCOCl + C_2H_5OH +$ 

$\longrightarrow RCOOC_2H_5 +$  HCl^-

$RCOCl +$ 

a better electrophile than RCOCl

$\xrightarrow{C_2H_5OH} RCOOC_2H_5 +$  HCl^-

PART - III (MATHEMATICS)

81. (b) $1 \quad y^2 \quad (x \quad e^{\tan^{-1} y})dydx \quad 0$

$(1 \quad y^2)dx \quad (e^{\tan^{1} y} \quad x)dy$

$\frac{dx}{dy} \quad \frac{e^{\tan 1 \, y}}{1 \quad y^2} \quad x$

$\frac{dx}{dy} \quad \frac{1}{1 \quad y^2}.x = \frac{e^{\tan 1 \, y}}{1 \quad 2y}$

Which is the linear different equation of the form $\frac{dx}{dy}$ RxS, where R and S are functions of y or constant (s)

$$\text{I.F} = e^{\int \frac{1}{1+y^2}\,dy} = e^{\tan^{-1}y}$$

Hence required solution is

$$x.(\text{I.F.}) = \int \frac{e^{\tan^{-1}y}}{1+y^2}(\text{I.F})dy$$

$$x.e^{\tan^{-1}y} = \int \frac{e^{\tan^{-1}y}}{1+y^2}(e^{\tan^{-1}y})dy$$

$$x.e^{\tan^{-1}y} = \int \frac{e^{2\tan^{-1}y}}{1+y^2}dy \qquad ...(1)$$

Put $t = \tan^{-1}y$

$$\frac{dt}{dy} = \frac{1}{1+y^2} \quad dt = \frac{1}{1+y^2}.dy$$

$$\int e^{2\tan^{-1}y}\frac{dy}{1+y^2} = \int e^{2t}.dt = \frac{e^{2t}}{2} + K$$

Hence equation (1) becomes,

$$xe^{\tan^{-1}y} = \frac{1}{2}e^{2t} + K$$

$$xe^{\tan^{-1}y} = \frac{1}{2}e^{2\tan^{-1}y} + K$$

$$2xe^{\tan^{-1}y} = e^{2\tan^{-1}y} + K$$

82. (a) $\vec{A} = \hat{i} + 2\hat{j} + \hat{k}$

$\vec{O} = -2\hat{i} + \hat{j} + \hat{k}$

Angle between faces OAB and ABC = Angle between AO and AC

If Q be the angle between AO and AC, then

$$\cos\theta = \frac{\vec{AO}.\vec{AC}}{|\vec{AO}||\vec{AC}|}$$

$$= \frac{1(-2) + 2(-1) + 1.1}{\sqrt{1+4+1}.\sqrt{4+1+1}} = \frac{-3}{6}$$

$$= \frac{1}{2} \quad \cos\theta = \cos 120$$

$\theta = 120°$

83. (c) Given ellipse : $\frac{x^2}{16} + \frac{y^2}{b^2} = 1$

Now $b^2 = a^2(1 - e^2)$

$b^2 = 16(1 - e^2)$, $\frac{b^2}{16} = 1 - e^2$

$e^2 = 1 - \frac{b^2}{16} = \frac{16 - b^2}{16}$ $\quad e = \frac{\sqrt{16 - b^2}}{4}$

Foci = $(ae, 0) = \left(\sqrt{16 - b^2}, 0\right)$

Given hyperbola : $\frac{x^2}{144} - \frac{y^2}{81} = \frac{1}{25}$

$$\frac{x^2}{\frac{12^2}{5}} - \frac{y^2}{\frac{9^2}{5}} = 1$$

Now, $b^2 = a^2(e^2 - 1)$

$$\frac{9^2}{5} = \frac{12^2}{5}(e^2 - 1)$$

$$\frac{9^2}{12} = e^2 - 1,$$

$$e^2 = 1 + \frac{81}{144} = \frac{144 + 81}{144}$$

$$e = \frac{15}{12} = \frac{5}{4}$$

Foci = $(ae, o) = (\pm 3, 0)$

Since foci of the given ellipse and hyperbola coincide, therefore

$\sqrt{16 - 2b} = 3 \quad 16 - b^2 = 9$

$b^2 = 7$

84. (a) $f'(3) = \tan\frac{3}{4} - \tan\frac{}{4} - 1$

85. (b)

Required probability

= P (First win) × P(First win) × P(Second win)

+ P(First Defeat) × P(First win) × P(Second win)

$$= \frac{1}{2}\frac{1}{2}\frac{1}{2} + \frac{1}{2}\frac{1}{2}\frac{1}{2} + \frac{1}{2}\frac{1}{2}\frac{1}{2} = \frac{1}{4}$$

86. (b) $a \quad b \quad c \quad 0$

$(a \quad b \; c)2 \; 0$

$|a|^2 \quad |b|^2 \quad |c|^2 \; 2(a.b \; b.c \quad c.a) \quad 0$

$9 + 4 + 1 + 2 \; (a.bb.c \quad c.a) \quad 0$

$a.b \quad b.c \quad c.a \quad 7$

87. (d) Let r (x) = f (x) . g (x)
= x2 . 2x = 2x3
r(x) = 6x2
Px u=t 06 x2 = 0,
Max r(x) = 2(2)3 = 16
or Max (f (x), g(x)) = 16

x	0	2
r(x)	0	16

$I(x) = \int_0^2 16dx$

I(x) = 16x20= 32 – 0 = 32

88. (b)B = ABA–1 (Given)
But B = BAA–A
ABA–1 = BAA–1 AB = BA
Now (A + B) (A – B) = A2 – AB + BA – B2
= A2 – AB + AB – B2[AB = BA]
= A2 – B2

89. (b) (1 + – 2)7 = (–2– 2)7 = (–22)7
= –128 (4)32 = – 128 2

90. (d) Here, r $2\hat{i}3\hat{j}\hat{k}$ i $2\hat{j}3\hat{k}$

r i $\hat{j}2\hat{k}$ and F i $\hat{j}$ $\hat{k}$

Then, the required moment is given by

r F i $\hat{j}$ $2\hat{k}$ i $\hat{j}$ $\hat{k}$

$\hat{k}$

$$= \begin{vmatrix} \hat{i} & \hat{j} & \\ 1 & 1 & 2 \\ 1 & 1 & 1 \end{vmatrix} \quad 3\hat{i} \; 3\hat{j}$$

Moment about given point =$3\hat{i}3\hat{j}$

91. (b) g (x). g(y) = g(x) + g (y) + g (x y) – 2 ...(1)
Put x = 1, y = 2, then
g (1). g(2) = g (1) + g (2) + g (2) – 2
5g (1) = g (1) + 5 + 5 – 2
4g (1) = 8 g(1) = 2

Put $y \quad \frac{1}{x}$ in equation (1) , we get

$g(x).g \; \frac{1}{x} \quad g(x) \quad g \; \frac{1}{x} \quad g(1) \quad 2$

$g(x).g \quad g(x) \quad g \; x \quad 2 \quad 2$

$[\quad g(1) \quad 2]$

This is valid only for the polynomial
g (x) = 1 + xn ... (2)
Now g (2) = 5 (Given)
1 + 2n = 5 [Using equation (2)]
+ 2n = 4, 2n = 4, –4
Since the value of 2n cannot be –Ve.
So, 2n = 4, n = 2
Now, put n = 2 in equation (2), we get
g (x) = 1 + x2

$\underset{x \quad 3}{Lt} \; g(x) \; = \underset{x \quad 3}{Lt} \; (1 \; x2) \quad = 1 + (3^2)$

= 1 + 9 = 10, – 8

92. (c) Any tangent to parabola y2 = 8x is y =

$mx \quad \frac{2}{m}$ ...(i)

It touches the circle x2y2 12x 4 0,
if the length of perpendicular from the centre (6, 0) is equal to radius $\sqrt{32}$.

$$\frac{6m \quad 2m}{\sqrt{m2 \quad 1}} \quad \sqrt{32}$$

$3m \quad 1m^2 \quad 8(m2 \quad 1)$

$(3m2 \; 1)2 \quad 8(m4 \; m2)$

$m4 \quad 2m^2 \quad 1 \quad 0 \quad m \quad 1$

Hence, the required tangents are y = x + 2 and y = –x – 2.

93. (b)Given ex $y \quad \sqrt{1 \quad y2}$

$ex \quad y \quad \sqrt{1 \quad y2}$

Squaring both side, we have
e2x + y2 – 2exy = 1 + y2
2ex y = e2x – 1

$$y \quad \frac{e^{2x}\ 1}{2e^{x}} \qquad y \quad \frac{1}{2}\ e^{x} \quad e^{x}$$

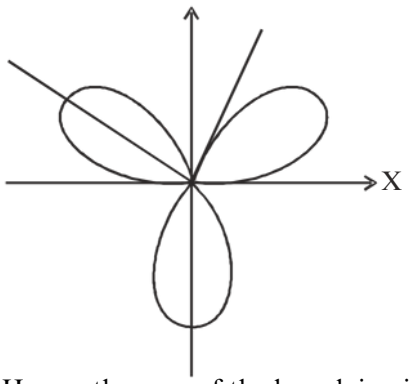
94. (d) If curve r = a sin 3

To trace the curve, we consider the following table :

3	0	$\frac{}{2}$		$\frac{3}{2}$	2	$\frac{5}{2}$	3
	0	$\frac{}{6}$	$\frac{}{3}$	$\frac{}{2}$	$\frac{2}{3}$	$\frac{5}{6}$	
r	0	a	0	a	0	a	0

Thus there is a loop between 0 & $\frac{}{3}$

as r varies from r = 0 to r = 0.



Hence, the area of the loop lying in the positive quadrant $\frac{1}{2}\int_{0}^{\frac{}{3}} r^{2}\,d$

$$\frac{1}{2}\int_{0}^{\frac{}{3}} \sin^{2} .13d$$

[On putting,3 d $\frac{1}{3}$d]

$$a^{2}\int_{0}^{\frac{}{6}} \sin^{2} d$$

$$a^{2}\int_{0}^{\frac{}{6}} \frac{1 \cos 2}{2} d \qquad \cos 2 \quad 1 \quad 2\sin$$

$$a^{2}\int_{0}^{\frac{}{6}} \sin^{2} d \qquad \frac{a^{2}}{12}\left[\frac{\sin 2}{2}\right]_{0}^{\frac{}{6}}$$

$$\frac{a^{2}}{12}\left[\frac{}{2}\right]_{0}^{\frac{}{6}} \qquad \frac{a^{2}}{24}$$

95. (a)Replacing each hexadecimal digit by the corresponding 4-digit binary numeral, we have

(ABC D16) = (1010 1011 1100 1101)2

96. (c)Let the norm2’a1. ’tl hcaeut te‘stq tuhaet ipoanr aobf othlae at the point ‘t

at $(at_1^2, 2at_1)$ is $y + t_1x = 2at_1 + at_1^3$

Since it passes through the point 2‘t’ i.e $(at_2^2, 2at_2)$

$2at_2 + at_1t_2^2 = 2at_1 + at_1^3$

$2a(t_1 - t)2 + at_1(t_1^2 - t_2^2) = 0$

$2 + t_1(t_1 + t_2) = 0 \quad (t_1 \quad t_2 \quad 0)$

$2 + t_1^2 + t_1t_2 = 0$

$t_1t_2 = -(t_1^2 + 2) \qquad t_2 \qquad t_1 \quad \frac{2}{t_1}$

97. (b) $s = t^3 - 12t^2 + 6t + 8$

$$\frac{ds}{dt} \quad 3t^2 \quad 24t \quad 6$$

$$\frac{d^2s}{dt^2} \quad 6t \quad 24$$

Acceleration = 0

$6t - 24 = 0$

$t = 4$

R e3qi×u (r4ed)2 –e l2o4c i×ty $\frac{ds}{}$ 4 = + 6

= 48 – 96 + 6 = 42 udntitts4

X = a . b

98. (a)

99. (b) Let $\cos^{1}\frac{1}{8}$, where $0 < < \frac{}{2}$.

$$2\cos^{1}\frac{1}{8} \quad \frac{1}{2}$$

$$\cos^{1}\frac{1}{8} \quad 2\cos^{1}\frac{1}{2}$$

Now, $\cos^{1}\frac{1}{8} = \cos = \frac{1}{8}$

$$2\cos^{2}\frac{}{2} \quad 1 \quad \frac{1}{8}$$

$\cos 2\frac{9}{16} \quad \cos\frac{3}{4}$

$[\ 0 < \frac{}{2\ 4}$, so $\cos\frac{3}{4}]$

100. (c Two constraints are x 0, y 0 and the third one will be of the type ax + byc .

101.) Let y denote the number of bacteria at any instant t then according to the question

(b $\frac{dy}{dt} \propto y \quad \frac{dy}{y} = k\,dt$ ... (i)

)

k is the constant of proportionality, taken to be + ve on integrating (i), we get

$\log y = kt + c$ ... (ii)

c is a parameter. let0 y be the initial number of bacteria

i.e., at t = 0 using this in (ii), $c = \log_0 y$

$\log y = kt + \log 0y$

$\log \frac{y}{y_0} = kt$ ...(iii)

$y = y_0 \ \frac{10}{100}\ y_0 \quad \frac{11y_0}{10}$0,when t = 2

So, from (iii), we get $\log \frac{11y_0}{10}{}_0 \quad k(2)$

$k = \frac{2\log 1110}{}$ ... (iv)

Using (iv) in (iii) $\log \frac{y}{y_0} \quad \frac{1}{2} \quad \log 1110\ t$

... (v)

let the number of bacteria become 1, 00, 000 to 2,00,000 in 1t hours. i.e., y = 2y0 when t = 1t hours. from (v)

$\log \frac{2y_0}{y_0} \quad \frac{1}{2} \quad \log 1110\ t \quad t1 = \frac{2\log 2}{\log 11\ 10}$

Hence, the reqd. no. of hours $= \frac{2\log 2}{\log 1110}$

102.(b) Consider $\sin 1\ \frac{1}{\sqrt{5}} \quad \cot 13$ ...(i)

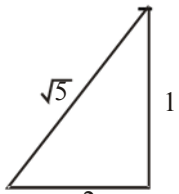
We have, $\sin 1\ \frac{1}{\sqrt{5}} \quad \cot 12$

From equation (i), we have

$\cos^{-1} 2 + \cot^{-1} 3 = \tan 1 \frac{1}{2} \quad \tan 11$

$= \tan 1\ 1\ 2\ \frac{\frac{1}{3} \quad \frac{1}{}}{11\ 2 \ldots 3 \quad 1}$

$= \tan 1 \frac{5/6}{61\ 6}$ $\tan 11 = \frac{}{4}$



103.(b)We have,

abcd = cos (2 + 2 + 2 +2) + i sin (2 + 2 + 2 +2)

$\sqrt{abcd}$ = [cos (2 + 2 + 2 +2) + i sin (2 + 2 + 2 +2)]1/2

or $\sqrt{abcd}$ = cos (+ + +) + i sin (+ + +).... (1)

[De Moivre's Theorem]

$\frac{1}{\sqrt{abcd}}$ = cos (+ + +) – i sin (+ + +) .... (2)

Adding (1) and (2), we obtain

$\sqrt{abcd} \quad \frac{1}{\sqrt{abcd}} = 2\cos(+++)$

104. (a)Standard deviation $\sqrt{npq} \quad 0$

Now mean = np =25 and q < 1

So $\sqrt{npq} \quad \sqrt{np} \quad 5$

0 5

105.(d)Number of ways

= [(3C $4C_3$ $5C_3$ $6C_3$ $7C_3$) 2 $^8C3$]2

= 392

106.(d) rank (A B) rank (A) andrank (A B) rank (B)

Therefore rank (A Bm)i n (rank A, rank B)

107. (a) Let A (a, 0, 0), B (0, b, 0), C (0, 0, c), then equation of the plane is $\frac{x}{a} \quad \frac{y}{b} \quad \frac{z}{c} = 1$

Its distance from the origin, $\frac{1}{a2} \quad \frac{1}{b2} \quad \frac{1}{c2} \quad \frac{1}{p2}$ ... (i)

If (x, y, z) be centroid ofA BC, then

$x = \frac{a}{3}, y = \frac{b}{3}, z = \frac{c}{3}$ ... (ii)

Eliminating a,b,c from (i) and (ii) required locus is

$x^{-2} + y^{-2} + z^{-2} = 9p^{-2}$

108. (c) There are 26 red cards and 26 black cards i.e., total number of cards = 52
P(both cards of different colours)
= P(B) P(R) + P(R) P(B)

$$= \frac{26}{52}\frac{26}{51} + \frac{26}{52}\frac{26}{51}$$

109. (a) The equation of the hyperbola is

$$x^2 - 2y^2 - 2x - 8y + 1 = 0$$

or $(x-1)^2 - 2(y+2)^2 + 6 = 0$

or $\frac{(x-1)^2}{6} - \frac{(y+2)^2}{3} = 1$

or $\frac{(y+2)^2}{3} - \frac{(x-1)^2}{6} = 1 \quad ...(1)$

or $\frac{Y^2}{3} - \frac{X^2}{6} = 1$

where $X = x - 1$ and $Y = y + 2$ ...(2)

The centre = (0, 0) in the X-Y co-ordinates.

The centre = (1, –2) in the x-y co-ordinates using (2).

If the transverse axis be of length 2a, then $a = \sqrt{3}$, since in the equation (1) the transverse axis is parallel to the y-axis.

If the conjugate axis is of length 2b, then $b = \sqrt{6}$.

But $b^2 = a^2(e^2 - 1)$

$6 = 3(e^2 - 1), \quad e^2 = 3$ or $e = \sqrt{3}$.

The length of the transverse axis $= 2\sqrt{3}$.

The length of the conjugate axis $= 2\sqrt{6}$.

Latus rectum $= \frac{2b^2}{a} = \frac{2 \cdot 6}{\sqrt{3}} = 4\sqrt{2}$

110. (c) Probability of getting a blue ball at any draw

$$= p = \frac{10}{1}$$

P [getting a blue ball 4th time in 7th draw]
= P [getting 3 blue balls in 6 draw] × P [a blue ball in the 7th draw].

$$= {}^6C_3 \left(\frac{1}{2}\right)^3 \left(\frac{1}{2}\right)^3 . \frac{1}{2}$$

$$= \frac{6 \cdot 5 \cdot 4}{1 \cdot 2 \cdot 3} \cdot \frac{1}{2^7} = 20 \cdot \frac{1}{32} \cdot \frac{5}{4} = \frac{5}{32}$$

111. (d) For the first circle centre = (3, 7)

Radius $r_1 = \sqrt{3^2 + 7^2 - 48} = \sqrt{10}$

For the second circle, centre (3, 0); radius $r_2 = 3$

So $|r_1 - r_2| < d$ (distance between the centres)

Circle don't cut and hence the number of common tangents = 4.

112. (d) We have,

$\cos^2\theta + \sin\theta + 1 = 0 \quad 1 - \sin^2\theta + \sin\theta + 1 = 0$

$$\sin\theta = -1 \left(\text{ sin } \frac{\pi}{2}\right) = \frac{3}{2}$$

$$\theta = \frac{5\pi}{4}, \frac{7\pi}{4}$$

113. (c) $\lim_{x \to 0} f(x) = \lim_{x \to 0}[(1+x)^{1/x}]^2 = e^2 = f(0)$

114. (d) $\log y = \frac{x}{\log x} \log 2$

$$\frac{d}{dx}\left(\frac{y}{x^e}\right) = 0$$

115. (d)
$$\int \frac{dx}{x^2(x^4+1)^{3/4}} = \int \frac{dx}{x^5\left(1+\frac{1}{x^4}\right)^{3/4}}$$

Put $1 + \frac{1}{x^4} = t \quad \frac{4}{x^5}dx = dt$

So, integral is

$$I = \int \frac{1}{t^{3/4}} dt = t^{1/4} + c = \left(1 + \frac{1}{x^4}\right)^{1/4} + c$$

116. (a) The number of words starting from A are 5! = 120

The number of words starting from I are 5!

= 120

The number of words starting from KA are 4! = 24

The number of words starting from KI are 4! = 24

The number of words starting from KN are 4! = 24
The number of words starting from KRA are 3! = 6
The number of words starting from KRIA are 2! = 2
The number of words starting from KRIN are 2! = 2
The number of words starting from KRISA are 1! = 1
The number of words starting from KRISNA are 1! = 1
Hence, rank of word 'KRISNA
= 2(120) + 3(24) + 6 + 2(2) + 2(1) = 324

117. (b) The lines are $\frac{x}{6} \quad \frac{y}{6} \quad \frac{2}{1} \quad \frac{z}{1}$

and $\frac{x \;\; 1}{12} \quad \frac{y}{6} \quad \frac{z}{1}$

Her e,

$a_1 \quad 2\hat{j} \; \hat{k}, b_1 \; 6\hat{i} \; 6\hat{j} \; \hat{k}, a_2 \quad \hat{i},$

$b_2 \quad 12\hat{i} \; k6\hat{j}\hat{}$

$$b_1 \quad b_2 \quad \begin{vmatrix} \hat{i} & j & k \\ 6 & 6 & 1 \\ 12 & 6 & 1 \end{vmatrix} \quad 12\hat{i} \; 18\hat{j} \; 36\hat{k}$$

Shortest distance $= \frac{\left| a_2 \quad a \quad .b_1 \quad b_2 \right|}{\left| b_1 \quad b_2 \right|}$

$$= \frac{\left| \hat{i} \quad 2\hat{j} \; \hat{k} \; . \quad 12\hat{i} \quad 18\hat{j} \; 36\hat{k} \right|}{\sqrt{12^2 \quad 18^2 \quad 36^2}}$$

$$= \frac{\left| 12 \quad 36 \quad 36 \right| \quad 84}{\sqrt{1764}} \quad \frac{}{42} \quad 2$$

118. (b) Given $f(x) = 2 - |x - 5|$

Domain of f(x) is defined for all real values of x.

Since, $|x - 5| \quad 0 \quad -|x - 5| \quad 0$

$2 - |x - 5| \quad 2 \quad f(x) \quad 2$

Hence, range of f(x) is $(-, 2]$.

119. (a) If A and B are two sets having m and n elements such that

$$1 \; n \; m = \sum_{r1}^{n} (1)^{n-r} C_r r^m$$

Number of surjection from A to B

$$= \sum_{r \; 1}^{n} (1)^{2r-2} \quad C_{(r)4}$$

$= (-1)^{2-1} \; 21C \; (1)^4 + (-1)^{2-2} \; 2C = (2)^{-4} \; 2 + 16$
$= 14$

120. (d) Let $I = \int_a^b xf(x)dx$

Leta + b – x = z – dx = dz
When x = a, z = b and when x = b, z = a

$$I \quad \int_b^a (a \quad b - z) f(z)dz$$

$$I \quad (a \quad b) \int_a^b f(x)dx - \int_b^a x \, f(x)dx$$

$$I \; (a \; b) \int_b^a f(x)dx - I;$$

$$2I \; (a \; b) \int_b^b f(x)dx$$

$$\text{Hence, } I \quad \frac{a \quad b}{2} \int_a^b f(x)dx$$

PART - IV (ENGLISH)

121 (b)
122 (a)
123 (d)
124 (a)

"Whether" is correct because the question concerns a choice not a condition. With the expression "the number of" a singular verb is needed and hence "was" is correct. "Liable" is used in expressions such as "liable to prosecution" and not for expressions of possibility.

125 (b)